

# OXYGEN-RELATED POINT DEFECTS IN SILICON AND GERMANIUM

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## Abstract

A modelling study of several oxygen related defects in silicon and germanium crystals is reported. These include radiation and thermally activated defects. The problem of thermal donor formation is revised in detail. Here we report the properties of the simple interstitial oxygen complexes, their diffusivity and clustering properties, culminating with a novel model for the thermal double donor defects (TDD). The model is also extended to the hydrogen-related shallow thermal donor family, STD(H). According to the model, electrons from over-coordinated oxygen atoms with a donor level lying above that of a stress-induced state, are transferred to the latter. This picture is analogous to that of an externally doped quantum-dot.

*To my parents,  
Adélio and Maria Isabel.*

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# List of Publications

1. J. Coutinho, R. Jones, P. R. Briddon, S. Öberg, L. I. Murin, V. P. Markevich, J. L. Lindström, *Thermal Double Donors as Quantum Dots*, to appear in Phys. Rev. Lett.
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4. J. Coutinho, R. Jones, P. R. Briddon, S. Öberg, L. I. Murin, V. P. Markevich, J. L. Lindström, *Interaction between hydrogen and the interstitial carbon-oxygen center in Si*, to appear in Physica B.
5. L. I. Murin, V. P. Markevich, J. L. Lindström, V. V. Litvinov, J. Coutinho, R. Jones, P. R. Briddon, S. Öberg, *Isotopic effects on local vibrational modes of thermal double donors in Si and Ge*, to appear in Physica B.
6. J. Coutinho, R. Jones, P. R. Briddon, S. Öberg, *Oxygen and dioxygen centers in Si and Ge: Density-functional calculations*, Phys. Rev. B **62**, 10824 (2000).
7. V. P. Markevich, L. I. Murin, M. Suezawa, J. L. Lindström, J. Coutinho, R. Jones, P. R. Briddon, S. Öberg, *Observation and theory of the VOH<sub>2</sub> complex in silicon*, Phys. Rev. B **61**, 12964 (2000).
8. J. Coutinho, R. Jones, P. R. Briddon, S. Öberg, *Formation and diffusivity of small oxygen aggregates in Si and Ge*, Proceedings of the Second ENDEASD Workshop, (Stockholm, 2000).



9. V. P. Markevich, L. I. Murin, M. Suezawa, J. L. Lindström, J. Coutinho, R. Jones, P. R. Briddon, S. Öberg, *Local vibrational mode bands of VOH complexes in silicon*, Physica B **273-274**, 300 (1999).

# Introduction

Almost all silicon wafers used for micro-electronic circuits are prepared by the Czochralski technique (Abe, 1985). Here, polysilicon nuggets and doping elements are melted in a silica crucible. A crystal seed dipped into the melt is pulled and rotated, such that dislocation-free  $\sim 200$  mm diameter ingots are obtained. Because of the high oxygen solubility ( $\sim 10^{18}$  cm $^{-3}$ ) in the melt (Hrostowski and Kaiser, 1959), interstitial oxygen defects ( $O_i$ ) are normally present in Cz-Si wafers as a super-saturated solution. Despite these concentrations, interstitial oxygen was known to be electrically harmless and located at a bond-centre site (Kaiser *et al.*, 1956). The main reason why oxygen is a beneficial impurity in Si, stems from two main reasons. (i) oxygen greatly enhances mechanical resistivity of Si crystals, and (ii) in the form of SiO $_2$  precipitates, it is used as a getterer for highly undesirable transition metals (*intrinsic gettering*) (Shimura, 1994).

In the mid 1950's, when semiconductor silicon (Si) was still in its early stages of development for electronic applications, it was found that the conductivity of Si samples grown by the Czochralski (Cz) method could be dramatically enhanced after heat treatments around 450°C (Fuller *et al.*, 1954). Soon after, it was realised that oxygen-related donor defects were at the origin of this enhancement. The thermal activation of these defects lead to their labelling as *thermal donors* (TD) (Fuller and Logan, 1957; Kaiser *et al.*, 1958). Concentrations of TD defects could in fact reach orders of magnitude higher than that of the dopant — presenting a serious threat to device performance after heat-treatment fabrication processes.

When Fuller *et al.* (1954) discovered the conductivity enhancement, they also noticed a recovery of the initial resistivity following heat treatments above 600°C. This is basically what we call a *donor-killing* process, employed to break the TD defects.

Today we know about the existence of several thermally activated oxygen-related donor families. In general they are referred to as thermal donors (TD), comprising thermal double donors (TDD), shallow thermal donors (STD), new donors (ND), and other less studied classes like the ultra-shallow thermal donors (USTD) (Jones, 1996). Here we are

particularly interested in the first two families. In the last 30 years, more than any other problem on defects in semiconductor, the most varied and sophisticated experiments were applied to study thermal donors. Unfortunately, the technique that could unravel the most structural and chemical information — magnetic resonance — resulted in structureless or extremely weak signals. However, in the recent years, considerable progress has been made with infra-red absorption spectroscopy. The revelation of local vibrational modes associated with oxygen aggregates (Lindström and Hallberg, 1996; Öberg *et al.*, 1998) (including the O-dimer and early TDD members), gives us an unprecedented opportunity to review the problem theoretically.

The most important features of TDD's established so far include (Jones, 1996):

- Up to 17 TDD(N) members were identified, with  $0 \leq N \leq 16$ ;
- The donor states are those of an effective-mass theory double donor, with first and second ionisation levels at  $\sim 70$  and  $\sim 150$  meV, monotonically decreasing with  $N$ ;
- The generation kinetics and the maximum concentration of donors depend on the oxygen content;
- Initial TDD growth is mediated by a 1.7 eV activation barrier, which decreases to 1.1 eV for the later species;
- The overall donor symmetry is  $C_{2v}$ , although small deviations were reported after high-field resonance experiments;
- Short heat treatments above  $600^\circ\text{C}$  destroys the electrical activity of TDD's, which is accompanied by an increase of  $O_i$  content;
- Impurities like carbon, nitrogen, hydrogen and aluminium are known to influence the production of the donors.
- Electron irradiation and hydrostatic pressure strongly enhance TDD formation rates
- Each TDD member appears to produce at least three infra-red active local vibrational modes at  $\sim 1000$ ,  $\sim 720$  and  $\sim 580$   $\text{cm}^{-1}$ .

Inspection of the list given above, lead us to conclude that despite a half-century of active debate, the general picture is well understood, but details by which thermal donor defects form, as well their chemical nature and structure remain obscure. Therefore we have a fundamental problem to be solved. Most importantly, (i) following the current steady rate of device miniaturisation, soon the presence of a mere few donors and low dopant uniformity will certainly affect the overall device performance; (ii) formation of oxygen-free (*denuded*) zones demand a detailed knowledge of the early stages of oxygen aggregation. Being aware that oxygen-rich Ge crystals or Ge rich Cz-Si also suffers from the thermal donor problem, it is expected that SiGe technology, a promising material to operate in the microwave region, will inherit the knowledge from its group-IV constituents. These are some convincing facts driving the semiconductor community to study the problem.

This thesis is divided into six chapters, starting with a description of the method, culminating with models for TDD and STD defects. Chapter 2 presents a review of the relevant experimental details involved in the TDD problem. These include electron paramagnetic resonance (EPR) and electron-nuclear double resonance (ENDOR), photoluminescence (PL), deep-level transient spectroscopy (DLTS) and infra-red (IR) absorption. In Chapter 3 we review previous modelling of vacancy-oxygen defects. This is an issue not only somewhat indirectly related to the TDD problem, but also serving as a *benchmark* test for the method employed here. Chapter 4 discusses the very early oxygen aggregates in Si and Ge, with oxygen diffusivity and self-interstitial ejection as central issues. In the two final chapters, the TDD and STD models are discussed, where calculated observables are directly compared with the experimental observations.

# Chapter 1

## Theoretical framework

### 1.1 The many-body problem

In the absence of external fields, the Schrödinger equation for a non-relativistic and stationary problem involving a set of  $N_e$  electrons and  $N_n$  atomic nuclei can be written as

$$\hat{\mathcal{H}}\Psi = E\Psi. \quad (1.1)$$

Here, the Hamiltonian  $\hat{\mathcal{H}}$  contains the usual kinetic and potential terms<sup>1</sup>,

$$\begin{aligned} \hat{\mathcal{H}} = & -\frac{1}{2} \sum_i^{N_e} \nabla_i^2 - \sum_\alpha^{N_n} \frac{1}{2M_\alpha} \nabla_\alpha^2 + \\ & + \frac{1}{2} \sum_{\substack{i,j=1 \\ i \neq j}}^{N_e} \frac{1}{|\mathbf{r}_i - \mathbf{r}_j|} - \sum_{i,\alpha=1}^{N_e, N_n} \frac{Z_\alpha}{|\mathbf{r}_i - \mathbf{R}_\alpha|} + \frac{1}{2} \sum_{\substack{\alpha,\beta=1 \\ \alpha \neq \beta}}^{N_n} \frac{Z_\alpha Z_\beta}{|\mathbf{R}_\alpha - \mathbf{R}_\beta|}, \end{aligned} \quad (1.2)$$

where  $M_\alpha$ ,  $Z_\alpha$  and  $\mathbf{R}_\alpha$  represent the mass, charge and location of the  $\alpha$ -th nucleus, and  $\mathbf{r}_i$  the  $i$ -th electron coordinate. The total wavefunction  $\Psi$  from Equation 1.1 is therefore

---

<sup>1</sup>All quantities are expressed in atomic units (unless otherwise specified). In this system of units,  $\hbar$ ,  $e$ ,  $m$  and  $4\pi\epsilon_0$  are taken to be unity, where  $e$ ,  $m$  and  $\epsilon_0$  are the electron charge, electron mass, and the permittivity of vacuum respectively. The unit of length is 0.529 Å, and the unit of energy is 27.211 eV.

a function of  $N_n$  nuclei coordinates, plus  $N_e$  electron spatial and spin coordinates,  $\mathbf{r}_i$  and  $s_i$  respectively,

$$\Psi \equiv \Psi(\mathbf{r}_1, s_1, \dots, \mathbf{r}_{N_e}, s_{N_e}; \mathbf{R}_1, \dots, \mathbf{R}_{N_n}). \quad (1.3)$$

Disregarding any analytical solution for 1.1 (only known for problems such as the hydrogen and  $\text{He}^+$  atoms (Schiff, 1955)), one can appreciate the fact that  $\Psi$  depends on  $3N_n + 4\sum_{\alpha} Z_{\alpha}$  scalar variables, and even the simplest problem with potential technological applications is simply intractable even when using the fastest computers available. This is the stage where one is forced to develop a theoretical framework by trading approximations for an useful output, keeping the standards of accuracy as high as possible.

## 1.2 Born-Oppenheimer approximation

By noting that the electron mass is  $\sim 2000$  times lighter than that of a neutron or proton, we expect electrons to respond *instantaneously* to atomic motion. In other words, the shape of an electron-only wavefunction will adapt adiabatically to nuclear motion. The idea proposed by Born and Oppenheimer (1925), was that a first order ansatz

$$\Psi(\mathbf{r}; \mathbf{R}) = \psi_{\mathbf{R}}(\mathbf{r}) \phi(\mathbf{R}) \quad (1.4)$$

for the total wavefunction  $\Psi$ , where  $\psi$  and  $\phi$  are separate electronic and nuclear wavefunctions, is a good solution for the ground state of the Hamiltonian in 1.2. The variables  $\mathbf{r}$  and  $\mathbf{R}$  represent now all electronic and nuclear degrees of freedom. As no magnetic fields are considered, we drop the spin indexes for the moment. The subscript on  $\psi$  stresses the fact that the electronic wavefunction depends on  $\mathbf{R}$  in a parametric way.

Substituting 1.4 in 1.2, one obtains

$$\begin{aligned} \widehat{\mathcal{H}}\psi_{\mathbf{R}}(\mathbf{r})\phi(\mathbf{R}) &= (E_n + E_e)\psi_{\mathbf{R}}(\mathbf{r})\phi(\mathbf{R}) - \\ &- \sum_{\alpha}^{N_n} \frac{1}{2M_{\alpha}} [\phi(\mathbf{R})\nabla_{\alpha}^2\psi_{\mathbf{R}}(\mathbf{r}) + 2\nabla_{\alpha}\psi_{\mathbf{R}}(\mathbf{r}) \cdot \nabla_{\alpha}\phi(\mathbf{R})]. \end{aligned} \quad (1.5)$$

with  $E_n$  and  $E_e$  as eigenvalues from the separate nuclear and electronic problems respectively,

$$\left(\widehat{\mathcal{T}}_n + \widehat{\mathcal{V}}_{nn}\right)\phi = E_n\phi \quad (1.6)$$

$$\left(\widehat{\mathcal{T}}_e + \widehat{\mathcal{V}}_{ee} + \widehat{\mathcal{V}}_{en}\right)\psi = E_e\psi. \quad (1.7)$$

Equations 1.6 and 1.7 include all kinetic ( $\widehat{\mathcal{T}}$ ) and potential ( $\widehat{\mathcal{V}}$ ) terms in the many-body Hamiltonian in 1.2. Subscripts n and e label the nuclear and electronic terms respectively. Now making use of the hypothesis — for  $M_{\alpha} \gg 1$ , the total energy  $E$  is given by the independent electronic and nuclear eigenvalues  $E_e$  and  $E_n$ , with the ansatz in 1.4 as eigenstate. Hence, a stationary state of a many-body system is normally defined after finding  $\psi$  for a set of fixed atomic positions (see Section 1.3).

From now on, we will then focus on the electronic problem and its Hamiltonian,

$$\widehat{\mathcal{H}} = \widehat{\mathcal{T}}_e + \widehat{\mathcal{V}}_{ee} + \widehat{\mathcal{V}}_{en} = \quad (1.8)$$

$$= -\frac{1}{2} \sum_i^{N_e} \nabla_i^2 + \frac{1}{2} \sum_{\substack{i,j=1 \\ i \neq j}}^{N_e} \frac{1}{|\mathbf{r}_i - \mathbf{r}_j|} - \sum_{i,\alpha=1}^{N_e, N_n} \frac{Z_{\alpha}}{|\mathbf{r}_i - \mathbf{R}_{\alpha}|}. \quad (1.9)$$

It is worth noting that when electron-nuclear coupling is strong, the Born-Oppenheimer breaks down. This is also the case for Jahn-Teller systems, where  $\nabla_{\alpha}\psi$  is large enough as to impose a nuclear distortion due mixing of the nuclear and electronic wavefunctions.

### 1.3 Variational principle

There are two main methods used to attain stationary solutions for the Hamiltonian in 1.8 — grid and variational methods. The first integrates the Schrödinger equation using discretisation methods, and the second uses a variational principle. In this method, a carefully chosen subspace  $\{\phi_1, \dots, \phi_M\}$  of Hilbert space is used to span an approximation  $\Psi_{\text{app}}$  of the ground-state wavefunction  $\Psi_0$  as

$$\Psi_0 \approx \Psi_{\text{app}} = \sum_i^M c_i \phi_i. \quad (1.10)$$

Now using the expectation value for the total energy  $E$  written as a functional of the wavefunction  $\Psi$ ,

$$E[\Psi] = \frac{\langle \Psi | \hat{\mathcal{H}} | \Psi \rangle}{\langle \Psi | \Psi \rangle}, \quad (1.11)$$

gives the approximate total energy

$$E_{\text{app}} = E[\Psi_{\text{app}}] = \frac{\sum_{i,j=1}^M c_i^* c_j H_{ij}}{\sum_{i,j=1}^M c_i^* c_j S_{ij}}, \quad (1.12)$$

with  $H_{ij} = \langle \phi_i | \hat{\mathcal{H}} | \phi_j \rangle$  and  $S_{ij} = \langle \phi_i | \phi_j \rangle$ . These are referred as the Hamiltonian and overlap matrix elements. Stationary states then follow from the condition that the derivative of  $E_{\text{app}}$  with respect to  $c_i$  vanishes, leading to

$$\sum_{j=1}^M (H_{ij} - E_{\text{app}} S_{ij}) c_j = 0, \quad \text{for } i = 1, \dots, M, \quad (1.13)$$

or in a more compact form, to the following generalised eigenvalue equation:

$$\mathbf{H} \cdot \mathbf{c} = E_{\text{app}} \mathbf{S} \cdot \mathbf{c}. \quad (1.14)$$



The lowest eigenvalue from the above secular equation is higher than (or equal to) the true ground state energy  $E_0$ . Including more basis functions into our set, the subspace becomes larger, and consequently  $E_{\text{app}}$  will decrease or become constant. This is known as the Rayleigh-Ritz variational principle (Kemble, 1932; MacDonald, 1933).

**Theorem 1 (Variational principle)** *The energy  $E_{\text{app}}$  computed from an approximate  $\Psi_{\text{app}}$  wavefunction is an upper bound to the true ground-state energy  $E_0$ . Full minimisation of the functional  $E[\Psi]$  with respect to the all allowed basis functions will give the true ground state  $\Psi_0$  and energy  $E_0 = E[\Psi_0]$ ; that is,*

$$E_0 = \min_{\Psi} E[\Psi]. \quad (1.15)$$

The variational principle is used in almost all electronic structure calculations where the ground state  $\Psi_0$  is the goal. This is also the case for density-functional methods.

## 1.4 Hartree-Fock method

The Hartree-Fock (HF) method (Fock, 1930; Roothaan, 1951; Slater, 1965; Stoneham, 1975) uses a variational approach in which the wave function of the many-electron system has the form of an anti-symmetrised product of one-electron wavefunctions (therefore taking into account the Pauli exclusion principle). These are elegantly written in the form of Slater determinants (Slater, 1929),

$$\Psi_{\text{SD}}(\mathbf{x}_1, \dots, \mathbf{x}_N) = \frac{1}{\sqrt{N!}} \det \begin{bmatrix} \psi_1(\mathbf{x}_1) & \cdots & \psi_N(\mathbf{x}_1) \\ \vdots & \ddots & \vdots \\ \psi_1(\mathbf{x}_N) & \cdots & \psi_N(\mathbf{x}_N) \end{bmatrix}, \quad (1.16)$$

where  $\mathbf{x}_i$  includes spatial and spin coordinates of the  $i$ -th electron, and  $\psi_i$  are one-electron *spin-orbitals*, which we assume to be orthogonal. The wavefunctions  $\Psi_{\text{SD}}$  carries the exchange properties of a many-body wavefunction. The determinantal form ensures its

anti-symmetry as exchanging two electron coordinates affects  $\Psi_{\text{SD}}$  by a factor of  $-1$ , and  $\Psi_{\text{SD}} = 0$  if two electrons with the same coordinates are present.

Considering  $\Psi_{\text{SD}}$  as a solution of the Hamiltonian in 1.8, one arrives at an expectation value for the total energy,

$$E = \sum_i^N H_i + \frac{1}{2} \sum_{i,j=1}^N (J_{ij} - K_{ij}), \quad (1.17)$$

where  $H_i$  is the one-electron integral

$$H_i = \int \psi_i^*(\mathbf{x}) \left[ -\frac{1}{2} \nabla_i^2 - \sum_{\alpha=1}^{N_n} \frac{Z_\alpha}{|\mathbf{r}_i - \mathbf{R}_\alpha|} \right] \psi_i(\mathbf{x}) d\mathbf{x}, \quad (1.18)$$

and  $J_{ij}$  and  $K_{ij}$  are called *Hartree* and *exchange integrals*. These are given by the following two-electron terms,

$$J_{ij} = \iint \psi_i(\mathbf{x}) \psi_i^*(\mathbf{x}) \frac{1}{|\mathbf{r} - \mathbf{r}'|} \psi_j(\mathbf{x}') \psi_j^*(\mathbf{x}') d\mathbf{x} d\mathbf{x}' \quad (1.19)$$

$$K_{ij} = \iint \psi_i(\mathbf{x}) \psi_j^*(\mathbf{x}) \frac{1}{|\mathbf{r} - \mathbf{r}'|} \psi_i(\mathbf{x}') \psi_j^*(\mathbf{x}') d\mathbf{x} d\mathbf{x}', \quad (1.20)$$

where integration in  $\mathbf{x}$  represent spatial integration and spin summation, i.e.,  $\mathbf{x} = (\mathbf{r}, s)$ . The reason why the two-electron summation in 1.17 include the  $i = j$  term is because  $J_{ii} = K_{ii}$ . Hence, this summation is composed of an electron-electron repulsion term, plus an exchange component representing spin-correlation effects.

Minimisation of 1.17 subject to the orthogonality condition  $\langle \psi_i | \psi_j \rangle = \delta_{ij}$ , gives the Hartree-Fock equations (McWeeny, 1989; Thijssen, 1999),

$$\hat{\mathcal{F}} \psi_i(\mathbf{x}) = \sum_{j=1}^N \epsilon_{ij} \psi_j(\mathbf{x}), \quad (1.21)$$

with  $\hat{\mathcal{F}}$  known as Fock operator, and defined as

$$\widehat{\mathcal{F}} = \widehat{h} + \widehat{j} - \widehat{k} \quad (1.22)$$

with  $\langle \psi_i | \widehat{h} | \psi_i \rangle = H_i$  (see Equation 1.18), and

$$\widehat{j}(\mathbf{x})f(\mathbf{x}) = \sum_{k=1}^N \int \psi_k^*(\mathbf{x}')\psi_k(\mathbf{x}')\frac{1}{|\mathbf{r} - \mathbf{r}'|}f(\mathbf{x}) d\mathbf{x}' \quad (1.23)$$

$$\widehat{k}(\mathbf{x})f(\mathbf{x}) = \sum_{k=1}^N \int \psi_k^*(\mathbf{x}')f(\mathbf{x}')\frac{1}{|\mathbf{r} - \mathbf{r}'|}\psi_k(\mathbf{x}) d\mathbf{x}' \quad (1.24)$$

for  $f(\mathbf{x})$  an arbitrary function. The matrix  $\epsilon$  consists of Lagrange multipliers from the minimisation procedure. Its diagonal elements are obtained after integrating the Fock operator, i.e.,

$$\epsilon_i \equiv \epsilon_{ii} = \langle \psi_i | \widehat{\mathcal{F}} | \psi_i \rangle = H_i + \sum_{j=1}^N (J_{ij} - K_{ij}), \quad (1.25)$$

which after summation and compared with Equation 1.17, gives the total energy as

$$E = \sum_{i=1}^N \epsilon_i - \frac{1}{2} \sum_{i,j=1}^N (J_{ij} - K_{ij}). \quad (1.26)$$

Usually, in a computer implementation of the HF method, the spin-orbitals  $\psi_i$  are expanded as a linear combination of atomic orbitals. Hence, as in Section 1.3, after carefully choosing a set of  $M$  functions  $\phi_i(\mathbf{x})$ , we define

$$\psi_j(\mathbf{x}) = \sum_i^M c_{ij}\phi_i(\mathbf{x}) \quad (1.27)$$

The Fock equation then takes a matrix form, and therefore we end with a generalised eigenvalue problem similar to that of Section 1.3, called *Roothaan equation* (Roothaan, 1951),

$$\mathbf{F} \cdot \mathbf{c}_j = \epsilon_j \mathbf{S} \cdot \mathbf{c}_j, \quad (1.28)$$

where  $\mathbf{S}$  is again the  $M \times M$  overlap matrix  $S_{ij} = \langle \phi_i | \phi_j \rangle$ . The above equation is solved in a self-consistent way, until the wavefunction convergence is attained along with the total energy.

The physical meaning of the eigenvalues from the Roothaan equation was developed by Koopmans (1934).

**Theorem 2 (Koopmans' theorem)** *Assuming that the eigenstates  $\mathbf{c}_j$  do not vary after removal of one electron from the system, the ionisation energy  $I_m$  of the  $m$ -th electron is given by  $I_m = -\epsilon_m$ .*

An important consequence of the Koopmans theorem is the ability to calculate excited states within the HF method.

In this section, we did not include the spin in the formulation. This leads to *open-shell* or *unrestricted systems*, as opposed to the spin-averaged *closed-shell systems*. In the open-shell formalism, the non-local matrix elements  $J_{ij}$  and  $K_{ij}$  must couple both spins by explicitly summing over this degrees of freedom. For a review on this issue, see Slater (1965); Schaefer (1977); Lawley (1987).

The Hartree-Fock theory has one major short-coming — the wavefunction does not incorporate electron-correlation, i.e., the spin-orbitals do not have a functional dependence on  $\mathbf{r}_i - \mathbf{r}_j$ . This problem can be solved by expressing  $\Psi$  as a linear combination of Slater determinants, known as Configuration Interaction (CI) method. Unfortunately, this carries a serious computational cost as the number of determinants grows rapidly with the size of the system. Also the evaluation of the  $J_{ij}$  and  $K_{ij}$  matrix elements is a demanding computational task — its CPU-time scales with the fourth power of basis size. In fact, even with help of modern supercomputers, only systems with a few tens of atoms can be studied (see for example Pisany *et al.* (1988); Kantorovich *et al.* (2000)).

## 1.5 Density-Functional Theory

As we saw in Section 1.4, application of the all-electron HF method is prohibitive in extended systems. The non-local character of both the  $\hat{j}$  and  $\hat{k}$  operators (their values at  $\mathbf{r}$  depend on another coordinate  $\mathbf{r}'$ ), complicates the evaluation of the  $J_{ij}$  and  $K_{ij}$  matrix elements. Most of today's state-of-the-art electronic structure calculations in solids use Density-Functional Theory (DFT) (Hohenberg and Kohn, 1964; Kohn and Sham, 1965). This theory has been extensively reviewed over the last two decades (Lundqvist, 1983; Parr and Yang, 1989; Jones and Gunnarsson, 1989). Here the total energy  $E \equiv E[n]$  is a functional of the electronic charge density  $n(\mathbf{r})$ , as opposed to the wavefunction in HF. It is then proposed,

$$E[n] = F[n] + \int v_{\text{ext}}(\mathbf{r})n(\mathbf{r}) d\mathbf{r}, \quad (1.29)$$

with  $v_{\text{ext}}$  representing an external potential to which the electrons are subject. This includes the ion-electron interaction and other fields. The functional  $F$  is universal (system-independent), and accounts for electronic kinetic energy, electron-correlation and exchange-correlation.

**Theorem 3 (First Hohenberg-Kohn theorem)** *The external potential is determined, within a trivial additive constant, by the electron density  $n(\mathbf{r})$  (Hohenberg and Kohn, 1964).*

In DFT, the number of electrons, the external potential, and therefore the ground-state wavefunction along with all its properties are uniquely defined by the charge density.

**Theorem 4 (Second Hohenberg-Kohn theorem)** *For a trial density  $\tilde{n}(\mathbf{r})$ , such that  $\tilde{n}(\mathbf{r}) \geq 0$  and  $\int \tilde{n}(\mathbf{r}) d\mathbf{r} = N$  (Hohenberg and Kohn, 1964),*

$$E_0 \leq E[\tilde{n}]. \quad (1.30)$$

This expression is analogous to Equation 1.15, and is the basis of a variational principle. Hence in this case

$$E_0 = \min_{\tilde{n}} E[\tilde{n}]. \quad (1.31)$$

The striking feature of this method, is that despite the huge simplification of adopting the charge density as the variational variable, no approximations are made. Still as in HF, the exchange-correlation contribution to the functional  $F$  is a non-local quantity.

### 1.5.1 Kohn-Sham equations

In DFT, an effective independent particle Hamiltonian is arrived at, leading to the following Schrödinger set of one-electron equations (Kohn and Sham, 1965):

$$\left[ -\frac{1}{2}\nabla^2 - \sum_{\alpha} \frac{Z_{\alpha}}{|\mathbf{r} - \mathbf{R}_{\alpha}|} + \int \frac{n(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d^3\mathbf{r}' + \frac{\delta E_{xc}[n]}{\delta n(\mathbf{r})} \right] \psi_{\lambda}(\mathbf{r}) = \epsilon_{\lambda} \psi_{\lambda}(\mathbf{r}). \quad (1.32)$$

with the density  $n$  obtained by summing up all  $N$  occupied spin-orbital states,

$$n(\mathbf{r}) = \sum_{\lambda=1}^N |\psi_{\lambda}(\mathbf{r})|^2. \quad (1.33)$$

The first three terms of Equation 1.32 are the kinetic energy, the external potential imposed by the ions, and the Hartree energy respectively. The fourth term lumps together all remaining many-body effects in the form of an exchange-correlation functional. One main pillar of DFT is the existence of an universal  $E_{xc}$  density functional (depending only on the electron density  $n$ ), leading to the knowledge of the *exact* ground-state total energy and density.

The total energy functional for the many-electron system is given by (Parr and Yang, 1989)

$$E[n] = \sum_{\lambda=1}^N \epsilon_{\lambda} - J[n] + E_{\text{xc}}[n] - \int V_{\text{xc}}[n] n(\mathbf{r}) d\mathbf{r}. \quad (1.34)$$

In Equation 1.34, the Hartree energy and the exchange-correlation potential ( $J$  and  $V_{\text{xc}}$  respectively) are written as

$$J[n] = \frac{1}{2} \int \frac{n(\mathbf{r})n(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r} d\mathbf{r}' \quad (1.35)$$

$$V_{\text{xc}}[n] = \frac{\delta E_{\text{xc}}[n]}{\delta n(\mathbf{r})}. \quad (1.36)$$

The exact form of  $E_{\text{xc}}$  is however unknown, but some standard approximations are currently used. In fact, improvements to this functional is still one of today's active research areas (Doren *et al.*, 2001; M. A. L. Marques, 2001).

Equations 1.32 and 1.33 – known as *Kohn-Sham equations* (Kohn and Sham, 1965), are solved in a self-consistent loop. We first choose a trial charge density and solve Equation 1.32. The resulting eigenvectors are fed into 1.33 to build a new charge-density, which is the input to Equation 1.32. This process (*self-consistency cycle*) keeps going until the charge-density does not appreciably change.

The above formalism neglects any spin-dependence. Apart from the  $E_{\text{xc}}$  correlation functional, all terms are linear with respect to the charge density. The extension of the Kohn-Sham scheme to spin-polarised systems was given by von Barth and Hedin (1972); Rajagopal and Callaway (1973). Here we define the charge density as being made up of spin-up and spin-down densities,  $n(\mathbf{r}) = n_{\uparrow}(\mathbf{r}) + n_{\downarrow}(\mathbf{r})$ , but we still have a non-local  $E_{\text{xc}}[n_{\uparrow}(\mathbf{r}), n_{\downarrow}(\mathbf{r})]$ . This will be discussed later. Note that we have now one-electron spin-orbitals, and therefore the total charge density is

$$n(\mathbf{r}) = \sum_{\lambda=1}^{N/2} \sum_s |\psi_{\lambda}(\mathbf{r}, s)|^2. \quad (1.37)$$

### 1.5.2 The exchange-correlation functional

In DFT, the exchange-correlation energy is accounted by the  $E_{xc}[n]$  non-local density functional. This functional is however unknown. Several approaches have been taken to overcome this problem. The most common is to assume a local density approximation (LDA), or local spin-density approximation (LSDA) for non-zero spin systems (Kohn and Sham, 1965; von Barth and Hedin, 1972; Perdew and Zunger, 1981). Here, it is assumed that the exchange-correlation energy is local. Normally this energy is separated into exchange and correlation parts, where in LSDA notation,

$$E_{xc}[n_{\uparrow}, n_{\downarrow}] = E_x[n_{\uparrow}, n_{\downarrow}] + E_c[n_{\uparrow}, n_{\downarrow}]. \quad (1.38)$$

The exchange functional is linear with respect to  $n$ , and its analytic form is given by (von Barth and Hedin, 1972),

$$E_x[n_{\uparrow}, n_{\downarrow}] = -\frac{3}{2} \left( \frac{3}{4\pi} \right)^{1/3} \left( n_{\uparrow}^{4/3} + n_{\downarrow}^{4/3} \right). \quad (1.39)$$

The correlation part is however more complicated. In the high-density regime, perturbation theory yields one expression (Perdew and Zunger, 1981), while in the low-density regime, a Green function quantum Monte Carlo method yields another (Ceperley, 1978; Ceperley and Alder, 1980). A simple parameterised functional form is then fitted to the numerical results. Several parameterisations are available, namely those from Perdew and Zunger (1981) (PZ), Vosko *et al.* (1980) (VWN) and Perdew and Wang (1992) (PW). First-order expansions of  $E_{xc}$  in the density were also developed. This is the generalised gradient approximation (GGA), and includes terms depending on  $\nabla n$  (Perdew, 1991; Perdew *et al.*, 1996*a,b*).

## 1.6 Pseudopotentials

It is well known that the standard properties of molecules or solids are governed by valence electrons. Electrons in core-states behave much like those in isolated atoms, creating a



screening effective potential — a *pseudopotential*, seen by the valence electrons. The idea behind the pseudopotential method is to split the all-electron Coulomb operator into two separate parts, i.e., one that takes care of the inner core-states, and the other dealing with valence states. This allows us to drop matrix elements regarding the core-electrons, and focus only on few remaining ones. Detailed information on the pseudopotential method has been extensively reported (Harrison, 1966; Brust, 1968; Stoneham, 1975; Heine, 1970; Pickett, 1989).

Two main reasons justify this approach, i) a full electron potential implies large total energies, therefore leading to large errors when comparing similar systems, ii) the number of basis functions required to fit all states (especially those at the core) would become prohibitively large, and affordable expansions would carry catastrophic consequences to accuracy of the total energy.

Obviously the utilisation of pseudopotentials has implications. Some assumptions (or approximations) are made, namely i) the *frozen core approximation* which assumes the core states to be unperturbed when the atom is transferred to a specific environment, and ii) the *small core approximation* where one assumes negligible overlap between core and valence states.

### 1.6.1 Basic formulation

Transferability *measures* the quality of a pseudopotential. That is, a pseudopotential will be transferable if it can reproduce the properties of the valence electrons, in a wide range of different problems. To accomplish this, the pseudopotential must be constructed by stripping off valence electrons from the atom, leaving behind an *ionic-pseudopotential* (Heine, 1970). Within the density-functional framework,

$$\widehat{V}_{\text{ion}}^{\text{ps}}(\mathbf{r}) = \widehat{V}^{\text{ps}}(\mathbf{r}) - \int \frac{n^{\text{ps}}(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' - \widehat{V}_{\text{xc}}[n(\mathbf{r})], \quad (1.40)$$

with

$$n^{\text{ps}}(\mathbf{r}) = \sum_{\lambda} |\psi_{\lambda}^{\text{ps}}(\mathbf{r})|^2. \quad (1.41)$$

In equations 1.40 and 1.41,  $\widehat{\mathcal{V}}^{\text{ps}}$  is the pseudopotential of the neutral atom and  $n^{\text{ps}}$  the charge-density from the valence states. Note that in 1.40 we not only subtract a classic Coulombic term, but also all exchange-correlation interactions  $\widehat{\mathcal{V}}_{\text{xc}}$  between the valence electrons (Pickett, 1989). In this thesis, the pseudopotentials of Bachelet, Hamann and Schlüter are used (Hamann *et al.*, 1982). These were tabulated by Bachelet *et al.* (1982) for elements between H and Pu.

## 1.7 Boundary-conditions and basis functions

The DFT code implementation used in this work has important features which need to be described. Among these is the use of a real-space Gaussian type basis set (Jones and Briddon, 1999). The choice of the boundary conditions has also important consequences. Here we treat the problem using supercells, involving Brillouin-zone (BZ) integration and reciprocal-space expansions using a Fourier-transformation (Briddon, 1999; Coutinho *et al.*, 2000b). We start by defining a supercell.

### 1.7.1 The supercell

Let us assume a crystallographic material with a unit cell defined by its unit vectors  $\mathbf{a}_i$ , with  $i = 1, 2$  and  $3$ , volume  $v_0$ , and containing a set of  $n_a$  atoms located at  $\mathbf{r}_j$  ( $j = 1, \dots, n_a$ ) from the origin of the unit cell. The Bravais lattice points are then given by  $\mathbf{l}_n = \sum_i n_i \mathbf{a}_i$ . Reciprocal-space unit vectors  $\mathbf{G}_i$  are then automatically defined as

$$\mathbf{G}_i = 2\pi \frac{\mathbf{a}_j \times \mathbf{a}_k}{\mathbf{a}_i \cdot (\mathbf{a}_j \times \mathbf{a}_k)} \quad (1.42)$$

with  $i, j, k = 1, 2, 3$ .

A supercell is defined by the linear transformation  $\mathbf{W}$  with integer elements  $W_{ij}$ , operating on  $\mathbf{a}_i$ ,

$$\mathbf{A}_j = \sum_{i=1}^3 W_{ij} \mathbf{a}_i, \text{ and } W = \det(\mathbf{W}). \quad (1.43)$$

The larger cell with unit vectors  $\mathbf{A}_j$  is a *supercell* with volume  $\Omega = v_0 W$ , and define a lattice of points  $\mathbf{L}_\mathbf{n} = \sum_i n_i \mathbf{A}_i$  for all integers  $n_i$ . Its reciprocal space unit-vectors  $\mathbf{g}_j$  define a unit cell  $W$  times smaller than that of the  $\mathbf{G}_j$  vectors, i.e.,

$$\mathbf{g}_j = \sum_{i=1}^3 L_{ij}^{-1} \mathbf{G}_i \quad (1.44)$$

with  $L_{ij}^{-1}$  representing the elements of  $\mathbf{L}^{-1}$ . The supercell contain  $N_a = n_a W$  atoms, and their location  $\mathbf{R}_i$  ( $i = 1, \dots, N_a$ ) can be defined by any set of  $N_a$  independent atomic positions  $\mathbf{R}_i$ ,

$$\mathbf{R}_i = \mathbf{l}_\mathbf{n} + \mathbf{r}_k, \text{ for all } \mathbf{R}_i - \mathbf{R}_j \neq \mathbf{L}_\mathbf{m}. \quad (1.45)$$

In the expression above,  $k$  can take any value between  $1 \leq k \leq n_a$ , and the index  $\mathbf{n}$  can be any integer vector. The important point is that no two atomic positions (say  $\mathbf{R}_i$  and  $\mathbf{R}_j$ ), may differ by a lattice vector  $\mathbf{L}_\mathbf{m}$ .

Inserting a defect in the supercell has important consequences. The basis vectors  $\mathbf{A}_i$  now form a conventional crystal with a smallest possible unit cell with volume  $\Omega$ , filled with atoms located at  $\mathbf{R}_i$ . The goal is to model defects in a crystalline environment. However, as a consequence of periodicity, a defect image will be located in each cell. Note that it does not matter where we place the defect — for example, displacing a substitutional impurity by  $\delta \mathbf{r}$  implies that all images will be displaced by the same vector. However, if the supercell is not adequate in terms of size and shape, spurious effects can take place in the form of defect-image coupling through elastic, Coulombic, dipolar and quadrupolar interactions.

One of the implications of using an LDA exchange-correlation functional is the underestimation (by  $\sim 50\%$ ) of the band-gap in semiconductors. If the unit cell is not large enough, mixing between defect-related gap states with the band extrema may be considerable. Hence, special attention must be paid to band-bending effects in gap states, especially for the shallow ones.

In the cluster approach, we do not have defect-image interaction, but different problems occur. The most important is defect-surface interaction. Unlike the supercell method, the total electric dipole may depend on the location of the defect (Jones and Briddon, 1999).

### 1.7.2 Basis functions

We define a set of Bloch basis functions  $B_{\mathbf{k}i}(\mathbf{r})$  that are built from a set of Cartesian-Gaussian functions  $\phi_i$  centred at  $\mathbf{R}_i$ , over  $N_L$  the lattice vectors  $\mathbf{L}_n$ ,

$$B_{\mathbf{k}i}(\mathbf{r}) = \frac{1}{\sqrt{N_L}} \sum_{\mathbf{L}_n} \phi_i(\mathbf{r} - \mathbf{R}_i - \mathbf{L}_n) e^{i\mathbf{k}\cdot\mathbf{L}_n}. \quad (1.46)$$

with  $\mathbf{k}$  as a reciprocal-space vector. The localised orbitals are given by

$$\phi_i(\mathbf{r}) = (x - R_{ix})^{l_1} (y - R_{iy})^{l_2} (z - R_{iz})^{l_3} e^{-a_i(\mathbf{r}-\mathbf{R}_i)^2}, \quad (1.47)$$

with  $s$ -,  $p$ - or  $d$ -like orbitals corresponding to  $\sum_i l_i = 0, 1$  or  $2$ , and with  $l_i \geq 0$ . The Kohn-Sham orbitals  $\psi_{\mathbf{k}\lambda}$  are then expanded over all  $B_{\mathbf{k}i}$  basis functions,

$$\psi_{\mathbf{k}\lambda}(\mathbf{r}) = \sum_i c_{\mathbf{k}\lambda,i} B_{\mathbf{k}i}(\mathbf{r}) \quad (1.48)$$

with the  $\mathbf{k}\lambda$  pair labelling the state. The charge-density is readily obtained as

$$n(\mathbf{r}) = \sum_{i,j,\mathbf{k}} b_{ij}(\mathbf{k}) B_{\mathbf{k}i}^*(\mathbf{r}) B_{\mathbf{k}j}(\mathbf{r}), \quad (1.49)$$

$$b_{ij}(\mathbf{k}) = \sum_{\lambda} f_{\mathbf{k}\lambda} c_{\mathbf{k}\lambda,i}^* c_{\mathbf{k}\lambda,j}, \quad (1.50)$$

where  $f_{\mathbf{k}\lambda}$  is the occupancy of the  $\mathbf{k}\lambda$  state. This should be 2 for a filled level and 0 for an empty one.

The advantage of using Gaussian-like functions is that their related integrals can be analytically found, and in contrast with oscillating basis functions, they can be made as to quickly vanish away from  $\mathbf{R}_i$  (Jones and Briddon, 1999). However, they are not orthogonal, and over-completeness can induce numerical instabilities.

### 1.7.3 Brillouin-zone sampling

In the supercell method, the calculation of physical quantities (as for example the total energy, charge density, density of states, etc), require integrations over the Brillouin-zone (BZ). The integrand function  $f(\mathbf{k})$  is periodic in reciprocal space, and has no simple analytic form. To avoid numerical integration over a dense mesh, several schemes were developed. As proposed by Baldereschi (1973) and Chadi and Cohen (1973), one or a set of  $N$  *special*  $\mathbf{k}_i$ -points can be used to obtain the average  $\bar{f}$  over the BZ, where

$$\bar{f} = \frac{\Omega}{(2\pi)^3} \int f(\mathbf{k}) d\mathbf{k} \approx \frac{1}{N} \sum_i^N f(\mathbf{k}_i). \quad (1.51)$$

Despite the obvious advantages of this method over a full integration, it provided no obvious way of checking the convergence of the calculations. A clearer scheme was proposed by Monkhorst and Pack (1976); Pack and Monkhorst (1977) (MP). The main advantages of their method are its simplicity, and convergence is verifiable. Here we define the following sequence of variables<sup>2</sup>,

$$u_i = (2i - I - 1)/2I, \quad (i = 1, \dots, I) \quad (1.52)$$

$$u_j = (2j - J - 1)/2J, \quad (j = 1, \dots, J) \quad (1.53)$$

$$u_k = (2k - K - 1)/2K, \quad (k = 1, \dots, K), \quad (1.54)$$

---

<sup>2</sup>In the original paper,  $I = J = K$  is imposed, and for a particular  $I$  the scheme is normally referred as MP- $I^3$ . However, here we extend the method such it is best suitable for non-cubic BZ cells

with the integers  $I, J$  and  $K \geq 1$  defining a grid of  $I \times J \times K$  points in the reciprocal space given by

$$\mathbf{k}(i, j, k) = u_i \mathbf{g}_1 + u_j \mathbf{g}_2 + u_k \mathbf{g}_3. \quad (1.55)$$

Now let us assume  $F, G$  and  $H$  to be point-groups for the Wigner-Seitz cell, Brillouin-zone and crystal respectively, with respective order  $g_F, g_G$  and  $g_H$ . Consequently,  $H \subseteq G \subseteq F$ . Note that as  $G$  must have time-reversal symmetry,  $G = H \times i$  where  $i$  is the inversion operation.

The MP scheme, uses the following recipe:

1. Define the initial grid  $\mathbf{k}(i, j, k)$  for a given set of  $I, J$  and  $K$  integers;
2. Generate a star from each  $\mathbf{k}(i, j, k)$  vector using symmetry operations from the lattice point group  $F$ ;
3. Eliminate all redundant  $\mathbf{k}$  vectors, by leaving only one irreducible representative — the *special  $\mathbf{k}$ -point*. This is done by folding each star within the BZ point-group  $G$ , and ensuring that it does not lie outside the BZ;
4. Each special  $\mathbf{k}_n$ -point is associated with a weighting factor  $w_n$ . These  $w_n$ 's are directly related to the representativity of  $\mathbf{k}_n$  in the BZ, i.e., with the order  $g_n$  of its site symmetry in within the BZ;

$$w_n = g_G/g_n \quad (1.56)$$

For example, in a crystal with  $C_{2v}$  point-group and cubic lattice, the BZ has  $D_{2d}$  symmetry. If the principal axis is along the  $z$ -axis, the  $\mathbf{k}$  vector  $(0, 0, 1/4)$  (with  $C_{2v}$  site symmetry) has a weighting factor  $w = 8/4 = 2$ , corresponding to the equivalent  $(0, 0, 1/4)$  and  $(0, 0, -1/4)$  vectors.

Finally, the as in 1.51, the average  $\bar{f}$ , or the integral of  $f$  over the BZ with volume  $(2\pi)^3/\Omega$ , is simply given by

$$\bar{f} = \frac{\Omega}{(2\pi)^3} \int f(\mathbf{r}) d\mathbf{r} \approx \frac{\sum_n w_n f(\mathbf{k}_n)}{\sum_n w_n}. \quad (1.57)$$

#### 1.7.4 Reciprocal-space basis

Although a real-space basis set is used to expand the Kohn-Sham orbitals, the periodic boundary conditions provide the opportunity to work on reciprocal-space as well. Several quantities are more efficiently evaluated in  $\mathbf{k}$ -space. This is the case of the Hartree (including the local pseudopotential), and exchange-correlation energies. As functionals of the charge density, they are periodic on the BZ. Their Fourier transformation is then a series over reciprocal lattice vectors. Obviously, the quality of the transformation is strictly dependent on the grid of  $\mathbf{g}$ -vectors. In practice a uniform grid of vectors inside a sphere of radius  $g_{\text{cut}}$  that defines a *cut-off energy* is used,

$$E_{\text{cut}} = \frac{1}{2} g_{\text{cut}}^2. \quad (1.58)$$

Normally, this energy is increased until the total energy has attained a converged value. We will return to this issue in Section 1.9.

#### 1.7.5 Ewald summations

Evaluation of the Coulombic and dipolar interactions in crystals (including the Madelung energy), involves calculating conditionally converging sums, i.e., its final value depends on the order in which the terms are summed. The problem lies in the fact that a series like  $1/r^p$  over  $r$  (with  $p \leq 2$ ), converge very slowly as  $r$  goes to infinity. To solve this problem, Ewald (1921) proposed a method in which the series is split into a fast-converging and slowly-converging parts,

$$\sum_L \frac{1}{r_L^p} = \sum_L \frac{\text{erfc}(\alpha r_L)}{r_L^p} + \sum_L \frac{\text{erf}(\alpha r_L)}{r_L^p}. \quad (1.59)$$

Evaluation of the first term is straightforward as  $\operatorname{erfc}(x)$  converges to zero when  $x \rightarrow \infty$ . The last term, slowly converging in real-space, is Fourier transformed, and as a consequence its terms are now *sort-ranged* in reciprocal space. The parameter  $\alpha$  controls the transition between the real-space and reciprocal-space summations. Although the analytical result does not depend on the choice of  $\alpha$ , in practice this is not true as a consequence of the summations being taken over a finite set of lattice vectors. An extensive treatment of this method was given by Leeuw *et al.* (1980).

## 1.8 Calculation of observables

The density functional theory method is a ground-state theory. By definition, excited states are not accessible as the Kohn-Sham eigenstates are not electronic wavefunctions. They are a set of basis functions from which the electron density  $n$  is expanded. This is the price that it must be paid when writing the Hamiltonian as a functional of  $n$ . Nevertheless, many observables can be calculated. These include ground-state structures, electron density, solubilities, electrical levels, vibrational modes, elastic properties, migration barriers, etc.

In this section we discuss how these are obtained, and the experiments (later described in Chapter 2), they are to be compared.

### 1.8.1 Local structure - forces

As we saw in Subsection 1.5.1, the Kohn-Sham equations must be solved self-consistently. The self-consistent charge-density  $n$  is obtained when its Kohn-Sham orbitals give rise to the same potential used to obtain  $n$ . We then say that *self-consistency* has been reached. Once  $n$  is known, the force  $\mathbf{F}_\alpha$  acting on atom  $\alpha$  can be obtained as  $-\nabla_\alpha E$ , where  $E$  is the total energy. This can be understood as a consequence of the following theorem (Epstein *et al.*, 1967):



**Theorem 5 (Hellmann-Feynman theorem)** *Let  $\zeta$  be a parameter in the Hamiltonian and  $\Psi_\zeta$  an eigenstate of  $\hat{\mathcal{H}}$ . Then*

$$\frac{\partial E}{\partial \zeta} = \left\langle \Psi \left| \frac{\partial \hat{\mathcal{H}}}{\partial \zeta} \right| \Psi \right\rangle. \quad (1.60)$$

We can now apply this theorem to evaluate the forces acting in every atom. These are extremely important in finding the ground state structure of a set of atoms. They provide the necessary input for the algorithm that optimises the structure (called *relaxation*), with respect to the total energy. Here all atoms are moved along the direction of the force that it is acting on it, until all of them are smaller than a specified value.

The atomic structure is commonly measurable with diffracted X-rays or electrons (see for example Kisielowski (2001)). Experimental support for a particular structure may however lie in spectroscopic data which is directly related to the local atomic arrangement. These include hyperfine interactions, vibrational frequencies, gap-states, piezospectroscopic-tensors, etc.

### 1.8.2 Formation energies and occupancy levels

The chemical potential  $\mu_X$  is defined to be the derivative of the Gibbs free energy  $G = E + PV - TS$  for a given phase with respect to the number of particles of type  $X$ :  $\mu_X = \partial G / \partial n_X$  (Reif, 1965; Flynn, 1972). Here,  $X$  might represent an atomic species, or electrons. In thermodynamic equilibrium  $\mu_X$  must be the same in all phases in contact, so it can be considered as the free energy per particle. The  $PV$  term can be neglected for pressures involved in solid-state reactions, and hence the formation energy  $E_f$  of a crystal with a neutral defect can be expressed as

$$E_f = E_D - \sum_X n_X \mu_X - TS \quad (1.61)$$

where  $E_D$  is the total energy of the crystal with the defect, formed by bringing together

$n_X$  particles of species  $X$ . Chemical potentials can be considered as the energy  $X$  in a standard thermodynamic state.

Now if the defect possesses gap states, it can assume different charge states. Therefore, the formation energy of a charged defect must include a term with the electron chemical potential  $\mu_e$ . As we are dealing with solids, a natural choice is to lock  $\mu_e$  to the Fermi level  $E_F$ . Therefore it is convenient to define  $\mu_e = E_v + E_F$ , where  $E_v$  is the top of the valence band. The formation energy  $E_f(q)$  of the crystal with the defect in the charge state  $q$  is therefore

$$E_f(q) = E_D(q) - \sum_X n_X \mu_X + q(E_v + E_F) \quad (1.62)$$

where the entropy term from 1.61 is neglected. This is not always the best approximation especially at high temperatures. Equation 1.62 allows us to estimate several thermodynamic properties. These include solubilities, defect concentrations subject to the charge neutrality condition, occupancy levels, etc (Baraff and Schlüter, 1985; Qian and Martin, 1988; Northrup, 1989).

For example, the location of a  $(q/q + 1)$  level is given by the position of the Fermi-level for which the neutral and charged defects have the same formation energy. This is simply done by extracting  $E_F$  from the equation  $E_f(q) = E_f(q + 1)$ .

According to Equation 1.62 the formation energy of a defect at a non-neutral charge state  $q$  depends on the position of the valence-band top  $E_v$ . In a supercell calculation, due to finite size effects, the position of  $E_v$  differs in the defective supercell from its position in the perfect crystal. Therefore it is necessary to estimate the lineup of the energy levels. As proposed by de Walle and Martin (1987), this offset is the difference in the average potentials taken over a Bulk  $\bar{V}_B$  and defective supercells  $\bar{V}_D$  respectively. Assuming the valence-band top (from bulk) to coincide with the highest occupied state at  $\mathbf{k} = \Gamma$ , i.e.,  $\epsilon_{\lambda\Gamma}$ , then

$$E_v = \epsilon_{\lambda\Gamma} + \bar{V}_D - \bar{V}_B. \quad (1.63)$$

This is an *ab-initio* method, in the sense that it is a parameter-free approach. As for the band-gap height, LDA calculations should underestimate the occupancy levels position from the valence band. There are mainly two ways as to overcome this problem, (i) keeping it *ab-initio* but improving the exchange-correlation functional, or (ii) adopting parameter-dependent methods. This is the case of a semi-empirical scheme proposed by Resende *et al.* (1999). The donor or acceptor levels of a defect  $E(q/q+1)$  are calculated from the difference in total energies of charged and neutral defects,  $\Delta E_D(q/q+1) = E_D(q) - E_D(q+1)$ , and comparing the analogous quantity found for a *standard* defect (with well known donor or acceptor levels), that is,

$$E(q/q+1) - E_v = \Delta E_D(q/q+1) - \Delta E_S(q/q+1). \quad (1.64)$$

This method assumes that the defect and standard should have similar levels and treated in the same sized cell and basis (Resende *et al.*, 1999). It has proved very useful in anticipating the single and second acceptor levels of Sn-V defects in Si (Larsen *et al.*, 2000), and is affected by an error of  $\sim 0.2$  eV.

It should be emphasised that these are thermodynamic levels, i.e., they are differences between the ground states of a defect in two charge states. They influence the position of the Fermi-level through a charge balance equation or neutrality condition. These levels are commonly measured by capacitance methods, in particular by deep-level transient spectroscopy (DLTS). In principle, they can also be compared with optical absorption measurements. However, we must bear in mind that no atomic relaxation occurs during photo-ionisation. This should be less problematic for shallow defects, if the extent of the donor or acceptor wavefunction is such that the relaxation energy is negligible when compared with the band-gap.

### 1.8.3 Mulliken bond population

It is important to understand the properties of gap-states. For example, the carbon interstitial defect in Si has a donor state localised on a  $p$ -orbital centred on the carbon

atom. This was clearly demonstrated on resonance experiments (Trombetta and Watkins, 1987). One way to determine the contribution from a basis function  $\phi_i$  to a gap state  $\lambda$  is by calculating the Mulliken bond population  $p_\lambda(i)$  (Pople and Beverage, 1970), defined as

$$p_\lambda(i) = \frac{1}{N_L} \sum_{j,\mathbf{k}} c_{\mathbf{k}\lambda,i} S_{ij}^{\mathbf{k}} c_{\mathbf{k}\lambda,j}^*, \quad (1.65)$$

where  $S_{ij}^{\mathbf{k}}$  are the overlap matrix elements,

$$S_{ij}^{\mathbf{k}} = \int B_{\mathbf{k}i}^* e^{-i\mathbf{k}\cdot\mathbf{r}} B_{\mathbf{k}j} d\mathbf{r}. \quad (1.66)$$

Here the sum runs over the special  $\mathbf{k}$ -points, and  $\sum_i p_\lambda(i) = 1$ . If a state  $\lambda$  has a strong contribution from the orbital  $\phi_i$  centred on a particular atom, the coefficients  $c_{\mathbf{k}\lambda,i}$ , and therefore  $p_\lambda(i)$  will be large. We can then estimate the hybridisation of the state by comparing all  $p_\lambda(i)$  values for  $s$ ,  $p$  and  $d$ -type orbitals.

As we shall see in Chapter 2, magnetic resonance experiments can be interpreted as a linear combination of atomic orbitals. This allows paramagnetic wavefunctions to be characterised in terms of amplitude and angular momentum. The Mulliken bond population is therefore very useful when confronted with these measurements.

#### 1.8.4 Localised vibrational modes

Localised vibrational modes and their frequencies are quantities which can be accurately predicted by *ab-initio* methods. These can be directly compared with infra-red absorption or photoluminescence data. Here we use the adiabatic (or Born-Oppenheimer) approximation, in the sense that the nuclei are regarded as point-like masses surrounded by electrons that adiabatically follow their vibrational movement. We also assume the harmonic approximation, according to which, the total energy  $E$  of a system composed of  $N$  atoms is expanded to second order atomic displacements Born and Huang (1954); Maradudin *et al.* (1963); Stoneham (1975); Srivastava (1990),

$$E = E_0 + \frac{1}{2} \sum_{i,j}^N \mathbf{u}_i \cdot \mathbf{K}(i,j) \cdot \mathbf{u}_j, \quad (1.67)$$

where  $E_0$  is the static total energy,  $\mathbf{u}_i$  is the displacement of atom  $i$ , and  $\mathbf{K}(i,j)$  is a second-rank tensor whose elements  $K_{ab}(i,j)$  are normally referred as force-constants, given by the second derivatives of the total energy with respect to atomic motion at the equilibrium,

$$K_{ab}(i,j) = \frac{\partial^2 E}{\partial u_{ia} \partial u_{jb}}, \quad (1.68)$$

with  $a$  and  $b$  representing any of the three Cartesian coordinates.

The equation of motion of an atom  $i$  is given by

$$M_i \frac{\partial^2 \mathbf{u}_i}{\partial t^2} = -\nabla_i E = -\sum_j^N \mathbf{K}(i,j) \cdot \mathbf{u}_j. \quad (1.69)$$

Assuming a oscillatory solution  $\mathbf{u}_i(t)$ , one arrives to an eigenvalue problem,

$$\mathbf{D} \cdot \mathbf{U} = \omega^2 \mathbf{U}, \quad (1.70)$$

with the  $3N \times 3N$  matrix called *dynamical matrix* (Born and Huang, 1954),

$$D_{ab}(i,j) = \frac{1}{\sqrt{M_i M_j}} K_{ab}(i,j). \quad (1.71)$$

Its  $3N$  eigenvalues  $\omega^2$  are the square frequencies associated with  $3N$  normal modes  $\mathbf{U}$ . Note that each normal mode is a  $3N$  dimensional vector representing the motion of all  $N$  atoms.

For periodic systems, one need to include a lattice labelling index  $l$ . Hence the  $i$ -th atom in the  $l$ -th unit cell has a displacement represented by  $\mathbf{u}_{li}$ , and a force constant is now represented by  $\mathbf{K}(il, j'l')$ . A solution to Equation 1.69 assumes now a wave-like form, and the dynamical matrix elements for a unit cell are then given by,

$$D_{ab}^{\mathbf{k}}(i, j) = \frac{1}{\sqrt{M_i M_j}} \sum_l K_{ab}(i0, jl) e^{i\mathbf{k} \cdot (\mathbf{r}_{jl} - \mathbf{r}_{i0})}, \quad (1.72)$$

where a phase factor depending on the equilibrium positions of atoms  $\mathbf{r}_{il}$  is introduced. Eigenvectors from  $D_{ab}^{\mathbf{k}}(i, j)$  are now complex and have the  $\mathbf{k}$ -vector as an additional *quantum number* for a complete labelling.

In practice, to calculate local vibrational modes, equation 1.71 is used, with the second derivatives  $K_{ab}(i, j)$  obtained from the *ab-initio* code. This involves moving all atom-pairs along Cartesian directions, and calculating the variation of the total energy.

For localised modes, only a few atoms are necessary to include in  $\mathbf{D}$ : specifically the defect atoms and their neighbours. This is because in these modes only the nearest atoms have considerable amplitude on  $\mathbf{U}$ . However, modes which lie close to the crystal vibrational band edges are better described if additional neighbours are included. This is easily accomplished if the force constants are derived from an empirical potential such as the one proposed by Musgrave and Pople (1962). Here the potential for atom  $i$  is

$$\begin{aligned} V_i = & \frac{1}{4} \sum_j k_r^{(i)} (\Delta r_{ij})^2 + \frac{r_0^2}{2} \sum_{i>k} k_\theta^{(i)} (\Delta \theta_{jik})^2 + r_0 \sum_{k>j} k_{r\theta}^{(i)} (\Delta r_{ij} + \Delta r_{ik}) \Delta \theta_{jik} + \\ & + \sum_{k>j} k_{rr}^{(i)} \Delta r_{ij} \Delta r_{ik} + r_0^2 \sum_{l>k>j} k_{\theta\theta}^{(i)} \Delta \theta_{jik} \Delta_{kil}. \end{aligned} \quad (1.73)$$

where  $\Delta r_{ij}$  and  $\Delta \theta_{jik}$  are the changes in the  $i - j$  bond length and the angle between  $i - j$  and  $i - k$  bonds. The sums run over the nearest neighbours of atom  $i$ , and the coefficients  $k^{(i)}$  are fitted in order to reproduce well known experimental quantities, like elastic constants, Raman frequency, etc.

### 1.8.5 Stress-energy tensor

An important characteristic of a defect with lower symmetry than the host crystal, is the stress-energy tensor or piezospectroscopic tensor  $\mathbf{B}$  (Watkins, 1996). In the absence of

any imposed stress, isolated defects are equally distributed over all equivalent orientations related by the symmetry of the crystal. However, applying a compressive stress across a particular direction results in an increase in energy of those defects exerting a compressive stress along this direction, and a decrease in energy of those which impose a tensile stress. Let us suppose that we have a volume  $V_0$  of cubic crystal under strain, containing  $N$  defects,  $N_i$  of which are oriented along direction  $i$ . In the elastic regime, the total energy is

$$E = E_0 + NE_f + \frac{V_0}{2} \boldsymbol{\epsilon} \cdot \mathbf{C} \cdot \boldsymbol{\epsilon} + \sum_i N_i \mathbf{B}^{(i)} \cdot \boldsymbol{\epsilon}, \quad (1.74)$$

subject to the condition  $N = \sum_i N_i$ . The first term is the total energy of the perfect crystal in the absence of external strain  $\boldsymbol{\epsilon}$ . The second term is the formation energy of all defects. The third term is the strain energy stored in the crystal with elastic coefficients  $C_{klmn}$ , and finally, the elements of the traceless second rank tensor  $\mathbf{B}^{(i)}$  are given by

$$B_{lm}^{(i)} = \frac{\partial E_f^{(i)}}{\partial \epsilon_{lm}}, \quad (1.75)$$

represent the variation of the formation energy  $E_f^{(i)}$  of a defect oriented along  $i$ , with respect to strain. Provided that  $\sum_i \mathbf{B}^{(i)}$  is diagonal, if all equivalent orientations are equally distributed ( $N_i = N_j$  for all  $i$  and  $j$ ), and

$$\sum_i N_i \mathbf{B}^{(i)} \cdot \boldsymbol{\epsilon} = \frac{N}{3} \text{Tr} \mathbf{B} (\epsilon_{11} + \epsilon_{22} + \epsilon_{33}). \quad (1.76)$$

At the equilibrium,  $\partial E / \partial \epsilon_{ij} = 0$ , leading us to a traceless tensor  $\mathbf{B}$ .

Assuming no interaction between defects, each one has its own partition function. Given  $r$  possible orientations, the probability  $p_i$  of finding a defect aligned along  $i$  is

$$p_i = e^{-\beta \mathbf{B}^{(i)} \cdot \boldsymbol{\epsilon}} / \sum_j^r e^{-\beta \mathbf{B}^{(j)} \cdot \boldsymbol{\epsilon}}, \quad (1.77)$$

with  $\beta = 1/k_B T$ , and hence for two different alignments we have,

$$\frac{p_i}{p_j} = e^{-\beta(\mathbf{B}^{(i)} - \mathbf{B}^{(j)}) \cdot \boldsymbol{\epsilon}} \quad \text{subject to} \quad \sum_i^r p_i = 1. \quad (1.78)$$

Both expressions in 1.77 and 1.78 are used in experiments to obtain the  $B_{lm}$  components. Uniaxial stress at a predefined temperature  $T$  is applied to the sample, where after waiting long enough, defects will reach an equilibrium alignment distribution given in Equation 1.77. The probability values  $p_i$ , are then measured, as they are proportional to the intensity of some spectroscopic signal. Note that not all  $B_{lm}$  components are independent. The stress-tensor is:

1. Traceless, i.e.,  $B_{11} + B_{22} + B_{33} = 0$ . This condition follow from the fact that in the absence of stress, all defects are randomly aligned, and the volume derivative of the energy must vanish at the equilibrium;
2. Symmetric ( $B_{lm} = B_{ml}$ );
3. Symmetric with respect to any symmetry operation  $\mathbf{R}$  of the point-group of the defect,  $\mathbf{R}^{-1} \cdot \mathbf{B} \cdot \mathbf{R} = \mathbf{B}$ .

To calculate the stress-tensor for a defect, we deform the defective supercell with a set of strain tensors compatible with the symmetry of the defect, and solve Equation 1.75. This procedure can be preceded by a volume relaxation of the supercell, imposing the traceless condition. If the volume is not relaxed, an extra volumetric component is included in a non-traceless stress-energy tensor  $\mathbf{B}'$ . Using Equations 1.76 and 1.74, and assuming only volumetric distortions in a cubic material ( $\epsilon_{ii} = \epsilon$  and  $B = (C_{1111} + 2C_{1122})/3$ ), we now have

$$E = E_0 + NE_f + \frac{9}{2} V_0 B \epsilon^2 + N \text{Tr} \mathbf{B}' \epsilon, \quad (1.79)$$

where  $B$  is the crystal bulk modulus. To find the volume change per defect  $\Delta V/N = (V - V_0)/N$  we simply solve  $\partial E/\partial \epsilon = 0$ , to find that



$$\frac{\Delta V}{N} = -\frac{1}{3B} \text{Tr } \mathbf{B}'. \quad (1.80)$$

Comparing Equations 1.74 and 1.79, we conclude that

$$\mathbf{B} = \mathbf{B}' - \frac{1}{3} \text{Tr } \mathbf{B}'. \quad (1.81)$$

Using equations 1.80 and 1.81, we can calculate the anisotropic stress-energy tensor elements  $B_{lm}$ , as well as predict the volume relaxation of the crystal for a specific defect density.

### 1.8.6 Migration and reorientation barriers

To calculate the activation energy for the diffusion (or reorientation) of a defect, the saddle point lying in the pathway between translationally equivalent (or symmetrically equivalent) sites must be found (Flynn, 1972). This can be achieved by relaxing the cell subject to some constraint preventing the defect from returning to its equilibrium site. In some cases this can be done by constraining the symmetry of the defect and in others by imposing algebraic constraints on bond lengths in a way described previously (Jones *et al.*, 1991). These type of constraints are ideal for situations where in the saddle-point some bond between atoms  $i$  and  $j$  is about to be broken, and the  $i - k$  bond is about to be created. Appropriate constraints are then:

$$c = |\mathbf{R}_i - \mathbf{R}_j|^2 - |\mathbf{R}_i - \mathbf{R}_k|^2, \quad (1.82)$$

with  $c = 0$  when the  $i - j$  and  $i - k$  distances are equal. All the atoms in the cell are relaxed subject to  $c$  taking specific values. Using this procedure, the configuration energy surface can be found as a function of  $c$  and the barrier estimated by interpolation (Jones *et al.*, 1991). Previously this method was used to find the saddle-point configuration of interstitial oxygen in Si (Newman and Jones, 1994).

## 1.9 Convergence criteria

There are several convergence criteria that must be addressed: the cut-off in the Fourier expansion of the charge density, the number of shells of vectors  $\mathbf{L}_n$  required to evaluate the Madelung energy (see Ewald method in Subsection 1.7.5), the mesh of special  $\mathbf{k}$ -points used to sample the band structure energy, the exponents used in the Gaussian basis functions and the size of the supercell. These criteria are not independent of each other and several iterations are needed to generate satisfactory values. Having selected a basis and supercell, the first three are easily dealt with: The number of shells of lattice vectors, the terms in the Fourier expansion and the number of  $\mathbf{k}$ -points generated by a MP-scheme are increased until the energy changes by less than 0.001 a.u. per atom.

The Fourier transform of the charge density includes reciprocal lattice vectors  $\mathbf{g}$  corresponding to kinetic energies up to 80 a.u. for Si and Ge, and 300 a.u. when oxygen is included in the cell. The large cut-offs arise from the use of the BHS pseudopotentials and the lack of an occupied core  $p$ -orbital for oxygen.

The convergence criteria involving the number of Gaussian exponents and the size of the supercell are more problematic. The wavefunction basis consists of  $N$  Gaussian  $s$ - and  $p$ -orbitals, each specified by an exponent and located at the nuclei, and  $M$  similar orbitals located at each bond centre to simulate the effect of higher order angular momentum functions like  $d$ -orbitals. The Gaussian exponents for Si, O and Ge were found by minimising the energy of a cell containing bulk material or a disiloxane molecule  $\text{O}-(\text{Si}-\text{H}_3)_2$ . The exponents were selected in the range between 0.1 and 3.6 a.u. by using a Metropolis-like algorithm. All the exponents used are given in Table 1.1.

The table also shows that the calculated lattice parameters and bulk moduli for Si and Ge lie within 1% of the experimental values and that these structural parameters have converged for the smallest (4, 1) basis set. As a test, the structure of  $\alpha$ -quartz was also evaluated and the lattice parameters found to be within 0.6% of the observed values with the (4, 1) Si and (6, 1) O basis.

The energy, however, is much more sensitive to the basis and Table 1.2 shows its variation

Table 1.1: Basis exponents (a.u.) for  $s$ - and  $p$ -Gaussian orbitals for Si, Ge and O. AC refers to orbitals sited at atoms while BC refers to those sited at bond centres.  $(N, M)$  refer to numbers of orbitals placed at nuclei and at bond centres respectively. Lattice parameters  $a_0$  (Å), the bulk moduli  $B$  (GPa), found from the basis sets are also given. Experimental values for  $a_0$  and  $B$  from James and Lord (1992) and Singh (1993) respectively.

Species	Silicon		Germanium		Oxygen	
$(N, M)$	(4, 1)	(4, 2)	(4, 1)	(4, 2)	(6, 1)	(6, 2)
AC	0.1454	0.1272	0.1499	0.1509	0.2043	0.2815
	0.5002	0.3938	0.3747	0.4008	0.4339	0.5470
	1.2102	1.1592	0.9369	0.9018	0.9409	1.1665
	3.5712	3.1164	2.3422	2.4433	2.2011	2.5534
					4.7881	5.3166
				10.3587	11.4959	
BC	0.1946	0.1474	0.1632	0.1435	0.4624	0.2081
		0.3838		0.3824		0.4238
$a_0$ (calc.)	5.390	5.394	5.579	5.568		
$B$ (calc.)	99.5	94.3	76.3	74.2		
$a_0$ (obs.)	5.431		5.658			
$B$ (obs.)	97.9		77.2			

Table 1.2: Total energies (a.u.) for bulk Si and  $\alpha$ -quartz. The formation energy (eV), for an interstitial oxygen centre was evaluated using equation 1.62, and is given in the right hand column.

Basis		$E_{2\text{Si}}$	$E_{3\text{SiO}_2}$	$E_f(\text{O}_i)$
Si	O			
(3, 0)	(6, 0)	-7.8623	-108.1744	1.989
(3, 1)	(6, 1)	-7.9187	-108.4906	1.973
(4, 1)	(6, 1)	-7.9271	-108.5423	1.809
(4, 2)	(6, 2)	-7.9309	-108.5485	1.817
(4, 3)	(6, 3)	-7.9317	-108.5502	1.820

with different  $(N, M)$  values. Here the energies for primitive cells of Si and  $\alpha$ -quartz were evaluated using a MP-8<sup>3</sup> sampling mesh and fixed cell parameters equal to the converged values. It is clear that for the (4, 1) Si basis, the absolute energy per atom of bulk Si is in error by as much as 0.05 eV. Similarly, the Si (4, 1) and O (6, 1) basis produces an error in the total energy of a unit cell of quartz of 0.008 a.u. or 0.2 eV.

The absolute energy is, however, not of major concern. Of greater interest are the formation energies of defects and their relative energies (Subsection 1.8.2). The chemical potentials for Si and Ge are simply the energies per atom in the bulk phase. When dealing with oxygen defects in Si, we take  $\mu_{\text{O}}$  to be given by the energy of an oxygen atom in  $\alpha$ -quartz, namely  $\mu_{\text{O}} = (E_{3\text{SiO}_2} - 3\mu_{\text{Si}})/6$ . A similar equation involving  $\text{GeO}_2$  gives the chemical potential for oxygen in Ge. The formation energy then gives the equilibrium density of oxygen atoms in Si (Ge) when in equilibrium with  $\text{SiO}_2$  ( $\text{GeO}_2$ ).

The chemical potentials vary substantially with the basis as discussed above but the formation energies  $E_f$  of defects calculated using a consistent basis are much less sensitive. This is illustrated in Table 1.2 which shows that  $E_f$  for interstitial oxygen in Si has converged to within 10 meV, for the (4, 1) Si and (6, 1) O basis. These calculations used 64 Si cells and MP-2<sup>3</sup> sampling.

Table 1.3: Energy per silicon atom and formation energy of  $O_i$  in Si, eV, evaluated in several supercells and sets of special  $\mathbf{k}$ -points.  $scN$ ,  $fccN$ , and  $bccN$  refers to simple cubic, faced centred cubic, and body centred cubic lattices containing  $N$  Si atoms;  $n$  denotes the MP- $n^3$  sampling grid used.

Supercell	$n$	$E_{\text{Si}}$	$E_f(O_i)$	
			Calc. <sup>a</sup>	Calc. <sup>b</sup>
<i>sc64</i>	1	-107.7433	1.06	
<i>fcc128</i>	1	-107.7577	1.38	1.1
<i>sc216</i>	1	-107.8393	1.66	
<i>bcc32</i>	2	-107.8452	1.83	1.8
<i>sc64</i>	2	-107.8534	1.81	
<i>sc8</i>	20	-107.8549		

<sup>a</sup>This work.

<sup>b</sup>From Pesola *et al.* (1999a)

We now discuss the effect of different sized supercells and sampling schemes. For this the basis was fixed to be Si (4, 1) and O (6,1) and the unit cells volume was relaxed. Table 1.3 shows that using a single  $\mathbf{k}$ -point at  $\Gamma$  in a 64 Si atom cell gives an error in the energy per atom of about 0.1 eV but this decreases to about 0.0015 eV for an MP-2<sup>3</sup> scheme Monkhorst and Pack (1976). Thus in 64 atom cells, we invariably used this scheme. The MP-1<sup>3</sup> sampling scheme was only used in 216 atom cells. Also shown, is the formation energy of  $O_i$ . Here it is clear that the use of MP-1<sup>3</sup> sampling gives poor energies except in the largest 216 atom cells.

To check the effect of the size of the supercell on the defect, the volume of the cell ought to be relaxed. Defects can exert strong compressive or tensile stresses, and the total energy per cell is reduced by expanding or contracting the lattice. Whereas each defect gives a finite volume change – irrespective of the volume of the supercell – the fractional volume change should vanish in the limit of large cells. The magnitude of this change is then a

measure of the sensitivity to cell size.

## 1.10 Summary

The DFT formalism has been presented as an accurate method for solving the ground state of a many-electron problem. In its formalism, the charge density is used as a variational variable, without introduction of approximations. Unfortunately, an exact exchange-correlation functional is still unknown. The LDA form of this functional was used throughout this thesis. In this sense, DFT might be seen as a pragmatic approach, allowing us to explore larger problems than those solvable with the all-electron Schrödinger equation.

The pseudopotential method, also plays a key role. Without them, the problem of a simple Ge atom would be as costly as that of a small cluster made of  $\sim 10$  *pseudo* Ge atoms. This allows us to model defects embedded in supercells with up to  $\sim 200$  group-IV atoms (plus the defect).

Finally, bearing in mind that we are using a ground-state theory, we must acknowledge the variety of observables that we are allowed to accurately predict. These include optical, mechanical and thermodynamic properties, which combined with the experiments, allows us to grasp many microscopic properties of defects in semiconductors.

## Chapter 2

# Experimental survey

### 2.1 Electron Paramagnetic Resonance

From a spectroscopic point of view, electron paramagnetic resonance (EPR) forms the basis for one of the most powerful techniques of defect characterisation. With it, valuable information concerning the microstructure of defects in crystals can be readily obtained. The wavefunction symmetry of a paramagnetic state, the site symmetry and identity of nearby atoms with a finite nuclear magnetic moment, and the angular-momentum character of the resonant electron are examples of properties that can be directly observed (Watkins, 1999; Bourgoin and Lannoo, 1983; Stoneham, 1975). Complementary techniques can be used to extract even more information. Stress alignment and its thermal recovery, has proven to be extremely efficient in providing new insights on defects (Watkins and Corbett, 1961*a*; Watkins, 1975).

#### 2.1.1 Zeeman splitting

An unpaired electron within a spherically symmetric potential, possesses both orbital and intrinsic angular momenta  $\mathbf{L}$  and  $\mathbf{S}$  with amplitudes  $L$  and  $S$  quantised by integers  $l$  and  $s$  respectively, *i.e.*,

$$L = \sqrt{l(l+1)}\hbar \quad l = 0, 1, \dots \quad (2.1)$$

$$S = \sqrt{s(s+1)}\hbar \quad s = \frac{1}{2}, 1, \dots \quad (2.2)$$

The respective magnetic moments  $\boldsymbol{\mu}_L$  and  $\boldsymbol{\mu}_S$  contribute to a total magnetic moment  $\boldsymbol{\mu}$ ,

$$\boldsymbol{\mu} = \boldsymbol{\mu}_L + \boldsymbol{\mu}_S = -\mu_B g_L \mathbf{L} - \mu_B g_S \mathbf{S}, \quad (2.3)$$

where  $\mu_B$  is a proportionality factor of  $e\hbar/2m_e c$ , known as the Bohr magneton,  $g_L = 1$  and  $g_S = 2.0023$  are the so called *g-values* associated with  $\mathbf{L}$  and  $\mathbf{S}$ .

In a solid the unpaired electron also experiences a crystal field composed of valleys and saddles, and as shown by van Vleck (1932), the angular momentum can be quenched. Nevertheless, the unpaired spin distribution induces a small magnetic momentum via spin-orbit coupling. This is taken into account by expressing the total magnetic moment with an effective  $\mathbf{g}$ -tensor instead of the previous  $g$ -value. Therefore

$$\boldsymbol{\mu} = -\mu_B \mathbf{g} \cdot \mathbf{S}, \quad (2.4)$$

where  $\mathbf{g}$  is now a second rank tensor that mirrors the anisotropy of the spin density distribution and its orientation relative to some axial system. This new information arises from the induced magnetic dipole on atoms surrounding the unpaired electron. Bearing this in mind, one can divide  $\mathbf{g}$  into an isotropic term equal to  $g_e = 2.0023$  (corresponding to the  $g$  value of a free electron), and a deviation  $\Delta\mathbf{g}$  carrying the signature of the environment,

$$\mathbf{g} = g_e \cdot \mathbf{l} + \Delta\mathbf{g}. \quad (2.5)$$

Here  $\mathbf{l}$  is the unit matrix.  $\Delta\mathbf{g}$  can be evaluated by perturbation theory, where a spin-orbit coupling term  $\lambda \mathbf{L} \cdot \mathbf{S}$  is expanded to second order. Thus, if  $|n\rangle$  and  $|0\rangle$  represent excited



and ground states with energies  $E_n$  and  $E_0$  respectively, as Bourgoin and Lannoo (1983) shown,

$$\Delta \mathbf{g} = -2\lambda \sum_n \frac{\langle 0 | L | n \rangle \langle n | L | 0 \rangle}{E_n - E_0}. \quad (2.6)$$

A steady magnetic field  $\mathbf{H}$  along an arbitrary direction couples with  $\boldsymbol{\mu}$ , resulting in a Hamiltonian  $\mathcal{H}_{Ze}$ , where

$$\mathcal{H}_{Ze} = \mu_B \mathbf{H} \cdot \mathbf{g} \cdot \mathbf{S}. \quad (2.7)$$

The  $(2S + 1)$  degenerate electronic states are now split. This phenomenon is called the Zeeman splitting. For a particular direction of the magnetic field given by a unit vector  $\mathbf{h}$ , the electron spin can be considered as quantised along an effective magnetic field  $H \mathbf{h} \cdot \mathbf{g} = H |\mathbf{h} \cdot \mathbf{g}| \mathbf{h}_s$  with direction  $\mathbf{h}_s$ . This allows us to approximate the energy eigenvalues from the Hamiltonian in 2.7, using the azimuthal spin quantum number  $m_s$  as follows,

$$E = \mu_B H m_s \mathbf{h} \cdot \mathbf{g} \cdot \mathbf{h}_s = \mu_B H m_s \frac{(\mathbf{h} \cdot \mathbf{g}) \cdot (\mathbf{g} \cdot \mathbf{h})}{|\mathbf{g} \cdot \mathbf{h}|}, \quad (2.8)$$

where the allowed transitions, for which  $\Delta m_s = \pm 1$ , occur between equally spaced levels separated by

$$\Delta E = \mu_B H \sqrt{\mathbf{h} \cdot \mathbf{g}^2 \cdot \mathbf{h}} = \mu_B H g. \quad (2.9)$$

Note that here the direction of  $\mathbf{H}$  is fixed, and therefore the  $\mathbf{g}$ -tensor is contracted towards a scalar. The Zeeman splitting between  $m_s = \pm 1/2$  states is shown as  $t_0$  in Figure 2.1. For magnetic fields of the order of  $\sim 1$  T, the energy separation  $\mu_B H g$  typically corresponds to photon frequencies of 1 - 30 GHz (microwave region). Monitoring electronic transitions between Zeeman states is the basis of EPR. In practice it is difficult to have a source of microwaves tunable in a wide enough spectral region. Instead, this one is fixed with some frequency  $\omega$ , and the magnetic field  $\mathbf{H}$  is allowed to vary until resonance occurs.

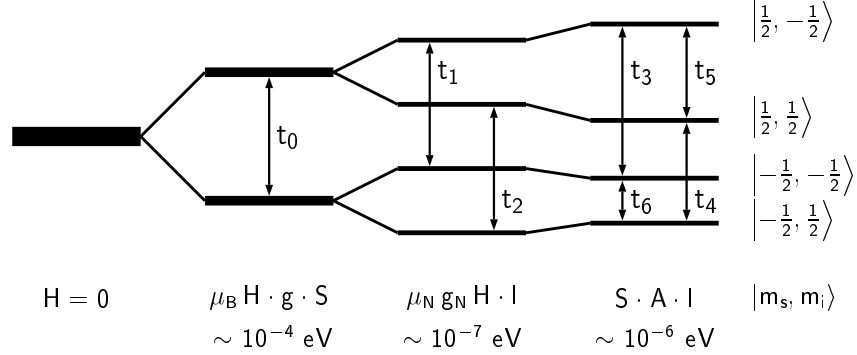


Figure 2.1: Energy levels of a system with  $S = 1/2$  and  $I = 1/2$  under influence of a magnetic field. EPR transition are allowed when  $\Delta m_s = \pm 1$  and  $\Delta m_i = 0$ , whereas for ENDOR the selection rules are  $\Delta m_s = 0$  and  $\Delta m_i = \pm 1$ .

### 2.1.2 Angle dependent patterns

As defined in Subsection 2.1.1, the coupling between the unpaired spin associated with a defect state and an external magnetic field is mediated through a tensor  $\mathbf{g}$ . The Hamiltonian was then found to have solutions which are proportional to  $\sqrt{\mathbf{h} \cdot \mathbf{g}^2 \cdot \mathbf{h}}$ . Expressing the unit vector  $\mathbf{h}$  in terms of the angles  $\theta_i$  that it makes with the Cartesian axes ( $i = 1, 2, 3$ ), the quantity inside the square root can be expanded to

$$g^2 = \mathbf{h} \cdot \mathbf{g}^2 \cdot \mathbf{h} = \sum_i [\mathbf{g}^2]_{ii} \cos^2 \theta_i + 2 \sum_k \varepsilon_{ijk} [\mathbf{g}^2]_{ij} \cos \theta_i \cos \theta_j, \quad (2.10)$$

where  $[\mathbf{g}^2]_{ij}$  represent the tensorial element indexed by the  $i, j$  pair, and  $\varepsilon_{ijk} = 1$  if  $i \neq j \neq k \neq i$ , and zero otherwise. In silicon crystals, a defect transforming within a point group  $G$  of order  $g_G$ , can take  $24/g_G$  different orientations (Kaplianskii, 1964). Hence, each of the  $24/g_G$  different  $\mathbf{g}$ -tensor orientations correspond to a  $g^2$ -value in Equation 2.10, and therefore to an individual EPR resonance. However, since in practice the magnetic field is kept in the  $(0\bar{1}1)$  plane, one is restricted to 12 orientations (Sieverts, 1978). In this plane  $\sin \theta_1 = \sqrt{2} \cos \theta_2 = \sqrt{2} \cos \theta_3$ , allowing us to drop the indexes, and rewrite Equation 2.10 for any orientation of  $\mathbf{H}$  within the plane,

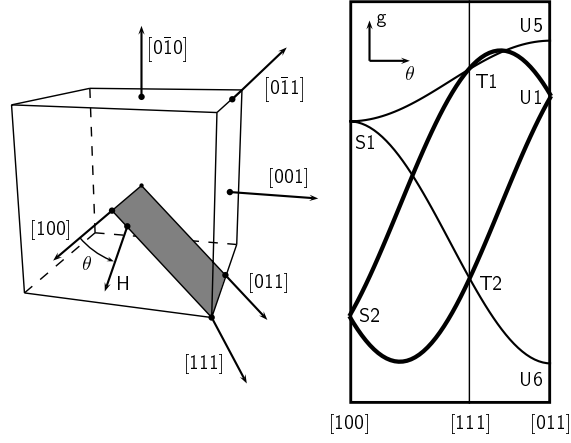


Figure 2.2: Angular variation of the magnetic field  $\mathbf{H}$  relative to the cubic crystallographic axes in an EPR experiment (left). Angular dependence of a spin-half rhombic-I symmetry ( $C_{2v}$ ) EPR signal (right). Thick and thin lines are doubly and non degenerate defect orientations relative to  $\mathbf{H}$ .

$$g^2 = g_{11}^2 \cos^2 \theta + \frac{1}{2} (g_{22}^2 + g_{33}^2) \sin^2 \theta + \frac{1}{2} (g_{12}^2 + g_{13}^2) \sin \theta \cos \theta + g_{23}^2 \sin^2 \theta. \quad (2.11)$$

If the defect possesses any structural symmetry, say that all atomic coordinates can be transformed within the symmetry operator  $\mathbf{R}$ , then additional constraints will be imposed on the  $\mathbf{g}$ -tensor, i.e.,  $\mathbf{R}^{-1} \cdot \mathbf{g} \cdot \mathbf{R} = \mathbf{g}$ . For example, if a paramagnetic defect possesses  $C_{2v}$  symmetry, the number of distinct orientations is reduced to 6, and Equation 2.11 is further simplified to

$$g^2 = g_{11}^2 \cos^2 \theta + (g_{33}^2 + g_{23}^2) \sin^2 \theta. \quad (2.12)$$

The  $g^2$  values corresponding to each orientation of the defect, are then monitored by varying the direction of the magnetic field. A typical EPR pattern for a  $C_{2v}$  defect is shown in the right-hand side of Figure 2.2,

The  $g$ -values for the  $[100]$ ,  $[111]$  and  $[011]$  high-symmetry directions, are commonly denoted as S-, T-, and U-values respectively. One can readily observe that not all *branches* have the

same thickness. Thicker lines correspond to more intense resonances due to orientational degeneracy (Kaplanski, 1964). Hence, when  $\mathbf{H}$  is along [100], only two orientations of defects are distinguishable: those with the  $C_2$  axis parallel and perpendicular to  $\mathbf{H}$ . However, there are twice as many defects axially perpendicular to  $\mathbf{H}$  as those which are parallel to it. Therefore, for this particular orientation of  $\mathbf{H}$ , the EPR signal contains two features, namely at S1 and S2, with an intensity ratio of 2:4. Here we preserve the total number of possible orientations ( $6 = 4 + 2$ ).

We can now appreciate how powerful the measurement of the  $g$ -tensor associated with a paramagnetic defect can be. It not only provides us with information about the symmetry of the centre, but also gives us the anisotropy character of the unpaired electron. The eigenvalues  $g_i$  and eigenvectors  $\mathbf{g}_i$  of the  $g$ -tensor contain useful information. Very similar  $g_i$  elements indicate low anisotropy and vice versa. The principal directions inform us about the orientation of the paramagnetic spin density relative to the crystallographic axes. This kind of information is certainly priceless and unattainable by any other spectroscopic technique.

### 2.1.3 Hyperfine interaction

Until now, we considered the coupling between an external magnetic field and an unpaired spin. However, besides the external field, the electron is affected by other sources of magnetism within solids. In silicon, approximately 4.7% of the atoms belong to the  $^{29}\text{Si}$  isotopic species, possessing an intrinsic nuclear spin  $I = 1/2$ . We can imagine these as magnetic dipoles inducing its own magnetic fields, much like the applied field (being however  $\sim 2$  orders of magnitude weaker). These give rise to the hyperfine interaction. In this Subsection, a description will be given about how information concerning a particular defect is extracted from these weak interactions.

Consider an isolated atom whose nucleus possesses an intrinsic angular momentum  $\mathbf{I}$  where  $I = \sqrt{i(i+1)} \hbar$  and  $i = 0, \frac{1}{2}, 1, \dots$ . As for the electron, this nucleus has a magnetic moment

$$\mu_I = -g_N \mu_N \mathbf{I}, \quad (2.13)$$

where  $g_N$  is the nuclear  $g$ -value (for  $^{29}\text{Si}$ ,  $g_N = 1.1095$ ), and  $\mu_N$  the nuclear magneton. Analogously to  $\mu_B$ , the nuclear magneton is  $e\hbar/2Mc$ , but  $M$  is now the nuclear mass. Atoms with non-zero  $\mathbf{I}$  can interact with an unpaired electron, or with an external magnetic field. The last interaction is of Zeeman type, and in analogy with Equation 2.7, one can write a term to be added to the Hamiltonian as

$$\mathcal{H}_{Zi} = \mu_N \mathbf{H} \cdot \mathbf{g}_N \cdot \mathbf{I} = \mu_N g_N \mathbf{H} \cdot \mathbf{I}. \quad (2.14)$$

Note that in this situation we assume an interaction between  $\mathbf{H}$  and a point like nuclear dipole moment. Therefore  $\mathbf{g}_N$  is contracted to a scalar and the coupling is isotropic. A Zeeman-nuclear interaction for a system with  $I = 1/2$  is shown in Figure 2.1 involving a second splitting. Two associated EPR transitions are also indicated by  $t_1$  and  $t_2$ . These correspond to  $\Delta m_s = \pm 1$  and  $\Delta m_i = 0$ , where  $m_s$  and  $m_i$  are the azimuthal quantisations of the electronic and nuclear angular momenta.

Now if an atom with non-zero nuclear magnetic moment is in the neighbourhood of a paramagnetic defect, another type of hyperfine interaction can be observed. This can be thought as arising from the interaction between a local magnetic field  $\mathbf{H}_{\text{loc}} \propto \mathbf{A} \cdot \mathbf{I}$  induced by a magnetic nucleus, and the electronic spin, i.e.,

$$\mathcal{H}_{SI} = \mathbf{S} \cdot \mathbf{A} \cdot \mathbf{I}, \quad (2.15)$$

where  $\mathbf{A}$  is referred as hyperfine tensor. On the extreme right of Figure 2.1, the effect of this coupling is shown, and now EPR transitions (labelled as  $t_3$  and  $t_4$ ) do not possess the same energy. We see that  $\Delta E(t_4) \leq \Delta E(t_0) \leq \Delta E(t_3)$ , implying that the EPR spectra will be composed of strong absorption lines due to  $t_0$  transitions, plus a certain number of low- and high-energy side bands with intensity depending on the number of equivalent

nuclei giving rise to each particular sideband. We can now write the spin-Hamiltonian normally adopted for paramagnetic defects in semiconductors,

$$\mathcal{H} = \mathcal{H}_{Ze} + \mathcal{H}_{Zi} + \mathcal{H}_{SI} = \mu_B \mathbf{H} \cdot \mathbf{g} \cdot \mathbf{S} + \sum_k \left( \mu_N^{(k)} g_N^{(k)} \mathbf{H} \cdot \mathbf{I}^{(k)} + \mathbf{S} \cdot \mathbf{A}^{(k)} \cdot \mathbf{I}^{(k)} \right), \quad (2.16)$$

where the summation (taken over all atoms for which  $I \neq 0$ ) can eventually be substituted by a term expressing the location and statistical abundance of the corresponding atomic species. The hyperfine tensor  $\mathbf{A}^{(k)}$  as we shall see next, contains detailed information concerning the shape of the wavefunction near atom  $k$ .

The electron-nuclear hyperfine contribution in 2.16 can be described as dipole-dipole interaction between two magnetic dipole moments separated by a vector  $\mathbf{r}$ . Assuming only one magnetic nucleus, the operator associated with this observable can be written as

$$\mathcal{H}_{SI} = g \mu_B g_N \mu_N \left[ \left( \frac{3(\mathbf{S} \cdot \mathbf{r})(\mathbf{I} \cdot \mathbf{r})}{r^5} - \frac{\mathbf{S} \cdot \mathbf{I}}{r^3} \right) + \frac{8}{3} \pi \mathbf{S} \cdot \mathbf{I} \delta(r) \right]. \quad (2.17)$$

Here the first term is the classical dipole-dipole interaction, but a second term, called the Fermi contact interaction, must be included. The Fermi contact interaction is non-zero for spin-densities which have an  $s$ -like component at the nucleus. We can then separate the hyperfine interaction into isotropic and anisotropic parts, say with corresponding operators  $\hat{a}$  and  $\hat{b}$ ,

$$\hat{a} = \frac{8}{3} \pi g \mu_B g_N \mu_N \mathbf{S} \cdot \mathbf{I} \delta(r) \quad (2.18)$$

$$\hat{b} = g \mu_B g_N \mu_N \left( \frac{3(\mathbf{S} \cdot \mathbf{r})(\mathbf{I} \cdot \mathbf{r})}{r^5} - \frac{\mathbf{S} \cdot \mathbf{I}}{r^3} \right), \quad (2.19)$$

where  $\mathcal{H}_{SI} = \hat{a} + \hat{b}$ . We can now write a spin-Hamiltonian describing the hyperfine effects arising from a particular electronic wavefunction  $\psi$ ,

$$\mathcal{H}_{SI} = \mathbf{S} \cdot \mathbf{A} \cdot \mathbf{I} = \langle \psi | \hat{\mathcal{H}}_{SI} | \psi \rangle = \langle \psi | \hat{a} | \psi \rangle + \langle \psi | \hat{b} | \psi \rangle = \mathbf{S} \cdot \mathbf{a} \cdot \mathbf{I} + \mathbf{S} \cdot \mathbf{b} \cdot \mathbf{I}. \quad (2.20)$$

In this way, the hyperfine tensors  $\mathbf{a}$  and  $\mathbf{b}$  mirror the local amplitude and angular variation of the unpaired wavefunction around a particular atom. Experimental determination of  $\mathbf{A}$  follows the same procedure as that for  $\mathbf{g}$ . Providing that hyperfine peaks can be resolved, the direction of the magnetic field is varied in the  $(0\bar{1}1)$  plane, and again, sinusoidal patterns are observed. However, these can be much more complicated than those arising from the electron-Zeeman splitting since several sidebands can appear in a narrow spectral region. These patterns provide us with an immense amount of information, and for practical purposes only some values at S-, T- and U- are necessary to define  $\mathbf{A}$  (Sieverts, 1978). Another important feature of the hyperfine interaction analysis is the fact that all symmetry equivalent magnetic nuclei will contribute to the same band. Here  $\mathbf{A}^{(m)} = \mathbf{R}^{-1} \cdot \mathbf{A}^{(n)} \cdot \mathbf{R}$ , where  $\mathbf{R}$  relates both  $m$  and  $n$  equivalent atoms, and consequently the EPR signals arising from both nuclei will be superimposed (Kaplianskii, 1964). We then say that each hyperfine band arises from a *shell* of symmetrically equivalent magnetic nuclei.

#### 2.1.4 LCAO analysis of the hyperfine spectra

As we concluded from Equation 2.20, the hyperfine tensor  $\mathbf{A}$  quantifies the coupling between a nuclear magnetic dipole and the electron spin density. Isotropic and anisotropic tensors  $\mathbf{a}$  and  $\mathbf{b}$  were then defined for a general shape of the electronic wavefunction. In practice, wavefunctions associated with gap-states are normally approximated as linear combination of atomic orbitals  $\phi_i$  (LCAO) centred on each atom  $i$  near the defect (Slater, 1965, p. 203). Hence,

$$\psi(\mathbf{r}) = \sum_i \eta_i \phi_i(\mathbf{r}), \quad (2.21)$$

where  $\sum_i \eta_i^2 = 1$ . The atomic orbitals  $\phi_i$  are normally chosen to be composed of hybridised  $sp$ - functions  $f_{s,i}$  and  $f_{p,i}$ ,

$$\phi_i(\mathbf{r}) = \alpha_i f_{s,i}(\mathbf{r}) + \beta_i f_{p,i}(\mathbf{r}), \quad (2.22)$$

with  $\alpha_i^2 + \beta_i^2 = 1$ . The LCAO interpretation of A was pioneered by Watkins and Corbett (1961*a*) and shown to be extremely fruitful. From the parity of  $f_{s,i}$  and  $f_{p,i}$ , Equation 2.20 can be written as

$$\langle \psi | \widehat{a}_{mn}^{(i)} | \psi \rangle = \delta_{mn} \frac{8\pi}{3} g \mu_B g_N \mu_N \eta_i^2 \alpha_i^2 f_{s,i}^2(\mathbf{0}) \quad (2.23)$$

$$\langle \psi | \widehat{b}_{mn}^{(i)} | \psi \rangle = g \mu_B g_N \mu_N \eta_i^2 \beta_i^2 \left\langle f_{p,i} \left| \frac{3r_m r_n}{r^5} - \frac{\delta_{mn}}{r^3} \right| f_{p,i} \right\rangle. \quad (2.24)$$

Accurate self-consistent Hartree-Fock values for  $f_{s,i}^2(\mathbf{0})$  and the integral in 2.24 are available in the literature for numerous atomic species. It is now evident from Equations 2.23 and 2.24, that the measurement of the isotropic and traceless tensors  $\mathbf{a}^{(i)}$  and  $\mathbf{b}^{(i)}$  respectively, lead to the knowledge of the localisation  $\eta_i^2$  and the  $s$ - and  $p$ -character of the wavefunction on atom  $i$ , i.e.,  $\alpha_i^2$  and  $\beta_i^2$  respectively. If the hyperfine tensor does not exhibit axial symmetry, its interpretation is more difficult (Sieverts, 1978). This is the case of shallow impurity states, where hyperfines are predominantly isotropic and LCAO normally breaks down. This kind of states are more accurately studied by means of effective-mass theory (see Section 2.5).

### 2.1.5 Observation of resonance

In a real experiment, transitions between two paramagnetic states (say  $t_0$  in Figure 2.1), are driven by two mechanisms – radiation and thermal excitations. The former tends to equalise the defect populations  $n_-$  and  $n_+$  for which  $m_s = -1/2$  and  $m_s = +1/2$  respectively. However, the second drives the occupancy of these states according to a Boltzmann law, which takes into account the fact that the defect is embedded in a thermal bath (Bourgoin and Lannoo, 1983). One can readily see that if the thermally activated process is not the fastest mechanism, it will be impossible to restore a steady state differential population  $n_- - n_+ \neq 0$ , and the transition probability will vanish along with the EPR signal. The rate at which the system relaxes to the thermal equilibrium is limited by the spin-lattice relaxation time, which is an intrinsic property of a particular material. Thus if  $W$  is the



$|\frac{1}{2}\rangle \rightarrow |-\frac{1}{2}\rangle$  or  $|-\frac{1}{2}\rangle \rightarrow |\frac{1}{2}\rangle$  transition probability, and  $\tau_{\text{sl}}$  the spin-lattice relaxation time of the material of interest, EPR signals would only be observable only if

$$W \tau_{\text{sl}} \ll 1. \quad (2.25)$$

A semiconductor for which  $\tau_{\text{sl}}$  is too short is germanium. Here the lines are broad and difficult to detect. Moreover, other sorts of difficulties can appear during an EPR experiment. For example, in materials where the most abundant isotopic species of its chemical components have a non-zero nuclear magnetic moment (like gallium arsenide), signals are normally hidden by a strong background of hyperfines. Fortunately this is not the case for silicon, which is the material of main interest in this thesis, where the spin-lattice time is sufficiently short, allowing sharp signals to be detected. Furthermore, the  $\sim 4.7\%$  natural magnetic  $^{29}\text{Si}$  nuclei enable the observation of important hyperfine interactions.

### 2.1.6 Example: Si-A centre

The Si-A centre (or VO) is a secondary radiation induced defect, where an oxygen atom inside a vacancy bridges two second neighbouring Si atoms, leaving two unsatisfied Si-dangling bonds which collapse to form a weak Si-Si reconstruction (Watkins and Corbett, 1961*a*; Corbett *et al.*, 1961). This defect is shown on the left hand side of Figure 2.3. The EPR data concerning this defect can be summarised as follows (Watkins and Corbett, 1961*a*) — EPR activity arises from the negatively charged defect with an electron trap 0.17 eV below the conduction band. This is shown schematically on the right hand side of the same figure, where an extra electron populates an anti-bonding orbital close to the conduction band bottom. The pattern of the  $g$  values can be fitted assuming a  $C_{2v}$  symmetry  $\mathbf{g}$ -tensor with principal values of 2.0093, 2.0025 and 2.0031 for  $g_1$ ,  $g_2$  and  $g_3$ , and principal directions along  $[110]$ ,  $[1\bar{1}0]$  and  $[001]$  respectively. Hyperfine interactions with 4.7% abundant  $^{29}\text{Si}$  isotopes (with a nuclear magnetic moment  $I = 1/2$ ), were resolved. These arise from five different shells, and from the relative intensities of the hyperfine signals, it was possible to estimate the number  $N^{(i)}$  of equivalent Si atoms belonging to

Table 2.1: LCAO analysis of the Si-A centre from the  $^{29}\text{Si}$  hyperfine signals measured by EPR (Watkins and Corbett, 1961*a*) and ENDOR (van Kemp *et al.*, 1989*a*). Shell labelling follow the original work.  $N^{(i)}$  is the number of Si atoms in each shell, and  $\alpha_i^2$ ,  $\beta_i^2$  and  $\eta_i^2$  are the  $s$  and  $p$  character and relative localisation of the wavefunction on atoms from shell  $i$  respectively.

	Shell	A	B	C	D	E	
	$N^{(i)}$	2	2	2	4 - 6	4 - 6	
EPR	$\alpha_i^2$	0.37	0.26	0.25	0.25	$\sim 1$	
	$\beta_i^2$	0.63	0.74	0.75	0.75	$\sim 0$	
	$\eta_i^2$	0.355	0.049	0.034	0.022	0.002	
	Shell	<i>Mad1</i>	<i>Mad2</i>	<i>Mad3</i>	<i>Mad4</i>	<i>G1</i>	<i>G2</i>
	$N^{(i)}$	2	2	2	2	4	4
ENDOR	$\alpha_i^2$	0.302	0.195	0.188	0.236	0.171	0.203
	$\beta_i^2$	0.698	0.805	0.812	0.764	0.829	0.797
	$\eta_i^2$	0.300	0.044	0.031	0.016	0.021	0.009

shell  $i$ . Using an LCAO analysis it was concluded that most part of the spin density is localised around a shell (labelled A) with two Si atoms (see Table 2.1). Shells with 4-6 atoms were also reported. However, we must bear in mind that a  $C_{2v}$  symmetry defect only has shells where  $N^{(i)}$  is 1, 2 or 4. Unequivocal evidence about  $N^{(i)}$  can be obtained if a resolved signal could be monitored with different orientations for  $\mathbf{H}$ , allowing the precise site-symmetry to be found. Experiments with samples containing the magnetic  $^{17}\text{O}$  isotope did not reveal any O-related hyperfine.

Although detailed information about the ground state of  $\text{VO}^{(-)}$  was provided by EPR, an even richer picture has been reported using electron-nuclear double resonance (ENDOR). This technique, much more sensitive than EPR, was pioneered by Feher (1959*a*). Here a powerful microwave source quenches the EPR signal by equally populating ground and excited states with  $\Delta m_i = 0$ , giving rise to a differential population of states with  $\Delta m_i \neq 0$ .

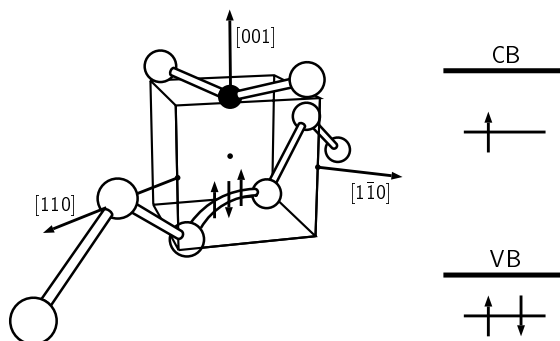


Figure 2.3: (left) Structure of the A-centre defect in Si, and (right) its level scheme in the negative charge state. Two paired electrons occupy a bonding state, and an unpaired electron occupies an anti-bonding level.

These correspond to transitions labelled as  $t_5$  and  $t_6$  in Figure 2.1. Angular patterns similar to those obtained in EPR for the hyperfine A, are then monitored during an ENDOR experiment.

Measurements of  $^{29}\text{Si}$  ENDOR reveal a total of 50 distinct shells. The six strongest hyperfines are shown in Table 2.1. Among all, 1, 20, 6 and 23 of them have  $C_2$ ,  $C_{1h}$ ,  $C_{1h}$  and  $C_1$  site-symmetry, and labelled as of  $T$ ,  $Mad$ ,  $Mbc$  and  $G$ -type respectively. Most of the spin-density was found to be localised on the  $\{1\bar{1}0\}$  plane defined by the reconstructed Si-Si unit plus the O-atom (van Kemp *et al.*, 1989a). In Table 2.1 we can see a clear agreement between the LCAO analysis from the EPR and ENDOR hyperfines. Hyperfine interactions as far as 12 Å from the defect were resolved, despite the strong localisation of the wavefunction. A plot of  $\eta^2$  vs shell-distance, shows that the wavefunction has higher amplitude on the Si atoms lying along the two semi-infinite  $[110]$ -chains, starting on both weakly bonded Si atoms respectively (see Figure 2.3). These Si-chains account for 81% of localisation.

Measurements of  $^{17}\text{O}$ -ENDOR were also reported (van Kemp *et al.*, 1989b). Regardless of the fact that the O-atom sits at a nodal plane of the anti-bonding wavefunction, it was possible to detect oxygen-related ENDOR transitions. The isotropic component of the hyperfine interaction is about  $a = 3$  MHz, corresponding to  $\eta^2 \sim 0.06\%$ , justified as arising

from spin-polarisation, or self-interaction effects. The anisotropic part of  $A$  correspond to a localisation of  $\eta^2 = 1.18\%$  on a  $p$ -like orbital along the  $[110]$  direction.

## 2.2 Photoluminescence

Photoluminescence (PL) is an optical method for characterisation of light emitting centres, by means of photonic excitation. Other methods to produce luminescence can also be employed, such as accelerated electrons, electric fields, and heat, for cathode-, electro-, and thermo-luminescence respectively. Luminescence occurs when a system in an excited electronic state relaxes to a lower energy state by a radiative process. For reviews of this technique, see Davies (1981); Lightowlers (1990); Davies (1999), and in particular the detailed report on luminescent centres in silicon by Davies (1989).

### 2.2.1 Excitations in silicon

It is beyond the scope of this thesis to describe the PL technique in detail, and attention will be focused only on relevant issues to the present work, i.e., a brief description of bound-exciton luminescence in defective silicon crystals. Silicon has a 1.17 eV indirect band-gap ( $E_g$ ), and in a PL experiment, the excitation source normally injects photons with energy  $h\nu > E_g$ , such that electron-hole (EH) pairs are created. Thermalisation of these pairs rapidly occurs, as they accumulate at the band edges.

Electrons and holes can relax via several routes, namely by being captured by carrier traps (defects), electron-hole recombination, and free-exciton (FE) formation (Lightowlers, 1990; Dean and Herbert, 1979). In the first process, defects are charged, and eventually discharged such thermodynamic equilibrium is recovered. In the last route, formation of free-excitons can be followed by FE-recombination or impurity trapping. Here we say that a bound-exciton (BE) is formed, which ultimately can decay via BE-recombination. Other processes which are less relevant to this work can also occur. In particular, with intense light sources, bound-multiexciton and electron-hole drops are normally observed

(Lightowers, 1990). Note that the indirect gap in silicon makes FE annihilation possible only when accompanied by phonon emission, giving rise to long FE life-times of up to 60  $\mu\text{s}$  in very pure crystals (Merle *et al.*, 1978), allowing them to migrate several hundreds of  $\mu\text{m}$ .<sup>1</sup> In the presence of defects the FE life-time decreases drastically due to capture and BE formation.

## 2.2.2 Vibronic coordinate diagram

Electronic transitions associated with defects are in principle accompanied by local bonding changes. We would then expect that the sudden change on the electronic charge density during the transition will also imply a change in the vibrational state. These coupled electronic-vibrational transitions are referred as *vibronic transitions*. In Figure 2.4 the configuration coordinate of a system is shown. Here the total energy of a crystal with some defect is shown as a parabola centred at the equilibrium atomic configurations ( $Q_g$  and  $Q_e$  for the ground and excited states respectively). This idealised system has one unique normal mode  $Q$  for atomic vibration. Assuming that the harmonic term of the inter-atomic potential is the same in both states,

$$E_g(Q) = \frac{1}{2}\mu\omega^2(Q - Q_g)^2 \quad (2.26)$$

$$E_e(Q) = h\nu_0 + \frac{1}{2}\mu\omega^2(Q - Q_e)^2, \quad (2.27)$$

where  $\mu$  and  $\omega$  are the reduced mass and frequency of an oscillator with a normal coordinate  $Q$ . As shown in Figure 2.4, both electronic states possess their own set of phonon states separated by  $\hbar\omega$ .

Now let us suppose that we populate the excited state by illuminating the system. For  $T = 0$  K, thermalisation rapidly pulls the system towards the zero-phonon state with an energy of  $h\nu_0 + \hbar\omega/2$ . According to the Frank-Condon principle, light emission correspond to the downward bold transition in Figure 2.4, where the electronic state is changed in a much

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<sup>1</sup>Here the FE diffusivity of  $34 \text{ cm}^2\text{s}^{-1}$  at 20 K was used (Cuthbert, 1970).

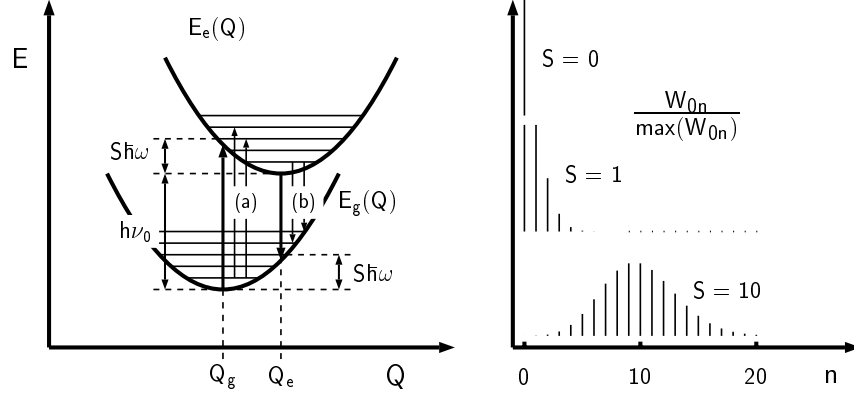


Figure 2.4: Configuration coordinate diagram for the ground and excited states around their equilibrium coordinates  $Q_g$  and  $Q_e$  respectively (left hand side). Absorption and emission processes are labelled as (a) and (b). Electronic transitions are assumed to be coupled by one unique normal mode  $Q$ . On the right side, relative intensities for  $n$ -phonon transitions at  $T = 0$  K are given for three different degrees of coupling.

smaller time scale than atomic relaxation. However, real emission spectra are normally composed of several peaks, corresponding to the number of phonons created during the process. These are the (b) type vibronic transitions in the same figure, where 3 and 4 phonons are created respectively. At  $T = 0$  K the transition probability associated with the creation of  $n$  phonons is given by

$$W_{0n} = \frac{S^n}{n!} e^{-S}, \quad (2.28)$$

where  $S$  is known as the Huang-Rhys factor. The physical significance of “S” can be understood as follows. If the excited state in (2.27) is expressed in terms of the ground state, we get a linear term in  $Q$  coupling the two states, i.e.,

$$E_e(Q) = \frac{1}{2}\mu\omega^2(Q - Q_g)^2 - \mu\omega^2\Delta Q \cdot Q + \frac{1}{2}\mu\omega^2(\Delta Q)^2 + h\nu_0, \quad (2.29)$$

where  $\Delta Q = Q_e - Q_g$ .

Hence, after a “vertical” excitation, the energy given by

$$E_e(Q_g) - E_g(Q_g) = \frac{1}{2}\mu\omega(\Delta Q)^2 = S\hbar\omega \quad (2.30)$$

is involved in phonon creation, and a “vertical” relaxation will most probably emit a photon with energy  $h\nu_0 - S\hbar\omega$ . Therefore  $S$  is the most probable number of phonons created (or annihilated) during the luminescence (or absorption) process.

A pure electronic transition (with no phonon creation) will occur with photon emission with an energy of  $h\nu_0$ . The spectral feature associated to this type of transition is normally referred as zero-phonon line (ZPL). However, if phonons are created, then a low energy side-band will appear below the ZPL. Since at  $T = 0\text{K}$  the vibronic transition probability between the excited and ground states  $|0, e\rangle$  and  $|n, g\rangle$  is given by Equation 2.28, the total spectrum will be composed by the ZPL plus a series of equally spaced vibronic side bands. This is illustrated on the right hand side of Figure 2.4, where the probability of a series of vibronic transitions is shown for three different values of  $S$ . For  $S = 0$  there is no electron-phonon coupling, and all transitions are purely electronic. For small values of  $S$ ,  $\Delta Q \neq 0$ , and the  $n$ -th side-band will have an intensity proportional to  $W_{0n}$ . Finally, for high values of  $S$  (strong coupling), all vibronic side-bands are modulated by a curve which is asymptotically Gaussian centred on  $h\nu_0 - S\hbar\omega$ .

### 2.2.3 Free-exciton luminescence

Let  $E_n(\mathbf{k})$  represent the electronic band structure for silicon. This is illustrated on Figure 2.5(a), where the one-electron Kohn-Sham energy states are plotted along the (100), (110) and (111) cubic directions within the Brillouin-Zone (BZ). Here, conduction band minima occur at  $\mathbf{k}_i = 0.86 X$ . When free electrons and holes travelling with the same group velocity, i.e.,  $\nabla_{\mathbf{k}}E_c = \nabla_{\mathbf{k}}E_v$ , where subscripts c and b denote conduction and valence band states, they may be driven by their mutual Coulombic attraction and form free-excitons with well defined bound states. A simplistic approach, where the conduction and valence bands are assumed to be spherical in  $\mathbf{k}$ -space and non-degenerate, allows us to identify the electron-hole pair with an hydrogenic problem. Hence, for an electron orbiting

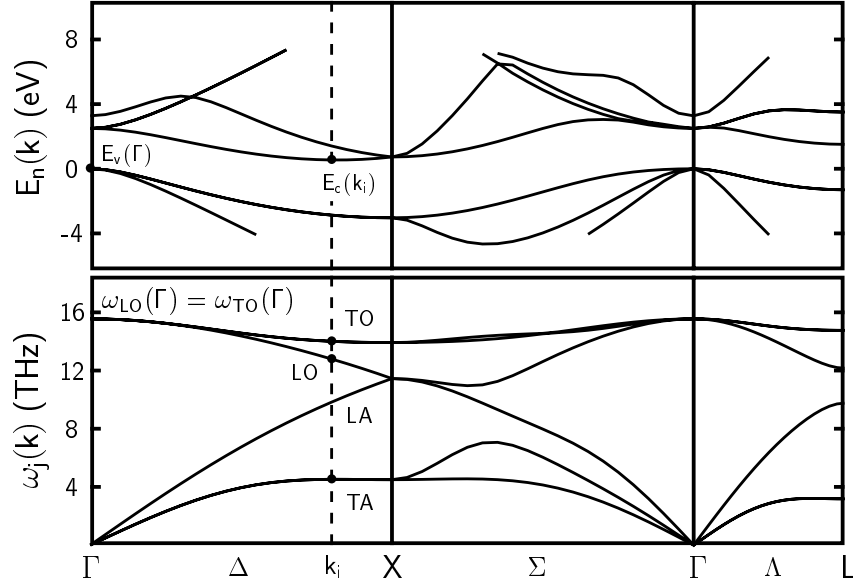


Figure 2.5: One-electron band structure  $E_n(\mathbf{k})$  (top), and phonon dispersion relations  $\omega_j(\mathbf{k})$  (bottom). Band gap  $E_c(\mathbf{k}_i) - E_v(\Gamma) = 0.54$  eV is a consequence of LDA. The phonon dispersion curves were calculated using an extended Keating interatomic potential (Keating, 1966) described by Sangster *et al.* (1992).

around a hole screened by a medium with dielectric constant  $\epsilon$ , the exciton bound states  $E_x(n)$  are given by (Kittel, 1986),

$$E_x(n) = E_g - \frac{\mu e^4}{2\hbar^2 \epsilon^2 n^2}, \quad (2.31)$$

where  $E_g$ ,  $\mu$  and  $n$  are the band-gap, the reduced mass of the electron-hole pair and the principal quantum number respectively. Given the ellipsoidal character and location in  $\mathbf{k}$ -space of the conduction band bottom in Si, a mass tensor must be used, and a more sophisticated approach is normally employed where band-extrema wavefunctions are used as a basis set to describe the exciton states (Cho, 1979). In this case  $s$  and  $p$  states are split due to the non-spherical conduction band minima as described in effective-mass theory (EMT). Direct optical transitions between  $1s$  and three non-degenerate  $2p$  states have been observed in silicon at 10.2, 11.4 and 12.0 meV (Lipari and Altarelli, 1976).



FE travel with a crystal momentum  $\hbar \mathbf{k}_i$  (see Figure 2.5). In principle FE recombination must be accomplished by creation or annihilation of a phonon with momenta  $\hbar \mathbf{k}_i$  or  $-\hbar \mathbf{k}_i$  respectively.<sup>2</sup> At low temperatures and in very pure crystals (trap free), FE luminescence can however be observed when multi-phonon coupling occurs (Dean *et al.*, 1967). In Figure 2.5 a calculation of the phonon dispersion relations for silicon is shown, where one can see that single-phonon assisted luminescence must be compensated by  $\hbar \omega_{TO} = 58.0$  meV,  $\hbar \omega_{LO} = 56.2$  meV, or  $\hbar \omega_{TA} = 18.4$  meV at  $\mathbf{k}_i$ , producing a series of phonon side-bands on the low energy side of a very weak ZP-line.

## 2.2.4 Bound-exciton luminescence

Given the wide separation in  $\mathbf{k}$ -space between the conduction band bottom and the valence band top, FE recombination probability is low in pure Si crystals. The FE life-time is strongly dependent on defect concentration. It goes from as long as 60  $\mu\text{s}$  in the purest floating-zone crystals, to 2  $\mu\text{s}$  when the boron concentration is only  $\sim 10^{12} \text{ cm}^{-3}$ . Impurities and defects can act as traps, confining the electron-hole pair on its neighbourhood with a binding energy  $E_{\text{bx}}$ .  $E_{\text{bx}}$  is a defect dependent quantity, representing the necessary energy to free the exciton. An exciton bound to a defect is referred as a bound exciton (BE) in contrast with the highly mobile FE. A BE can also be thought of an excited state of the defective crystal. Here, the defect is “partially” ionised, simultaneously binding an electron and a hole, much like a long lived transition state between the neutral and the ionised defects. Calculations on bound-excitons has been successful by using effective-mass theory (see Subsection 2.5.2) Stoneham and Harker (1975).

Returning to the configurational diagram (Figure 2.4), the excited state now represents a BE trapped by a defect with a vibrational coordinate  $Q$ . The ground state is attained after BE-recombination. In the excited state, either electron and hole can be more or less tightly bound to the defect. For example, the C-line in Si, believed to arise from the interstitial carbon-oxygen complex, has been shown to have an excited state made up

<sup>2</sup>Zero-phonon recombination has been reported due to small deviations from the cubic environment (Dean *et al.*, 1967).

from a strongly bound hole and a weakly bound electron (Thonke *et al.*, 1985). In fact, Kleverman *et al.* (1988) had shown that this excited state is responsible by a series of effective-mass-like photoluminescence excitation lines due to an electron weakly bound to a positive “pseudo”-ion.

### 2.2.5 Experimental aspects

Photoluminescence experiments can be performed using above or below band-gap excitation. Using below band-gap photoexcitation, light is not absorbed by the crystal, but centres can be directly excited, and by tuning the photon energy one can measure the response of the centre in frequency. This is called photoluminescence excitation spectroscopy (Davies, 1999). More commonly, above band-gap sources are used. Here, Ar<sup>+</sup> (2.41 eV) or Kr<sup>+</sup> (1.84 eV) gas state lasers are then employed. The penetration depth of these sources is of few  $\mu\text{m}$ , which has drastic experimental implications. In indirect band-gap semiconductors like silicon, FE’s can travel through the crystal, and store energy in defects by being captured. We then expect radiative decay to mirror somewhat the chemical and structural environment of the excited centre.

Isotopic effects can be detected in phonon sidebands As  $\omega \propto 1/\sqrt{\mu}$ , the change of the reduced mass  $\mu$  of an oscillator leads to a shift in the side-bands separation. However, in a particular local vibrational mode not all atoms necessarily contribute to  $\mu$ , and symmetry considerations must be taken into account. Nevertheless, it is possible to extract useful information about the chemical nature of a defect when a shift of a phonon sideband series is observed after isotopic substitution. For example, in a vibrational mode strongly localised around an oxygen atom, the isotopes <sup>16</sup>O and <sup>18</sup>O will be responsible for the appearance of two phonon replicas, where the frequency of the heavier mode will be approximately  $\sqrt{16/18} = 0.943$  of its lighter counterpart.

Isotopic effects are not an exclusive feature of phonon sidebands. Normally, as the electronic wavefunctions for excited and ground states are different, one should expect a different zero-phonon frequency for each of them, i.e.,  $\hbar\omega_g \neq \hbar\omega_e$ , and therefore, any change

in the reduced mass of the mode that couples both states should produce a shift in the ZP-line.

## 2.3 Deep level transient spectroscopy

In contrast to substitutional dopants that produce shallow states near the band edges, other impurity complexes are associated with deep and localised states. This is the case of various radiation-induced defects such as the vacancy (Watkins, 1992), divacancy (Watkins and Corbett, 1965; Coomer *et al.*, 1999b), or the vacancy-oxygen complex (Watkins and Corbett, 1961a; Kimerling, 1976). In this section, another spectroscopic technique, namely deep level transient spectroscopy (DLTS), first introduced by Lang (1974a), is described. Excellent review articles can be found in the literature (Miller *et al.*, 1977; Palmer, 1990; Mooney, 1999), and therefore a brief overview is given here.

### 2.3.1 Deep states in semiconductors

Defects having deep states in the band gap are characterised by ionisation or affinity energies of about or greater than  $E_g/10$ , implying a deep potential valley that makes the electron or hole wavefunction strongly localised around the defect. In thermal equilibrium, the charge state of a particular defect is governed by the steady state ejection and capture processes, which depend on doping, temperature and sample compensation. As a consequence, the chemical potential of electrons or holes for which a defect changes its charge state, will define a level within the band gap. Defects are normally classified as traps, generation or recombination centres, depending on the relative capture processes. If  $(e_n, e_p)$  are the electron and hole emission rates, and  $(c_n, c_p)$  their respective capture rates, we can classify deep level defects according to Figure 2.6. In that figure, a) shows an electron trap, where electron capture and ejection rates are favoured, and governing its charge state. An analogous situation is the one in b), but here, the defect behaves as a hole trap. Generation centres are those where electron and hole emission rates dominate the occupancy dynamics, and recombination centres are those that have large capture rates,

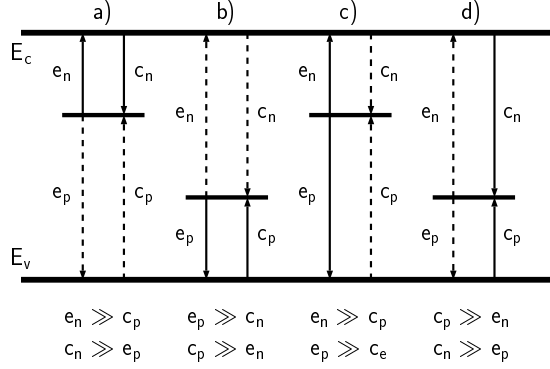


Figure 2.6: Scheme of traps, generation and recombination centres.  $E_c$  and  $E_v$  are the conduction and valence band edges respectively.  $e_x$  and  $c_x$  are the carrier ejection and capture rates, where  $x$  can be  $n$  or  $p$  for electrons and holes respectively.

so favouring the annihilation of electron-hole pairs [see c) and d) respectively]. Capture rates are given by

$$c_n = \sigma_n \langle v_n \rangle n \quad (2.32)$$

$$c_p = \sigma_p \langle v_p \rangle p, \quad (2.33)$$

where  $\sigma_n$  and  $\sigma_p$  are the electron and hole capture cross sections, and  $n$  and  $p$  are the free electron and hole concentration, respectively. The average electron or hole velocities  $\langle v_n \rangle$  and  $\langle v_p \rangle$  correspond to thermal averages, and assuming free carrier gases, these are given by

$$\langle v_n \rangle = \sqrt{\frac{3k_B T}{m_e^*}} \quad \text{and} \quad \langle v_p \rangle = \sqrt{\frac{3k_B T}{m_h^*}}, \quad (2.34)$$

where  $k_B$  is the Boltzmann constant and  $m_e^*$  and  $m_h^*$  are the electron and hole effective masses at their respective band edges.

At non-zero temperatures, thermal emission occurs. If  $\Delta E_n = E_c - E_T$  and  $\Delta E_p = E_T - E_v$  are depths of electron and hole traps measured from the conduction and valence

band extrema respectively,  $e_n$  or  $e_p$  will be proportional to a Boltzmann factor involving these energy differences. Hence  $\Delta E_n$  and  $\Delta E_p$  are free energies of ionisation. Following the principle of detailed balance, the emission and capture rates must match in thermal equilibrium, allowing us to write

$$e_n = \frac{\sigma_n \langle v_n \rangle N_c}{g} \exp(\Delta S_n/k_B) \exp(\Delta H_n/k_B T) \quad (2.35)$$

$$e_p = \sigma_p \langle v_p \rangle N_v g \exp(\Delta S_p/k_B) \exp(\Delta H_p/k_B T). \quad (2.36)$$

Here, we split each free energy into the entropy  $S$  and enthalpy  $H$  for the electron and hole trapping processes respectively.  $N_c$  and  $N_v$  are the densities of states for the conduction and valence bands respectively, and  $g$  the degeneracy of the trap. Note that  $N_c \propto T^{3/2}$  and the average velocities  $\langle v_p \rangle \propto T^{1/2}$ , and therefore  $\langle v_p \rangle N_c \propto T^2$  which must be taken into account when plotting the Arrhenius relations given by 2.35 and 2.36.

### 2.3.2 Measurements of the transient capacitance

In a semiconductor p-n junction or a Schottky diode, a carrier-depleted space charge region is formed as a consequence of an electric dipole across the junction. The width of this space charge layer can be controlled by applying an external potential difference, and therefore, we can think of this device as a variable capacitor. For p<sup>+</sup>-n or n-type Schottky diodes, the width of the space-charge is given by the well known expression,

$$W = \sqrt{\frac{2\epsilon(V_0 + V)}{eN_D}} \quad (2.37)$$

where  $\epsilon$  is the permittivity of the material,  $V_0$  and  $V$  the built-in and external potentials,  $e$  is the electron charge, and  $N_D$  the density of ionised donor dopants in the lightly doped side of the junction. The device capacitance is readily obtained as

$$C = \frac{\epsilon A}{W} = \sqrt{\frac{e\epsilon N_D}{2(V_0 + V)}} \quad (2.38)$$

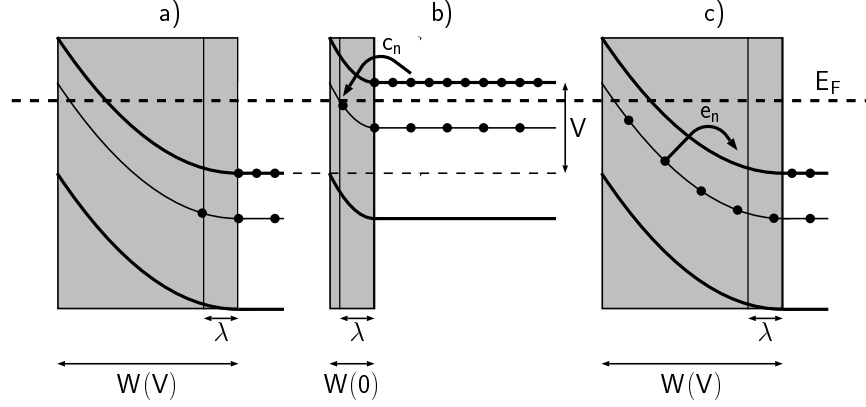


Figure 2.7: Band-structure diagram for the n-type side of a  $p^+-n$  junction or Schottky diode, under a majority-carrier pulse. Steps shown are a) before the pulse under reverse-bias, b) during pulse with zero voltage, and c) after pulse under reverse-bias applied voltage  $V$ .

where  $A$  is the junction area. The very important feature of these junctions is that after an electron or hole is emitted to the respective band edge, it is promptly expelled out of the depletion region in a time scale of  $10^{-12}$  to  $10^{-10}$  s, and therefore avoids being re-trapped by the impurity or other defects Mooney (1999).

As an example, let's consider Figure 2.7. Here we show the variation of the depletion region during a majority-carrier pulse. In the same figure we also show the band bending and a deep electron trap in the top half of the band gap. Outside the space-charge region the Fermi level is locked around the dopant level. Let us assume that the input signal is  $V$  (reverse bias) when  $t < t_i$  and  $t > t_f$ , and zero when  $t_i < t < t_f$ . Starting in a), with a steady state reverse bias  $V$ , one can notice that all the carriers are depleted from a region of width  $W$  given by equation 2.37. However, in the right-most side of the depletion region there is a low concentration of free carriers that can be captured by electron traps. This is called the transition region and its width  $\lambda$  depends on the Fermi and trap levels  $E_F$  and  $E_T$ , i.e.,

$$\lambda = \sqrt{2\epsilon \frac{E_F - E_T}{e^2 (N_D - N_T)}}, \quad (2.39)$$

where normally  $N_D - N_T \approx N_D$ . In the transition region the electron capture rate is higher than the ejection rate, and therefore the charged defect has a long life time here. After  $t = t_i$  [see b)], a zero-bias pulse is applied to the junction for sufficient time that all traps are filled; then after the pulse (at  $t > t_f$ ), there is a transient regime that is due to thermally-induced emission of electrons from the traps [see c)] at a rate  $e_n$  such that the space-charge region is recovered.

During the filling process, the density of filled traps  $n_T(t)$  is given by

$$n_T(t) = N_T (1 - e^{-c_n t}) \quad (2.40)$$

whereas during the transient emptying process,

$$n_T(t) = N_T e^{-e_n t}. \quad (2.41)$$

Assuming  $N_D \gg N_T$ , the capacitance of the junction per unit area can be written as

$$C(t) = C_0 \left[ 1 - \frac{N_T}{2N_D} \exp(-e_n t) \right], \quad (2.42)$$

where  $C_0$  is the quiescent capacitance given by Equation 2.38. The relative temporal capacitance change  $(\Delta C/C_0)$ , which is the sensitivity of the junction to trapped charges, is then

$$\frac{\Delta C}{C_0} = -\frac{N_T}{2N_D} \exp(-e_n t). \quad (2.43)$$

Note that the sign of the capacitance change is negative when emission majority carriers takes place and positive for minority carriers. This feature makes it easy to know which type of carriers are being emitted.

In a DLTS experiment, periodic filling pulses are applied to a reverse biased junction, where the  $C(t)$  transients having different temperature-dependent time constants  $\tau = 1/e_n$  are

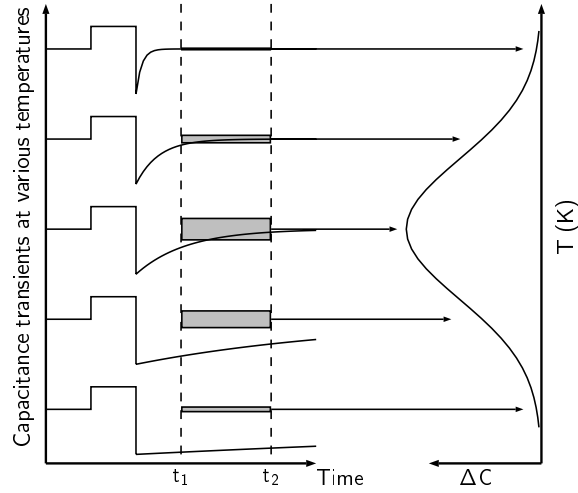


Figure 2.8: Implementation of a DLTS rate window by means of a boxcar differentiator with gates set at times  $t_1$  and  $t_2$

studied. In Figure 2.8 the box-car method (Lang, 1974*a,b*), is depicted. Here, a DLTS signal defined as  $C(t_2) - C(t_1)$  is measured, and this signal has a maximum value at the temperature for which

$$\max(e_n) = \frac{1}{t_2 - t_1} \ln \left( \frac{t_2}{t_1} \right). \quad (2.44)$$

By changing  $t_1$  and  $t_2$ , we alter the temperature  $T$  for which  $\max(e_n)$  occurs. Several pairs  $(T, e_n)$  for the peak of the DLTS signal are extracted, plotted as  $\ln(e_n/T^2)$  versus  $1/T$ , and finally, by fitting the pre-exponential factor and power arguments in Equations 2.35 and 2.36, we obtain  $\Delta H$  and the capture cross section of the defect.

### 2.3.3 DLTS signal of the VO complex in Si

The vacancy-oxygen complex in silicon (or A-centre), is probably one of the best examples of an electron trap. Among other observations, the thermal behaviour of the DLTS and EPR signals were soon correlated. The defect was shown to be stable in the neutral and negative charge states, with an acceptor state 0.17 eV deep below the conduction band (Kimerling, 1976; Meese *et al.*, 1983).



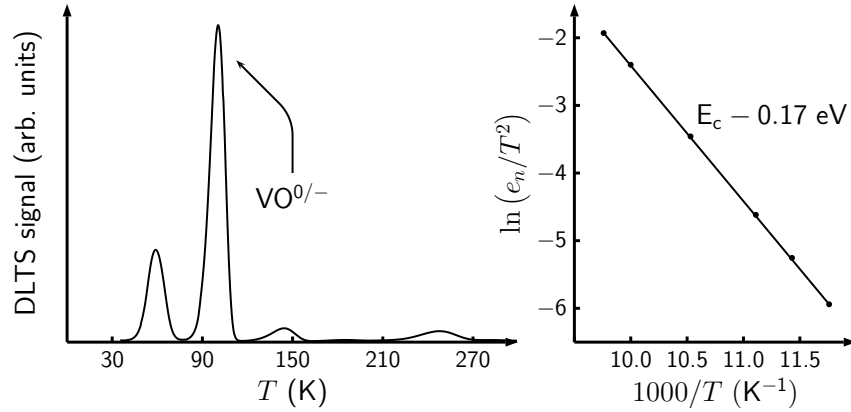


Figure 2.9: DLTS spectrum from a Cz-Si sample which has been irradiated with fast electrons at room temperature (on the left). The main defect produced after this treatment is the vacancy-oxygen complex (VO), which has a deep acceptor state 0.17 eV below the conduction band (on the right). Experimental data kindly provided by L. Rubaldo.

On the left side of Figure 2.9, a typical DLTS spectrum of silicon irradiated with fast-electrons (2 MeV) at room temperature, is shown. Among all features, the labelled peak around 100 K corresponds to the A-centre signature. Its thermal analysis allows us to obtain a thermal enthalpy  $\Delta H = 0.17$  eV for emission of the trapped electron into the conduction band. It must be noticed here that the temperature at which the emission rate is measured is much less than that to anneal out the VO defect ( $\sim 300\text{-}350^\circ\text{C}$ ). Obviously this is not always the case, where deeper traps with low thermal stability may not be measurable by DLTS.

## 2.4 Infra-red vibrational spectroscopy

The presence of defects in a crystalline host destroys at least the translational symmetry of the lattice, modifying the storage of vibrational energy in two main ways: By perturbing the vibrational density of states, where any new mode strongly overlaps existing host modes, or by introducing modes such their frequencies lie in spectral regions which are forbidden in the perfect crystal. In the first case the mode is called resonant, whereas in

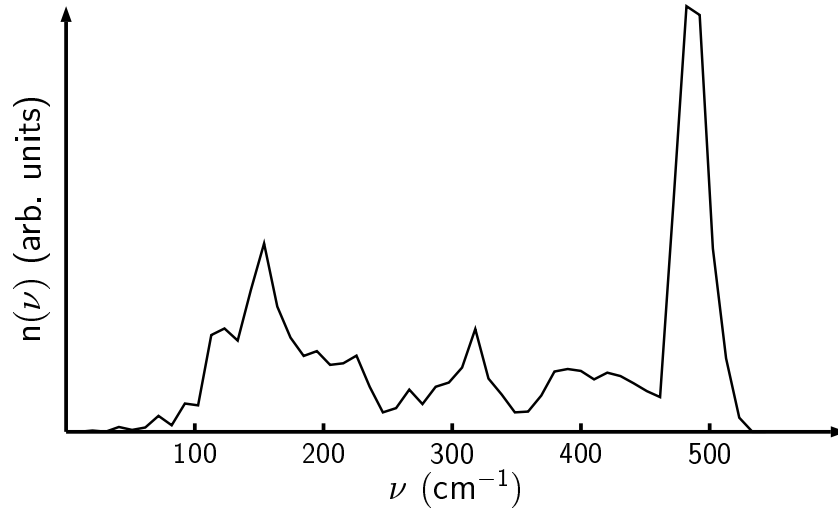


Figure 2.10: Calculated phonon density of states in silicon, using the extended Keating potential (Sangster *et al.*, 1992).

the second the mode is said to be localised, and its coupling with the lattice phonons is weak. Localised modes are normally divided into two classes, i.e., the local modes which appear above the maximum frequency allowed by the perfect crystal, and the gap modes which appear within gap regions. One can see from Figure 2.10 that we can not have gap modes in Si, as phonons with energies  $0 \leq \nu \leq \nu_R$  are allowed, with a maximum  $\nu_R = 523 \text{ cm}^{-1}$  called Raman frequency for Si.

Absorption of IR radiation by one-phonon excitation processes in group-IV semiconductors is forbidden. The presence of the inversion element in the space group implies a vanishing coupling between the optical modes at  $\Gamma$  and the electric field. However, multi-phonon processes are possible, providing that the total momentum created is zero and the selection rules are satisfied. In fact, particularly strong absorption occurs around  $\sim 600 \text{ cm}^{-1}$  and  $\sim 1000 \text{ cm}^{-1}$  in Si, which unfortunately is the region of many impurity related absorption features, including the thermal double donors.

In this section, the interpretation of vibrational IR absorption measurements is given. This includes the IR band strength and line width, mass and charge state effects. More detailed sources and further information can be found in works by Newman (1973); Stavola (1999)

and McCluskey (2000).

### 2.4.1 Local modes and integrated absorption

Not all local modes are IR-active. The electric dipole moment  $\boldsymbol{\mu}$  induced by a group of atoms oscillating about their equilibrium positions with a normal mode  $Q$ , can be expanded in a power series of  $Q$ , i.e.,

$$\boldsymbol{\mu} = \boldsymbol{\mu}_0 + \left(\frac{d\boldsymbol{\mu}}{dQ}\right)_0 Q + \left(\frac{d^2\boldsymbol{\mu}}{dQ^2}\right)_0 Q^2 + \dots, \quad (2.45)$$

where  $\boldsymbol{\mu}_0$  is the static electric dipole, and the derivatives are to be taken at the equilibrium configuration. For small vibration amplitudes, we can assume that  $\boldsymbol{\mu}$  is linear with  $Q$ . The transition probability between any initial and final states  $i$  and  $j$  respectively is proportional to  $|\langle i | \hat{\mathbf{e}} \cdot \boldsymbol{\mu} | j \rangle|^2$ , where  $\hat{\mathbf{e}}$  is the polarisation direction of the external electric field. Clearly, only odd terms from equation 2.45 will contribute to a non-zero transition probability. Higher order terms only contribute for a transition probability to higher harmonic states.

The integrated absorption (IA) of an IR band is proportional to the concentration of illuminated defects. Dawber and Elliot (1963) derived the commonly used expression for the IA of a non-degenerate mode with effective mass  $m$  as

$$\text{IA} = \int \alpha(\nu) d\nu = \frac{\pi \eta^2 N}{m n c^2}, \quad (2.46)$$

where  $\alpha$  is the absorption coefficient,  $n$  is the refractive index of the crystal,  $N$  the concentration of absorbing centres, and  $c$  the velocity of light. The quantity  $\eta = |d\boldsymbol{\mu}/dQ|$  has units of electric charge, and is normally referred to as the effective charge of the mode  $Q$ . Note that  $\eta$  is not related to the charge of the defect. In fact, neutral defects with values of  $\eta = 2$  or even higher have been reported (Newman, 1973). The absorption coefficient  $\alpha$  has units of  $\text{cm}^{-1}$ , and is the actual quantity that is measured during the experiments. This is done by relating the intensity of the incident light to that of the escaping beam. In

the absence of internal interference (due to multiple reflections), the transmitted intensity  $I_t$  is related to the incident intensity  $I_0$  by

$$I_t = \frac{(1 - R)^2 e^{-\alpha d}}{1 - R^2 e^{-2\alpha d}}, \quad (2.47)$$

where the  $d$  is the sample thickness, and the reflection coefficient  $R$  is given by

$$R = \frac{(n - 1)^2 + \kappa^2}{(n + 1)^2 + \kappa^2}, \quad (2.48)$$

where  $n$  and  $\kappa$  are the refractive index and the extinction coefficient respectively.

Equation 2.46 is of fundamental interest for spectroscopists since it allows the direct determination of the defect concentration once a calibration factor is known.

### 2.4.2 Temperature effects and band-shape

In general, the band frequency and its width depend on several factors. Among them is the thermal expansion of the lattice, which can perturb the local geometry of the defect, anharmonic coupling with other vibrations including host modes, or the life-time of excited states. Considering the dependence on the temperature due to thermal expansion, we start by defining a second rank tensor  $\mathbf{A}$  that gives us the band shift due to an applied stress given by another second rank tensor  $\boldsymbol{\sigma}$ ,

$$\Delta\omega = \mathbf{A} \cdot \boldsymbol{\sigma}, \quad (2.49)$$

Here,  $\mathbf{A}$  is normally referred as a piezospectroscopic tensor, and can be measured by a variety of spectroscopic techniques (Kaplanski, 1964). Assuming thermal expansion as a negative hydrostatic pressure, one can express  $\boldsymbol{\sigma}$  with help of the crystal elastic constants  $c_{11}$  and  $c_{12}$ , and the fractional change in the lattice parameter  $\Delta a_0(T)/a_0(0)$ , i.e.,

$$\sigma_{ij} = (c_{11} + 2c_{12}) \frac{\Delta a_0(T)}{a_0(0)} \delta_{ij}, \quad (2.50)$$

where  $\Delta a_0(T) = a_0(T) - a_0(0)$ , and  $a_0(T)$  is the crystal lattice parameter at any temperature  $T$ . Any quantitative estimate of  $\Delta\omega$  can be obtained by relating  $\Delta a_0(T)/a_0(0)$  with the thermal expansion coefficient  $\alpha(T)$  for the appropriate material.

Most commonly, low temperature (LT) absorption bands in Si are enhanced by  $\sim 3 - 8 \text{ cm}^{-1}$  when compared with those measured at room temperature (RT). Obviously,  $\Delta\omega$  is strongly dependent on the crystal-defect coupling, and in particular situations, anomalous shifts can in fact be observed. One example is the interstitial oxygen dimer in Si, where the room-temperature frequencies were found to lie  $\sim 0.3 \text{ cm}^{-1}$  above those measured at  $T = 10 \text{ K}$  (Murin *et al.*, 1998; Öberg *et al.*, 1998).

Line broadening is normally explained as due to the finite life-time of the promoted state. When anharmonic coupling with other modes takes place, an additional contribution which is dependent on the occupancy of the partner mode, and therefore strongly  $T$ -dependent, must also be considered. This is true in the case of  $1136 \text{ cm}^{-1}$  dominant band of the interstitial oxygen, where the coupling of an asymmetric mode stretch mode with a low-energy doubly-degenerate bend-mode makes the band shape vary dramatically with temperature (Bosomworth *et al.*, 1970). As recently proposed by Budde *et al.* (2001), a similar picture seems to be applied for the bond-centred hydrogen atom in Si.

### 2.4.3 Isotope and charge effects

Identification of the chemical composition of defects in semiconductors is a primary goal in spectroscopy. IR vibrational spectroscopy, can provide this information from band shifts that occur when samples containing different isotopes are investigated. It is known from a *ball and spring* that model, a diatomic molecule vibrates with a frequency  $\omega \propto \sqrt{1/\mu}$ , where  $\mu$  is the reduced mass of the atomic pair. A similar analysis can be applied to an infinite chain of atoms of mass  $M$  with the appropriate periodic boundary conditions (Kittel, 1986; Stavola, 1999; McCluskey, 2000). Here we get a Raman frequency of

$$\omega_R = \sqrt{\frac{4f}{M}}, \quad (2.51)$$

where  $f$  is some intrinsic force constant associated with the spring that binds each atom to its neighbours. Substitution of one chain-atom by another with mass  $m$  (keeping the same force constants), can lead to two distinct situations. If  $m \geq M$ , the density of vibrational states will be perturbed by the presence of an impurity mode below  $\omega_R$ , i.e., a resonant mode. However, if  $m < M$ , this perturbation appears above  $\omega_R$  as a local vibrational mode (LVM) with some frequency  $\omega_L$ . This last situation is of particular interest here, since these LVMs can be accurately predicted with *ab-initio* calculations. Resonant modes are normally calculated by perturbative methods (Montroll and Potts, 1955; Maradudin, 1966), and will not be discussed here.

The empirical diatomic model has been applied quantitatively to estimate isotopic shifts of impurities in crystals (Newman, 1973). Here, the LVM frequency is given by

$$\omega_L = \sqrt{f \left( \frac{1}{\alpha M} + \frac{1}{m} \right)} \quad (2.52)$$

where  $1 \leq \alpha \leq 4$  is a parameter that takes into account the coupling of the impurity with the host atoms. For example, the interstitial oxygen in silicon sits in the bond centre site, where  $^{16}\text{O}$  and  $^{18}\text{O}$  isotope versions produce absorption bands at 1136 and 1084  $\text{cm}^{-1}$  at liquid He temperatures respectively. The ratio  $^{16}\omega/^{18}\omega = 1.048$  can be compared with its estimated value by using equation 2.52, where  $^{16}\omega/^{18}\omega = 1.046$  is obtained by using  $\alpha = 2$  to account for two Si neighbours.

Although this approach works well with simple substitutional and interstitial impurities, it gives rather poor results for the absolute band frequencies. One certainly loses any faith on this model when treating complex defects where chemical bonding properties can be accurately described only with more sophisticated methods.

Another important phenomenon which can produce a shift in a LVM is associated with charge state effects. When a particular defect is electrically active, the capture or emission of carriers can change dramatically the local environment. The bonding properties (which can be interpreted as the spring force constants), are then perturbed, and the vibrational mode frequency will differ from that of the uncharged defect. The vacancy-oxygen complex

in Si is perhaps an obvious example, where the absorption band associated to the anti-symmetric mode of the Si-O-Si unit is shifted by  $\sim 50 \text{ cm}^{-1}$  when comparing the negative charge state with the neutral defect.

#### 2.4.4 IR absorption of the VO defect

The vacancy-oxygen complex (or substitutional oxygen) in silicon is the main product after annealing irradiated Cz-Si. It is a well studied defect by LVM-spectroscopy (Corbett *et al.*, 1961; Bean and Newman, 1971; Lindström *et al.*, 1999a). As the O atom bridges two second neighbouring Si atoms (see Figure 2.3), the longer Si-O-Si unit when compared with that in  $O_i$ , is responsible for a lower anti-symmetric stretch mode frequency at  $835 \text{ cm}^{-1}$ , compared with  $1136 \text{ cm}^{-1}$  for  $O_i$ . Since the VO defect can be in two different charge states, we concentrate first on the neutral. The  $835 \text{ cm}^{-1}$ -band can be seen in lower spectrum on Figure 2.11 under the  $V^{16}\text{O}^{(0)}$  label. In the upper spectrum, at  $799 \text{ cm}^{-1}$ , we have the same mode observed in a sample doped with  $^{18}\text{O}$  isotopes. This observation demonstrates unequivocally the presence of at least one O atom in the defect. In samples with both  $^{18}\text{O}$  and  $^{16}\text{O}$  isotopes only the  $835$  and  $799 \text{ cm}^{-1}$ -bands are observed, where the absence of mixed modes strongly supports the presence of only one O-atom in the defect.

As it was shown in Subsection 2.3.3, the VO defect possesses an acceptor level at  $E_c - 0.17 \text{ eV}$ . Therefore, in thermodynamic equilibrium, the negative charge state will be populated according to the position of the Fermi level. Although the spectra in Figure 2.11 were recorded from high resistivity samples, the constant presence of the excitation source pumps electrons to the conduction band, which are then trapped by VO defects. Therefore  $\text{VO}^{(0)}$  and  $\text{VO}^{(-)}$  are detected simultaneously. From the same figure we can notice dramatic increase in the frequencies (by  $\sim 50 \text{ cm}^{-1}$ ) for the negative defects compared with their neutral counterparts. The  $^{18}\text{O}$  rich sample had a high concentration of carbon, leading to the presence of a band at  $865 \text{ cm}^{-1}$  which belongs to an interstitial carbon-oxygen complex.

LVM calculations on the VO defect was previously done by Ewels *et al.* (1995) and Pesola *et al.* (1999a), who assigned an anti-symmetric stretch mode localised on the Si-O-Si

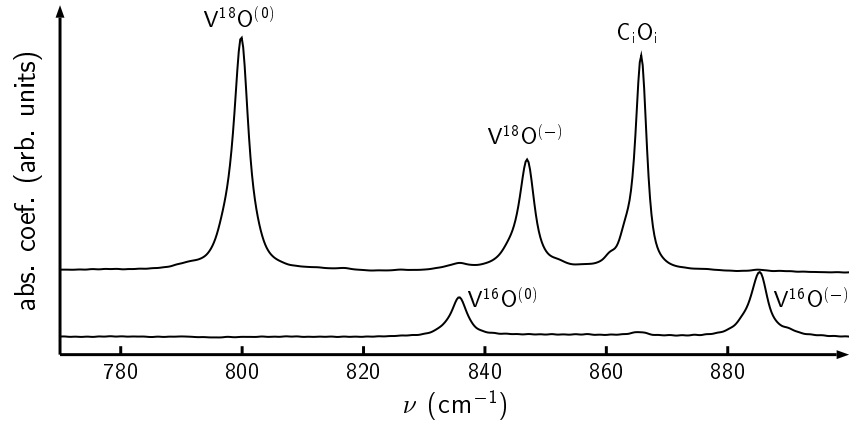


Figure 2.11: Infra-red absorption of the VO defect in Cz-silicon at 10 K. Upper spectrum was measured in a C-rich sample enriched with  $^{18}\text{O}$ . Lower spectrum is from a C-lean with naturally abundant oxygen. Experimental data kindly provided by J. Hermansson.

unit to the  $835\text{ cm}^{-1}$ -band. Also recently, a frequency enhancement mechanism for the negative defect was proposed (Coutinho *et al.*, 2000*b*). It is suggested that after filling an anti-bonding state with the trapped electron, a Coulombic repulsion between the high electron density region between the two Si-dangling bonds and the O-atom, flattens the Si-O-Si unit, strengthening the Si-O bonds.

## 2.5 Electronic IR-Absorption

### 2.5.1 Introduction

Substitution of a host Si atom by a singly-ionised group-V species, leaves all neighbouring Si atoms saturated, and the band-gap free of deep states. However, the excess of positive charge at the substitutional defect creates an attractive potential. In fact this potential is asymptotically Coulombic and slowly varying. This property is particularly useful as any electron moving in this potential spends most of its time in this far region. The properties of the extra electron (needed to neutralise the system), are then analogous to those in the hydrogen problem. However, as the potential is strongly screened by the medium, the



binding energy of this electron is of the order of 50 meV in Si. That is why these defects are normally called shallow donors or acceptors, or shallow dopants when deliberately introduced. Energy levels of excited states are commonly observed in the form of a Lyman series ( $1s \rightarrow 2p$ ,  $1s \rightarrow 3p$ , ...), or even the Balmer series ( $2s \rightarrow 3p$ ,  $2p \rightarrow 3s$ , ...). All these observations are very well described by effective-mass theory (EMT), early developed by Kohn (1955, 1957), and reviewed by Stoneham (1975); Ramdas and Rodriguez (1981).

On the other hand, some group-VI atoms (S, Se and Te), as well the thermal double donors, are known to produce a He-like series of excited states, behaving as double donors (Glodeneau, 1967; Ning and Sah, 1971; Grimmeiss and Janzén, 1992). Although substitutional chalcogen atoms create deep states in the gap (about 0.2-0.3 eV for the first ionisation energy), their infrared absorption spectra can still be interpreted within the EMT, and the comparison with the TDD defects is of considerable interest.

### 2.5.2 Effective-mass theory

The electronic band structure of Si has an indirect gap. This is shown on the top half of Figure 2.5, where the conduction band minima at  $\mathbf{k}_i$  is about  $0.8 \times 2\pi/a_0$  away from the valence band top. There are six equivalent minima along  $\langle 100 \rangle$  directions with effective mass of  $m_t = 0.19 m_e$  and  $m_l = 0.92 m_e$ , where  $m_e$  is the free-electron mass.

Let us imagine that a singly ionised group-V or doubly ionised group-VI atom replaces a host atom from a group-IV crystal with an isotropic conduction band minimum, and effective mass  $m_e$ . All four valence electrons may be assumed to form  $sp^3$  hybrid orbitals with four neighbours. The excess of positive charge  $Z$  at the impurity then generates a screened Coulomb potential

$$V_i = -\frac{Z}{\epsilon r}, \quad (2.53)$$

within the crystal with permittivity  $\epsilon$ . This equation is not valid in the neighbourhood of the impurity (often referred as central-cell region), but it is a good approximation for

$r \gg a_0$ . If an electron is brought back into the crystal, it will move with effective-mass  $m_e$  in the hydrogen-like potential  $V_i$ , and similarly to the hydrogen atom, a series of bound states at  $E_b$  below the conduction band will appear, where

$$E_b = \frac{Z^2 m_e}{2\epsilon^2 n^2} \quad (2.54)$$

In Equation 2.54,  $n = 1, 2, \dots$ . For a singly ionised group-VI impurity in the ground state, partial screening occurs and we may assume  $Z \approx 1$  when considering to bring back another electron.

In a more rigorous way to treat the problem in Si, we must assume all six equivalent conduction band minima, and an *hydrogenic* wavefunction is expanded in terms of Bloch functions  $\psi_{n\mathbf{k}}$ , but assuming that only conduction-band states ( $n = 0$ ) contribute appreciably to the wavefunction, i.e.,

$$\Psi(\mathbf{r}) = \sum_{j=1}^6 \alpha_j F_j(\mathbf{r}) \psi_{0\mathbf{k}_j}(\mathbf{r}). \quad (2.55)$$

Here the index  $j$  runs over the six conduction-band minima, the coefficients  $\alpha_j$  are evaluated numerically (disregarding redundancy arising from time-reversal and defect symmetry).  $F_j$  is known as hydrogen-like envelope function belonging to the  $j$ -th minimum, and solution of the the following hydrogenic Hamiltonian,

$$\left[ -\frac{\hbar^2}{2m_t} \left( \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) - \frac{\hbar^2}{2m_l} \frac{\partial^2}{\partial z^2} + V_i(\mathbf{r}) \right] F_j(\mathbf{r}) = E_b F_j(\mathbf{r}). \quad (2.56)$$

In Equation 2.56 the anisotropy of the conduction band minima is taken into account, hence splitting the p states into  $p_0$  and  $p_{\pm}$ . This makes every s,  $p_0$  and  $p_{\pm}$  states six-, six- and twelve-fold degenerate for an impurity with  $T_d$  symmetry. However, due to inter-valley coupling, this symmetry is lifted as a maximum of three-fold degeneracy is possible in Si. Fully symmetric s and  $p_0$  states unfold into  $A_1 + E + T_2$ , and  $p_{\pm}$  states into  $2T_1 + 2T_2$  (Ramdas and Rodriguez, 1981). This splitting is shown schematically in Figure 2.12 for a

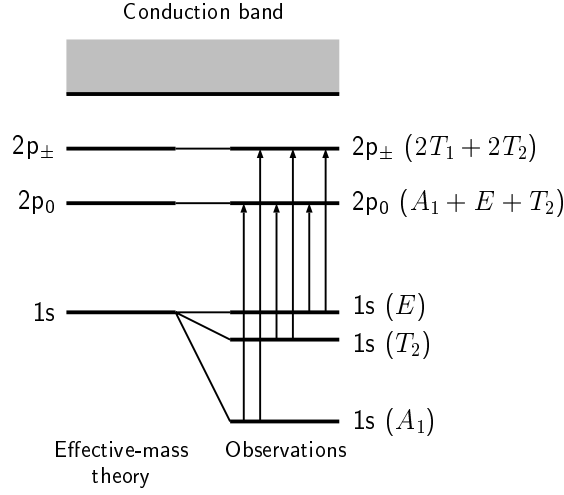


Figure 2.12: Energy level scheme of a substitutional donor in Si. Irreducible representations from a  $T_d$  point group are also shown.

substitutional donor, where the coefficients  $\alpha_i$  for an s state can be deduced by inspection (Tinkham, 1964) as

$$\begin{aligned}
 \alpha_i^{A_1} &= \frac{1}{\sqrt{6}} (1, 1, 1, 1, 1, 1) \\
 \alpha_i^{E'} &= \frac{1}{\sqrt{12}} (-1, -1, -1, -1, 2, 2) \\
 \alpha_i^{E''} &= \frac{1}{2} (1, 1, -1, -1, 0, 0) \\
 \alpha_i^{T_2'} &= \frac{1}{\sqrt{2}} (-1, 1, 0, 0, 0, 0) \\
 \alpha_i^{T_2''} &= \frac{1}{\sqrt{2}} (0, 0, -1, 1, 0, 0) \\
 \alpha_i^{T_2'''} &= \frac{1}{\sqrt{2}} (0, 0, 0, 0, -1, 1).
 \end{aligned} \tag{2.57}$$

We note that the wavefunction of the fully symmetric  $A_1$  s-state possesses the maximum amplitude at the origin, making it the ground state for attractive centres. Its binding energy is therefore strongly dependent on the chemical nature of the defect. This is the case of common dopants like substitutional phosphorus or arsenic, according to early EPR experiments by Fletcher *et al.* (1954*a,b*) and Feher (1959*a,b*). However, as group theory is unable by itself to establish the ordering of the split-up, other arrangements are possible. This is the case of interstitial Li in Si, where the ground state was attributed to a five-

fold degenerate  $1s(E + T_2)$  state, 1.8 meV below the  $1s(A_1)$  state (Watkins and Ham, 1970). The isotropic hyperfine interaction on  ${}^7\text{Li}$  was found to be less than 0.1 MHz. This corresponds to a minute spin localisation. Especially when comparing with the 3 MHz measured for the  ${}^{17}\text{O}$  hyperfine on the VO defect, despite the fact the the O atom sits at a node of the paramagnetic wavefunction. This situation is of particular interest here, as the TDD defects in Si were shown to possess a  $1s(T_2)$  ground state, where only two conduction band minima contribute to  $\Psi(\mathbf{r})$  (Stavola *et al.*, 1985). The 12-fold degenerate p-states, in principle, also split. However, as the amplitude of the wavefunction is very small nearby the defect, the split-up is often negligible.

### 2.5.3 Absorption of double donors

It is expected that the substitutional group-VI impurities like S, Se and Te should behave as double donors. DLTS experiments reported emission barriers of 0.587 and 0.302 eV to ionise  $S^+$  and  $S^0$  defects (Grimmeiss *et al.*, 1980). These values were confirmed by IR-absorption, where ground state binding energies of 613.5 and 318.3 meV were found for  $S^+$  and  $S^0$  respectively (Grimmeiss *et al.*, 1982; Jazén *et al.*, 1984). The strong deviation of these values from the EMT binding energies of a He-like donor double donor D [125.08 and 31.27 meV for  $D^+$  and  $D^0$  respectively (Faulkner, 1969)], was reproduced after including a central-cell correction and multi-valley scattering effects in the Hamiltonian (Pantelides and Sah, 1974). This term, affects then the energy separation between s-states. As the  $1s(E)$  states have zero amplitude at  $r = 0$ , their binding energies are expected to be close to the values predicted by EMT. In fact, both  $1s(E)$  and  $1s(T_2)$  states in  $S^0$  were measured to lie 31.6 and 34.62 meV below the conduction band respectively (Jazén *et al.*, 1984, 1985). These are to be compared with EMT  $1s(A_1 + E + T_2)$  degenerate states at  $E_c - 31.27$  meV (Faulkner, 1969). For the same reason, good agreement between theory and experiment is also observed for the binding energy of p-states.

In general, further splittings of s- and p-states can occur. This is the case for defects with lower symmetry than  $T_d$  such as the thermal donors. As these have  $C_{2v}$  symmetry, s-states will split into singlets. The same occurs for p-states. In fact, a small splitting of the  $p_{\pm}$ -

states was measured for these defects, somewhat mirroring their anisotropy (Wagner and Hage, 1989).

## 2.6 Summary

Several experimental techniques which are commonly used to probe the properties of defects have been described. These consist of not only spectroscopic methods, where a precise quantum of energy is emitted or absorbed by the system, but also of thermodynamic methods like DLTS, where a transient signal between two equilibrium states is monitored.

A great deal of information can be obtained, especially if one is able to correlate different techniques. EPR gives us the anisotropy and symmetry of a gap state, providing that partial occupancy takes place. Combined with LCAO analysis, many details of a defect and its surroundings might be accessible. Optical measurements like IR absorption or PL are among the most popular type of experiments. Local mode frequencies and isotopic shifts are vital regarding the chemical constituents, dynamics and bonding arrangement of a defect. Absorption due to electronic transitions in shallow defects also take part within the IR spectral region. Here, the interpretation of the experiments on the basis of effective-mass theory has proven very effective. Again, this allows us to *draw* a considerably detailed picture of the electronic structure associated with the defect.

Despite the fact that only a description of the basic physics underlying each method has been given here, a comprehensive understanding of the properties of a defect normally involve a cooperation between several techniques, and very often the introduction of some sort of external field which will perturb the Hamiltonian. This is the case of uniaxial stress, electric or magnetic fields. These perturbations must then be explained on the basis of a theoretical model. Other variants involve the creation of anisotropy such as stress-induced alignment, which in partnership with polarised excitations sources, allow experimentalists to monitor the resulting dichroism in the output signal, and eventually its recovery kinetics.

## Chapter 3

# Oxygen, Vacancies and Hydrogen

### 3.1 Introduction

The vacancy-oxygen (VO or A-centre), is one of the most common defects produced by room-temperature electron irradiation of Si or Ge containing oxygen (Watkins and Corbett, 1961*a,b*; Whan, 1965). It is believed to form through trapping of mobile vacancies by interstitial oxygen atoms. The accepted structure is shown in Figure 3.1(a) and involves a weak Si-Si reconstructed bond between the Si atoms labelled 3 and 4. In Si, the defect has an acceptor level at  $E_c - 0.17$  eV (Watkins and Corbett, 1961*a*), while the corresponding defect in Ge has an acceptor level located at  $E_c - 0.25$  eV (Fukuoka *et al.*, 1983). The acceptor level of the defect in Si has been calculated previously by the cluster method to be  $E_c - 0.13$  eV (Resende *et al.*, 1999).

In Si,  $\text{VO}^0$  and  $\text{VO}^-$  are known to possess IR-active LVMs with  $B_1$  symmetry at  $835\text{ cm}^{-1}$  and  $885\text{ cm}^{-1}$  respectively (Watkins and Corbett, 1961*b*; Bean and Newman, 1971). However, in Ge only one band at  $620\text{ cm}^{-1}$  has been attributed to the defect (Whan, 1965), probably in the neutral state.

Previous theoretical work has successfully investigated the defect in Si, although the upward shift in the LVM for  $\text{VO}^-$  was not explained (Ewels *et al.*, 1995; Pesola *et al.*, 1999*a*). Recent experimental work has assigned a combination band  $A_1 + B_1$  around  $1400\text{ cm}^{-1}$ ,

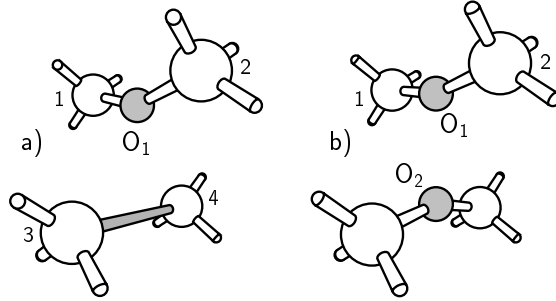


Figure 3.1: The VO (left), and VO<sub>2</sub> (right) centres. In a), the dark bond represents a reconstructed bond between Si or Ge atoms 3 and 4.

where  $A_1$  is a symmetric stretching mode at  $\sim 540 \text{ cm}^{-1}$  (Murin *et al.*, 1999; Lindström *et al.*, 1999b).

### 3.1.1 Structure and energetics

Table 3.1 gives structural details of the neutral VO<sup>0</sup> and charged VO<sup>-</sup> defects in both Si and Ge as found in cells with 64 atoms. The O atom in both charge states moves away from the  $T$ -site and bridges two second neighbour host atoms. The length of the reconstructed bond increases from 3.26 Å in the neutral defect to 3.42 Å in the negatively charged centre. This small change leads, as we shall show below, to a dramatic change in the piezospectroscopic tensor and local vibrational modes.

Table 4.2 gives the formation energies of the interstitial and neutral substitutional oxygen centres. It is clear that the formation energy of VO exceeds  $O_i$  by more than 2 eV, and thus the substitutional defect is only expected to be found at high temperatures or in the presence of a non-equilibrium concentration of vacancies produced for example by irradiation. Nevertheless, there is a strong binding between a vacancy and interstitial oxygen. The reaction energies are given in Table 3.2. Here a positive value indicates that the reaction is exothermic. This table shows there is a binding energy of about 1.6 eV between V and  $O_i$ . The formation energies for the vacancies in Si and Ge used in Table 3.2 were evaluated in 64 atom cells to be 3.61 and 2.20 eV respectively, in good agreement

Table 3.1: Bond lengths ( $\text{\AA}$ ) and angles (degrees) for VO and VO<sub>2</sub> centres in Fig. 3.1. X is Si or Ge and V denotes the centre of the vacancy

	Si			Ge		
	VO <sup>(0)</sup>	VO <sup>(-)</sup>	VO <sub>2</sub>	VO <sup>(0)</sup>	VO <sup>(-)</sup>	VO <sub>2</sub>
O <sub>1</sub> -X <sub>1</sub>	1.70	1.68	1.67	1.79	1.79	1.77
X <sub>1</sub> -X <sub>2</sub>	3.26	3.27	3.28	3.45	3.46	3.48
X <sub>3</sub> -X <sub>4</sub>	3.32	3.42	3.28	3.36	3.36	3.48
X <sub>1</sub> -O-X <sub>2</sub>	150	154	158	150	152	158
O-V	1.05	1.08	1.23	1.13	1.14	1.31

with recent plane-wave calculations (Puska *et al.*, 1998; Fazzio *et al.*, 2000).

### 3.1.2 Vibrational modes

The VO complex in Si has two fundamental local modes, whose combination frequency is estimated from a simple sum of the two fundamental  $A_1$  and  $B_1$  modes (see Table 3.3). The calculated values agree with the experiments within  $10 \text{ cm}^{-1}$  for Si and about  $20 \text{ cm}^{-1}$  for Ge. In Si, all three modes are strongly dependent on the charge state of the complex and increase in frequency for the negative charge state. In Ge only one localised mode is found.

In the negative charge state, the O atom is displaced away from the reconstructed bond consistent with the idea that the additional electron is trapped in this bond and repels the negatively polarised O atom. This movement leads to a compression of the bonds around O implying an enhancement in the LVM as shown in Table 3.3. It should be noted that within the LDA approximation, Ge is predicted to be a semimetal – the conduction band minimum at  $L$  has the same energy of the valance band maximum at  $\Gamma$ . This implies that the acceptor wavefunction in VO<sup>-</sup> is delocalised and consequently the calculated shift in the  $B_1$  mode probably underestimates the true shift (Coutinho *et al.*, 2000*b*).



Table 3.2: Reaction energies (eV) of vacancy-oxygen-hydrogen defects in Si and Ge. Negative values indicate endothermic behaviour.

Reactants	→	Products	Silicon		Germanium
			Calc. <sup>a</sup>	Calc. <sup>b</sup>	Calc. <sup>a</sup>
$V + O_i$	→	$VO$	1.57	1.4 <sup>c</sup> , 0.8 <sup>d</sup>	0.36
$O_i$	→	$VO + Si$	-2.04		-1.86
$V + O_{2i}$	→	$VO_2$	2.76	2.6 <sup>c</sup> , 1.6 <sup>d</sup>	1.04
$O_{2i}$	→	$VO_2 + Si$	-0.85		-1.18
$O_i + VO$	→	$VO_2$	1.73	1.8 <sup>c</sup> , 1.0 <sup>d</sup>	1.30
$VO + O_{2i}$	→	$VO_2 + O_i$	1.19	1.2 <sup>c</sup> , 0.8 <sup>d</sup>	0.68
$VO + H_{BC}$	→	$VOH$	2.02		
$VO + H_2$	→	$VOH + H_{BC}$	-0.09		
$VO + H_2$	→	$VOH_2$	2.41		
$VO + 2H_{BC}$	→	$VOH_2$	1.19		
$VOH + H_{BC}$	→	$VOH_2$	2.51		
$VOH + H_2$	→	$VOH_2 + H_{BC}$	0.40		

<sup>a</sup>This work.

<sup>b</sup>Pesola *et al.* (1999a)

<sup>c</sup>Using MP-2<sup>3</sup> for BZ sampling

<sup>d</sup>Using  $\Gamma$ -point for BZ sampling

Table 3.3: LVMS and their downward isotopic shifts ( $\text{cm}^{-1}$ ) for VO and VO<sub>2</sub> complexes in Si and Ge. These are compared with experimental infra-red data.

		<sup>16</sup> O		<sup>18</sup> O		<sup>16</sup> O, <sup>18</sup> O	
Mode		Obs.	Calc.	Obs.	Calc.	Obs.	Calc.
Si:VO <sup>0</sup>	$A_1 + B_1$	1370.0	1387	37.5	38		
	$B_1$	835.8	839	35.9	37		
	$A_1$	~534	548	~1	1		
Si:VO <sup>-</sup>	$A_1 + B_1$	1430.1	1404	39.1	39		
	$B_1$	885.2	872	38.2	38		
	$A_1$	~545	532	~1	1		
Si:VO <sub>2</sub>	$E$	894	893	39	41	0, 39	0, 41
	$A_1$		593		6		3
	$B_2$		557		0		0
Ge:VO <sup>0</sup>	$B_1$	620	642	31	33		
Ge:VO <sup>-</sup>	$B_1$		643		33		
Ge:VO <sub>2</sub>	$E$		690		36		0, 36
	$A_1$		363		13		6

### 3.1.3 Reorientation of VO

Two other configurations for the VO complex were investigated. Firstly, when the O atom is situated at the substitutional  $T$ -site, and secondly when it lies along one of the  $[111]$  directions with  $C_{3v}$  symmetry. In the neutral charge state, these configurations are less stable than the  $C_{2v}$ -form being 0.51 (0.10) eV and 0.26 (0.05) eV higher in Si (Ge) respectively (Coutinho *et al.*, 2000*b*). In the negative charge state these energies increase by factors of about 2 in Si and 4 in Ge. These results give an estimate of the activation barrier for the reorientation of the stable  $C_{2v}$  defect when its alignment changes from one  $[100]$  axis into another. Electron paramagnetic (EPR) studies in Si reveal that the reorientation barrier of the neutral defect is activated with an energy of 0.38 eV in good agreement with the calculated value of 0.26 eV (Watkins and Corbett, 1961*a,b*). Our calculations predict that in the negative charge state the reorientation barrier will be higher. This is in support of measurements on the recovery of the stress-induced dichroism of the  $885\text{ cm}^{-1}$  vibrational band, where a value between 0.4 and 0.5 eV was estimated (Pajot *et al.*, 1994). Stress-DLTS experiments by Andersen (2001) also came up with an activation energy of  $\sim 0.5$  eV. However, here the barrier enhancement is interpreted as the the sum of two processes. The first involves electron emission with a 0.17 eV high barrier. This is then followed by atomic reorientation mediated by a 0.38 eV barrier.

### 3.1.4 Stress-energy tensor

The calculated values of the stress tensor for the VO defect in Si also depends on the charge state (Coutinho *et al.*, 2000*b*). For the neutral defect, we find the three principal values and directions to be:  $B_1 = -9.79$  eV (along  $[100]$ : the  $C_2$  axis);  $B_2 = 5.49$  eV (along  $[011]$ ) and  $B_3 = 4.48$  eV (along  $[01\bar{1}]$ ). The  $[011]$  and  $[01\bar{1}]$  directions are parallel to the Si-O-Si and reconstructed Si-Si bonds respectively. The experimental values for  $B_1$ ,  $B_2$  and  $B_3$  are  $-11.1$ ,  $6.1$  and  $4.9$  eV respectively (Watkins and Corbett, 1961*a*).

For the negative charge state,  $B_1$ ,  $B_2$  and  $B_3$  are found to be  $-6.83$ ,  $7.81$  and  $-0.55$  eV compared with experimental values of  $-8.4$ ,  $8.8$  and  $-0.4$  eV respectively (Watkins and

Corbett, 1961a). The change of sign of  $B_3$  indicates that the defect is now compressive along the *reconstructed* bond. This arises as the additional electron occupies an anti-bonding orbital and pushes the surrounding lattice outwards. However, this argument ignores the differences in the volumes of the neutral and charged defects. In fact we found that the neutral defect led to a decrease in the volume of the supercell compared with bulk Si whereas the charged defect led to a slight increase.

## 3.2 The VO<sub>2</sub> defect

### 3.2.1 Introduction

The A-centre in Si is known to anneal out around 300°C with a simultaneous appearance of a strong IR-band at 894 cm<sup>-1</sup>. This band was originally assigned to the VO<sub>2</sub> centre (Corbett *et al.*, 1964b), formed when an interstitial oxygen atom traps a mobile VO-centre. However, there are some difficulties with this assignment. The concentration of O<sub>i</sub> appears to remain constant during the formation of the 894 cm<sup>-1</sup>-band, stress splitting measurements indicate a defect with low symmetry (Bosomworth *et al.*, 1970) and, in addition, the two O atoms must be dynamically decoupled as additional modes are not detected in isotopically mixed samples (el Fotouh and Newman, 1974; Svensson and Lindström, 1986). Previous modeling however supports the assignment to VO<sub>2</sub> with  $D_{2d}$  symmetry (Deleo *et al.*, 1985; Ewels *et al.*, 1995; Pesola *et al.*, 1999a). There the O atoms were found to be dynamically decoupled and the calculated modes were in fair agreement with the data. In addition, when the defect anneals out three high frequency O-related LVMS are observed which are consistent with the formation of VO<sub>3</sub> (Ewels *et al.*, 1995). Moreover, recent stress alignment experiments find the symmetry of the centre to be  $D_{2d}$  consistent with a VO<sub>2</sub> defect (Nielsen, 1996).

### 3.2.2 Defect structure

Our results support previous theoretical work in finding the ground state structure to possess  $D_{2d}$  symmetry. Here both oxygen atoms occupy equivalent positions by bridging atoms neighbouring the vacancy as shown in Figure 3.1(b). Structural details are given in Table 3.1, where it is noted that the Si-O bond lengths are shorter than in VO and there is a larger displacement of both oxygen atoms from the centre of the vacancy.

Table 4.2 shows that the formation energy of the defect in Si (Ge) is 0.85 eV (1.18 eV) higher than that of the staggered dimer. Thus arguments based on simple volumetric considerations implying that the aggregation of pairs of oxygen atoms lead to the creation of Si (Ge) interstitials are unlikely to be correct. The binding energy of  $O_i$  with a pre-existing VO defect is 1.73 eV.

### 3.2.3 Local vibrational modes

The LVMs of the defect are given in Table 3.3. These are in excellent agreement with the observed 894  $\text{cm}^{-1}$ -band and the O atoms, without any O-O bond, are found to be decoupled without any additional modes appearing in the mixed isotopic case. Thus the model correctly describes the observations (el Fotouh and Newman, 1974).

The  $\text{VO}_2$  centre in Ge has similar properties to the Si centre but has not yet been detected. The vibrational modes, given in Table 3.3, also consist of independent modes at 690  $\text{cm}^{-1}$  and 363  $\text{cm}^{-1}$ .

### 3.2.4 Stress-energy tensor

The stress tensor is axial with  $B_3 = -11.81$  eV and the principal direction is along the  $C_2$  axis joining the two O atoms and  $B_1 = B_2 = 5.9$  eV. It has however not yet been measured. The axial value of the  $B$ -tensor mirrors a considerably stronger compressive strain when compared with the VO defect. This stronger anisotropy must arise from the mutual Coulombic repulsion between the O atoms.

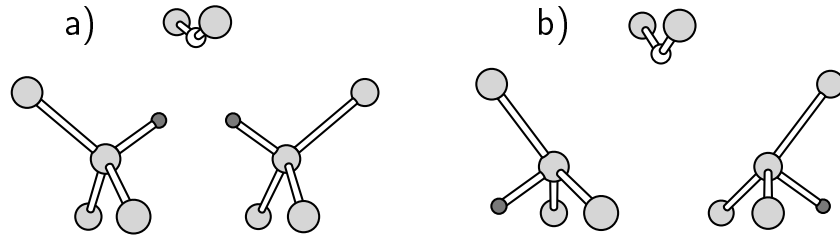


Figure 3.2: Defect structures for VOH<sub>2</sub> in Si. Silicon, oxygen and hydrogen atoms are shown as light gray, white and dark gray spheres.

### 3.3 Hydrogenation of the VO defect

#### 3.3.1 Introduction

It is known that hydrogen complexes with single vacancies by saturating the Si or Ge dangling bonds leading to VH<sub>*n*</sub> defects where *n* runs from 1 to 4 (Nielsen *et al.*, 1995, 1997; Estreicher, 1995; Coomer *et al.*, 1999*a*). In addition, recent work has demonstrated that hydrogen is easily trapped by the A-centre in Si forming VOH<sub>*n*</sub> defects where *n* is 1 or 2. The latter, shown in Figure 3.2, produces infrared absorption bands at 2151, 2126 and 943 cm<sup>-1</sup>, which were assigned to the symmetric and asymmetric stretch modes of Si-H, and the asymmetric stretch mode of the oxygen atom respectively (Markevich *et al.*, 2000). However no indication of the presence of the partially passivated A-centre (VOH) was found in this work. IR bands related to VOH<sub>2</sub> were clearly shown to be correlated with a precipitated disappearance of the A-centre at 150°C. These observations were also supported by cluster calculations (Markevich *et al.*, 2000). Here we report similar calculations done with the supercell code.

The VOH centre was suggested to account for the E3 DLTS acceptor level at  $E_c - 0.31$  eV formed in proton-implanted Fz-Si crystals (Svensson *et al.*, 1989). EPR experiments identify the centre which persists until 290°C in proton-implanted Cz-Si (Johannesen *et al.*, 2000). The hyperfine interaction with the proton located 2.5 Å from the Si atom with a dangling bond was resolved. The defect has  $C_{1h}$  symmetry below 180 K, but above 240 K the centre possesses  $C_{2v}$  symmetry arising from a thermally activated hopping of

the H atom between dangling bonds (Johannesen *et al.*, 2000; Nielsen *et al.*, 1999). The activation energy for the hopping of H and D atoms was found to be 0.18 and 0.26 eV respectively for the neutral defect. The same  $C_{2v}$  symmetry was found from a recent stress Laplace DLTS study on the E3 centre (Nielsen *et al.*, 1999). This is because the electron emission rate measured in DLTS occurred at a temperature where the H atom was able to hop between Si dangling bonds.

No vibrational modes of the defect have been reported to date. Previously, the defect had been investigated theoretically using a Hartree-Fock cluster method (Artacho and Ynduráin, 1989).

### 3.3.2 Defect structure

Relaxation of the neutral VOH defect with  $C_{1h}$  symmetry gave the Si-H and Si-O lengths to be 1.50 and 1.68 Å. The distance between the H atoms and the Si atoms with a dangling bond is 2.7 Å in good agreement with the experimental estimate of 2.5 Å. The ground state structure is shown in Figure 3.3(a). A trigonal form of the defect was also investigated (see Figure 3.3(b)), but this defect is unstable by 0.5 eV in favour of the  $C_{1h}$  structure.

Two configurations of the VOH<sub>2</sub> defect were investigated. In the first, both hydrogen atoms were placed inside the vacancy (see Figure 3.2(a)) in a manner similar with VH<sub>2</sub> (Nielsen *et al.*, 1995). In the second configuration, they lay outside, at anti-bonding sites, as in NiH<sub>2</sub> (Jones *et al.*, 1995). Both configurations have  $C_{2v}$  symmetry. We found that the second configuration was 1.25 eV higher in energy than the first where the hydrogen atoms lie inside the vacancy.

For the relaxed configuration, the Si-O bond lengths were 1.65 Å compared with 1.70 Å in the A-centre. Clearly, the saturation of the Si dangling bonds has increased the strength of the Si-O bonds. The calculations indicate that the energy released when the hydrogen molecule interacts with the the A-centre to form VOH<sub>2</sub>, is 2.4 eV. This strongly supports the view that A-centres are effective traps for mobile H<sub>2</sub> molecules.

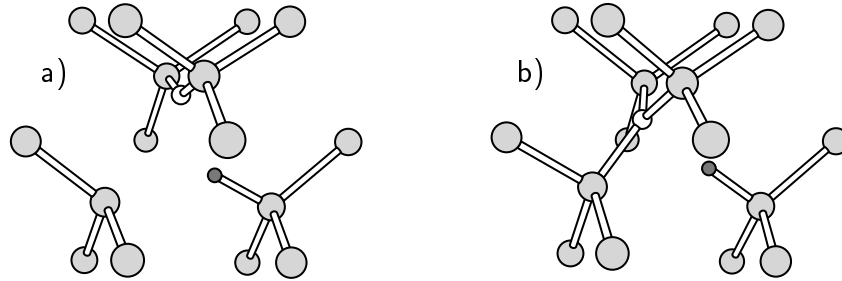


Figure 3.3: Defect structures for VOH in Si. Silicon, oxygen and hydrogen atoms are shown as light gray, white and dark gray spheres. Structures in a) and b) have  $C_{1h}$  and  $C_{3v}$  symmetry.

### 3.3.3 Local vibrational modes

The vibrational activity of VOH arises from almost decoupled oscillations of Si-O-Si and Si-H units. The  $854\text{ cm}^{-1}$ -mode is due to asymmetric stretch of Si-O-Si while hydrogen related stretch and bend modes are found at  $2042$ ,  $578$  and  $532\text{ cm}^{-1}$  respectively. These are recognized as such from the displacements of these atoms in the modes. Mixed isotopic data show these modes are almost decoupled. The  $565\text{ cm}^{-1}$ -mode is a breathing mode showing a small shift for both  $^{18}\text{O}$  and D substitution. The Si-D wag modes fall within the lattice modes, and thus, no isotopic shifts are available in Table 3.4. In the negative charge state, the  $854\text{ cm}^{-1}$ -mode increases to  $901\text{ cm}^{-1}$ . This mirrors the changes in the local mode of VO when it traps an electron.

The local vibrational modes for  $\text{VOH}_2$  along with their isotope shifts are given in Table 3.5. The calculated and observed frequencies and their isotopic shifts are in reasonable agreement (Markevich *et al.*, 2000). The two highest frequencies, at  $2248$  and  $2219\text{ cm}^{-1}$ , are the symmetric and anti-symmetric Si-H stretching modes respectively. The  $907\text{ cm}^{-1}$  frequencies correspond to the anti-symmetric stretching mode of the Si-O-Si unit,  $\sim 50\text{ cm}^{-1}$  above the analogous mode in VOH.

The calculated isotopic shifts (Table 3.5) show that the oxygen and hydrogen-related LVMS are completely decoupled: in either case, oxygen or hydrogen isotopic substitution



Table 3.4: LVMs of VOH in Si and their downward isotopic shifts ( $\text{cm}^{-1}$ ) for  $^{18}\text{O}$  and D substitution. R labels indicate resonant modes.

	$^{16}\text{O}$ , H	$^{18}\text{O}$ , H	$^{16}\text{O}$ , D	$^{18}\text{O}$ , D
	2042.4	0.0	575.3	575.4
	854.4	37.6	0.0	37.6
VOH <sup>0</sup>	578.5	0.0	R	R
	565.2	1.5	5.9	7.8
	532.5	0.4	R	R
	2045.7	0.0	576.0	576.0
	901.2	40.2	0.0	40.0
VOH <sup>-</sup>	594.3	0.0	R	R
	571.8	0.3	5.5	6.9
	554.1	1.6	R	R

Table 3.5: Calculated and measured LVM frequencies for VOH<sub>2</sub> in silicon. All frequencies and isotopic shifts (IS) are in cm<sup>-1</sup>.

	Obs. <sup>a</sup>	IS	Calc. <sup>a</sup>	IS	Symm.
V <sup>16</sup> OH <sub>2</sub>	2151.5		2248		A <sub>1</sub>
	2126.4		2219		B <sub>1</sub>
	943.5		907		B <sub>2</sub>
V <sup>16</sup> OD <sub>2</sub>	1567.4	584.1	1605	643	A <sub>1</sub>
	1549.1	577.3	1594	625	B <sub>1</sub>
	943.2	0.3	907	0	B <sub>2</sub>
V <sup>16</sup> OHD	2140.6	10.9	2224	24	A'
	1557.3	569.1	1609	610	A'
	~943.5	~ 0	907	0	A''
V <sup>18</sup> OH <sub>2</sub>			2248	0	A <sub>1</sub>
			2219	0	B <sub>1</sub>
			868	39	B <sub>2</sub>

<sup>a</sup>Markevich *et al.* (2000)

does not affect the LVMs. For example, the 907 cm<sup>-1</sup> O-related mode is unaffected by deuteration in agreement with observations.

The two highest H-related LVMs are also almost independent. The highest LVM is an A<sub>1</sub> mode and lies 29 cm<sup>-1</sup> above the anti-symmetric B<sub>1</sub> mode, in very good agreement with the observed splitting of about 25 cm<sup>-1</sup>. The observed splitting is similar to the one found (22.5 cm<sup>-1</sup>) for the VH<sub>2</sub> centre (Nielsen *et al.*, 1995).

The calculated oxygen-related mode at 907 cm<sup>-1</sup> is about 40 cm<sup>-1</sup> below the observed frequency, but it is much higher than that calculated for the A-centre at 839 cm<sup>-1</sup> (Coutinho

*et al.*, 2000*b*). This increase in frequency demonstrates that the saturation of the Si reconstructed bond leads to stronger Si-O-Si bonds and mirrors what is seen experimentally: namely the neutral A-centre has a mode at  $835 \text{ cm}^{-1}$  while the O-related mode in  $\text{VOH}_2$  lies at  $943.5 \text{ cm}^{-1}$ .

### 3.3.4 Energy levels

The  $\text{VOH}_2$  defect has the vacancy fully saturated. In fact, no electrical activity was found for this centre. However, VOH has a Si dangling bond, and an acceptor level has been claimed for this defect. We also investigated the possibility for the existence of a donor state, or even a double donor level. In the doubly positive charge state, the defect was also considered as shown in Figure 3.3(b), with the oxygen and H atoms lying in the same  $\langle 111 \rangle$  direction. Here the oxygen is three-fold coordinated, and as in  $\text{OH}_3$  molecule, easy to ionize.

The chosen standard defects (see Subsection 1.8.2) are the VO defect (for the acceptor level), and substitutional sulphur (for donor and double donor levels). These defects have levels at  $E(-/0) = E_c - 0.17 \text{ eV}$  (Watkins and Corbett, 1961*a*),  $E(0/+) = E_c - 0.30 \text{ eV}$  and  $E(+/+ +) = E_c - 0.59 \text{ eV}$  (Grimmeiss *et al.*, 1980).

The calculations indicate that the VOH defect has single acceptor and donor levels at  $E(-/0) = E_c - 0.32$  and  $E(+/0) = E_v + 0.42 \text{ eV}$ . No second donor state was found. The acceptor level is very near the experimental value at  $E(-/0) = E_c - 0.31 \text{ eV}$  (Svensson *et al.*, 1989). Recently, (Feklisova *et al.*, 2001) assigned a hole trap (H4) at  $E(+/0) = E_v + 0.28 \text{ eV}$  to VOH, and therefore we support those conclusions.

It is worthy to note that using for example carbon-interstitial as standard (with well known acceptor and donor levels at  $E(-/0) = E_c - 0.10$  and  $E(+/0) = E_v + 0.28 \text{ eV}$  respectively (Song *et al.*, 1990)), one gets acceptor and donor levels at  $E(-/0) = E_c - 0.40$  and  $E(+/0) = E_v + 0.21 \text{ eV}$  respectively for VOH — also in good agreement with the experiments.

The VOH defect is paramagnetic in the neutral charge state. A large  $^{29}\text{Si}$  hyperfine

splitting associated with a unique silicon site was identified in EPR experiments. The hyperfine tensor is almost axial and the unique principal axis deviates only  $3.9^\circ$  from the  $\langle 111 \rangle$  direction. This is a characteristic of a Si dangling bond. This dangling bond was found to account for 60% of the spin-density, of which 89% is of  $p$ -character. The hyperfine on H is nearly vanishing. Its isotropic component is 4.7 MHz, and thus much smaller than the 1420 MHz for atomic hydrogen (Johannesen *et al.*, 2000).

The Mulliken bond population for the highest occupied band was averaged using the MP-2<sup>3</sup> sampling scheme. Here we found no localization either on O or H atoms. The state is mostly localized on the Si atom. We estimated 53% of localization on this dangling bond, 86% of which is  $p$ -like. These values are in very good agreement with the EPR observations, and provide extra support for its assignment.

### 3.3.5 Hydrogen hopping

The activation energy for H hopping between the Si dangling bonds in the VOH defect can be estimated by relaxing the defect with  $C_{2v}$  symmetry. This gave a barrier,  $E_a$ , of 0.11 eV for the neutral defect but this neglects the zero-point energy of the H atom. If we assume that the contribution of this vanishes at the saddle point, where the Si-H bonds are very long at 1.80 Å, then the barrier will include the contribution of  $-\hbar\omega/2$  where  $\omega$  is the frequency of the Si-H stretch mode given in Table 3.4. The inclusion of this term effectively eliminates the barrier and implies that tunneling must become important. It is known that the barrier is apparently greater in the D case by about 0.07 eV Johannesen *et al.* (2000). For the negatively charged centre, the barrier increases to 0.18 eV.

In addition to the hopping of H, the O atom can also jump between different  $\langle 100 \rangle$  axes. An upper limit to this barrier can be found by constraining both O and H to lie on the same  $\langle 111 \rangle$  axis (see Fig. 3.3(b)). This configuration is found to be 0.42 and 0.72 eV above the ground-state for the neutral and negatively charged defects respectively. These values are greater than found for the A-centre consistent with the view that both H and a trapped electron impede the hopping of the O atom.

### 3.4 Summary

These studies reveal a number of previously unknown features. The VO and VO<sub>2</sub> defects are examined and it is found that charging the former defect leads to an increase in frequency as observed, while the latter is responsible for the 894 cm<sup>-1</sup> band in Si. Confirmation that the 894 cm<sup>-1</sup> band is due to VO<sub>2</sub> could come from an evaluation of the stress tensor which is given here.

The piezospectroscopic stress-energy tensor for VO has been evaluated for the first time. It demonstrates that the reconstructed bond in VO breaks when an electron occupies the anti-bonding state and the atoms with broken bonds move away from each other compressing the lattice. This type of calculation can be extended to many defects and links directly total energy calculations with spectroscopic data obtained from stressed crystals in which defects have been aligned.

The VOH defect is remarkable in that the H and O atoms can break their bonds leading to reorientation of the defect with activation barriers of a few tenths of an eV. The barriers are larger for the negatively charged defects. Calculated occupancy levels at  $E(-/0) = E_c - 0.32$  eV and  $E(+/0) = E_v + 0.42$  eV are in very good agreement with the measurements.

The calculated LVMs for VOH<sub>2</sub> and their isotopic shifts reproduce well the experimental values, and therefore support experimental findings that the H<sub>2</sub> molecule can interact with the A-centre.

## Chapter 4

# Early oxygen aggregates

### 4.1 Introduction

Oxygen is the most common and best studied impurity in Cz-Si (Shimura, 1994; Jones, 1996; Newman, 2000). Nevertheless, in spite of work extending over 50 years, many of its properties remain poorly understood. Even the structure of the isolated interstitial impurity — long believed to be a simple bent Si-O-Si unit similar to the arrangement in quartz — has come under recent debate. Detailed analysis of its far infra-red local vibrational modes (LVMS) has suggested that the energy barrier between the bent form with an Si-O-Si angle of around  $160^\circ$ , and the highly symmetrical configuration where the O atom lies at the bond centre (BC) is negligible.

Another dramatic suggestion is that the aggregation of two O atoms leading to an oxygen dimer does not lead to the ejection of a Si interstitial forming a  $\text{VO}_2$  centre, but is a defect with the remarkable property of migrating through the lattice at a rate faster than that of the single interstitial. This result has led to a reappraisal of both the rates at which larger oxygen clusters form, and the oxygen composition of the thermal donor defects which arise after sustained annealing of Cz-Si below about  $450^\circ\text{C}$  (Fuller *et al.*, 1954).

All these issues have tremendous implications on the overall picture of the early states of oxygen clustering, in particular on the chemical composition of thermal donor defects. We

start with the simplest and best studied oxygen defect — the interstitial oxygen ( $O_i$ ).

## 4.2 Interstitial oxygen defect

### 4.2.1 Introduction

Interstitial oxygen is known to lie near a bond centred site with equal Si-O bonds and the static defect can, in principle, assume either  $C_1$ ,  $C_{1h}$ ,  $C_2$  or  $D_{3d}$  symmetry. The different symmetries depend on the position of O with respect to the back bonded Si atoms as shown in Figure 4.1(a) and (b). In  $D_{3d}$ , the O atom lies at the bond centre. The defect possess several LVM-bands which, at low temperatures ( $T < 40$  K), lie around 30, 517, 1136 and 1750  $\text{cm}^{-1}$ . Although these bands have been intensively investigated in the last 50 years, only those at 30 and 1136  $\text{cm}^{-1}$  are clearly understood (Bosomworth *et al.*, 1970; Yamada-Kaneta *et al.*, 1990; Yamada-Kaneta, 1998)

The first arises from the motion of the O atom in a  $\{111\}$  plane normal to the Si-O-Si direction. These modes were analysed in terms of an empirical potential which led to the conclusion that the equilibrium Si-O-Si angle is  $164^\circ$  and that the energy barrier to the bond centre site is of the order of 10 meV (Bosomworth *et al.*, 1970). Further investigations have lowered the barrier to about 1 meV so that the O atom tunnels between equivalent sites leading to an effective  $D_{3d}$  symmetry (Yamada-Kaneta *et al.*, 1990). The 1136  $\text{cm}^{-1}$  ( $A_{2u}$ ) band arises from an asymmetric stretch of the two Si-O bonds, while the 517  $\text{cm}^{-1}$ -band, lying near the Raman line of bulk Si, has been assigned either to a symmetric stretch mode ( $A_{1g}$ ), or to an  $E_u$  mode with little amplitude on the O atom. The latter is required as the mode is insensitive to the oxygen mass.

The 1750  $\text{cm}^{-1}$ -band has been attributed to a combination of the 1136  $\text{cm}^{-1}$ -mode and an IR inactive band around 600  $\text{cm}^{-1}$  (Yamada-Kaneta *et al.*, 1990). This has recently been supported by the discovery of a new oxygen-related band at 648.2  $\text{cm}^{-1}$  assigned to a combination between a weak, or inactive mode, at  $\sim 618$   $\text{cm}^{-1}$  and the low energy band at 30  $\text{cm}^{-1}$  (Hallberg *et al.*, 1998).

In the case of Ge, the situation is less clear. Here, interstitial oxygen produces three absorption bands at  $\sim 1$ , 860, and 1260  $\text{cm}^{-1}$  (Gienger *et al.*, 1993; Kaiser, 1962). These can be considered as analogues of the 30, 1136, and 1750  $\text{cm}^{-1}$  bands in Si. Gienger *et al.* (1993) suggested that in Ge, the Ge-O-Ge angle is smaller than in Si and the low energy excitations are between different axial angular momentum states of a rigid buckled Ge-O-Ge rotator as shown in Figure 4.1(b). It is thus expected that the barrier for moving the O atom to the bond centre site is larger in Ge than Si.

Previous modelling studies in Si have determined both the structure of the defect and two high frequency O-related fundamentals (Snyder *et al.*, 1989; Jones *et al.*, 1992). These were located at 1104 and 554  $\text{cm}^{-1}$  and assigned to the asymmetric and symmetric modes of the buckled Si-O-Si unit respectively. The modes related to  $E_u$  fell below the Raman and were hidden by the lattice modes.

Calculations carried out in Ge, gave a symmetric stretch mode around  $\sim 400 \text{ cm}^{-1}$  (Artacho *et al.*, 1982), but no band near the Raman edge was reported. Again, the 1260  $\text{cm}^{-1}$ -band is assigned to a combination between the symmetric ( $\sim 400 \text{ cm}^{-1}$ ) and anti-symmetric (860  $\text{cm}^{-1}$ ) modes.

#### 4.2.2 Defect structure

Table 4.1 shows the relative energies and structure of the defect when confined to  $C_2$ ,  $C_1$ ,  $C_{1h}$ , and  $D_{3d}$  symmetry calculated in a 64 Si or Ge atom supercell (Coutinho *et al.*, 2000*b*). It is clear that in Si, there is very little energy difference between all the structures consistent with a tunnelling model.

In Ge, however, the bent Ge-O-Ge configuration, with an angle about  $144^\circ$ , is preferred with about 0.1 eV barrier to the  $D_{3d}$  structure. In these calculations the cell size was fixed using the calculated host lattice parameter  $a_0$  equal to 5.39 Å in Si, and 5.58 Å in Ge. However, the high concentration of defects ( $\sim 10^{21} \text{ cm}^{-3}$ ) may result in a substantial volume change and this was investigated by allowing the cell volume to relax. Figure 4.2(a) shows the variation in the total energy when the lattice parameter is varied. The energy



Table 4.1: Relative energies (in meV) and structural details of configurations for  $O_i$  in Si or Ge (denoted by X).

	Si				Ge			
	$C_2$	$C_1$	$C_{1h}$	$D_{3d}$	$C_2$	$C_1$	$C_{1h}$	$D_{3d}$
$E_{\text{rel}}$	0	9	1	13	0	12	3	106
X–O, Å	1.62	1.61	1.62	1.61	1.73	1.73	1.73	1.71
X–O–X, degrees	158	166	157	180	143	146	144	180

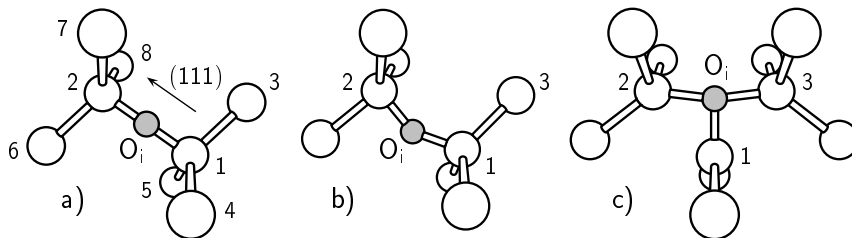


Figure 4.1:  $D_{3d}$  (a),  $C_{1h}$  (b) and Y-lid (c) configurations for interstitial oxygen.

difference between the  $C_2$  and  $D_{3d}$  structures vanishes for lattice dilations larger than 0.5% but the  $C_2$  structure is increasingly favoured under compression. The decrease in the energy of the cell when the lattice parameter is varied in this way is  $\sim 30$  meV in Si, while the bulk modulus is shifted downwards by  $\sim 2\%$  in Si and upwards by 0.5% in Ge. The effect of this concentration of oxygen is to increase the lattice parameter by 0.3% in both Si and Ge. Since the density of oxygen is  $1/64$  of that of Si, then this corresponds to a increased lattice parameter by  $\epsilon [O]/[Si]$ , where  $\epsilon$  is found to be 0.19. This agrees precisely with X-ray data giving the same value of  $\epsilon$  (Shaw, 1973; Imai *et al.*, 1987).

Table 1.3 gives the formation energy  $E_f$  of  $O_i$  in different sized cells. The calculated value lies between 1.66 and 1.81 eV in Si, somewhat larger than found by a plane wave method Pesola *et al.* (1999a). Assuming the solubility is given by  $N_{\text{BC}} \exp(-E_f/kT)$  where  $N_{\text{BC}}$  is the density of bond centre sites, we obtain an equilibrium solubility between  $6 \times 10^{16}$  and  $2 \times 10^{17} \text{ cm}^{-3}$  at  $1300^\circ\text{C}$ . This compares with a measured solubility of about  $3 \times 10^{18} \text{ cm}^{-3}$

Table 4.2: Formation energies (eV) for the single oxygen and di-oxygen centres in Si and Ge. *fccN*, *scN*, *bccN* and *ttrN* denote face-centred-cubic, simple-cubic, body-centred-cubic and tetragonal cells with  $N$  Si or Ge atoms. In the third column,  $n$  denotes the BZ sampling scheme utilised.

		MP- $n^3$	Cell	$O_i$	$O_{2i}^{\text{st}}$	$O_{2i}^{\text{sk}}$	$O_{2i}^{\text{dy}}$	VO	VO <sub>2</sub>
	Si	1	<i>sc</i> 216	1.66	2.88				
This work	Si	2	<i>sc</i> 64	1.81	3.08	3.27	4.79	3.85	3.93
	Si	2	<i>ttr</i> 96		3.04				
	Si	1	<i>fcc</i> 128	1.1	2.0	2.1			
Pesola <i>et al.</i> (1999a)	Si	2	<i>sc</i> 64					3.7	3.7
	Si	2	<i>bcc</i> 32	1.8	3.0	3.4			
This work	Ge	2	<i>sc</i> 64	1.19	1.76	2.31	3.61	3.05	2.94
	Ge	2	<i>ttr</i> 96		1.73				

which corresponds to a formation energy of interstitial oxygen of around 1.4 eV Newman and Jones (1994). These estimates have ignored the vibrational entropic contributions.

The O atom with  $C_2$  symmetry is displaced by 0.31 Å from the BC site in a  $\langle 110 \rangle$  direction leading to an Si-O-Si angle of 158°. The Si-O length is 1.62 Å, slightly longer than that in the  $D_{3d}$  configuration. Table 4.1 shows that similar geometries are obtained in the  $C_1$  and  $C_{1h}$  configurations.

### 4.2.3 Vibrational modes

The calculated LVMS for the  $C_2$  and  $D_{3d}$  structures and their isotopic shifts are shown in tables 4.3 and 4.4 (Coutinho *et al.*, 2000b). These are compared with values obtained previously and the observed modes. The frequencies for the combination bands were obtained by summing the fundamental modes.

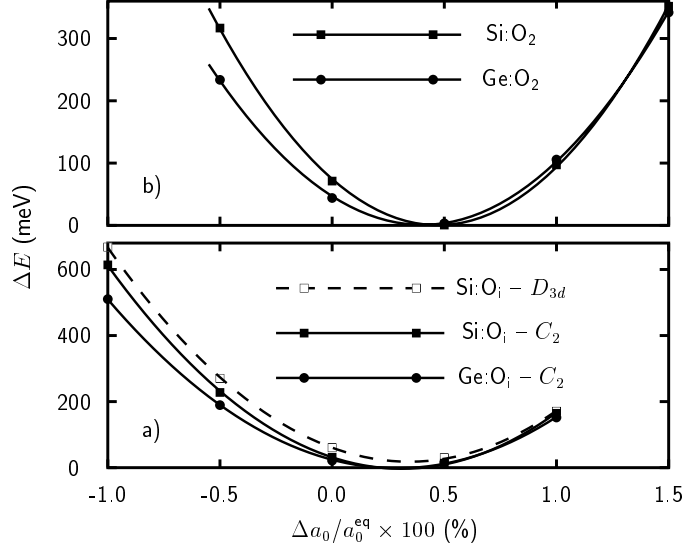


Figure 4.2: Relative Energies of a) interstitial oxygen in Si (squares) or Ge (circles), and b) staggered dimers in Si (squares) or Ge (circles) versus lattice parameter of 64 atom cell.  $a_0^{\text{eq}}$  refers to calculated Si and Ge bulk lattice constants of 5.39 Å and 5.58 Å respectively.

There are four fundamental modes for the  $C_2$  defect. Asymmetric ( $B$ ) and symmetric ( $A$ ) stretch modes lie at 1108 and 621  $\text{cm}^{-1}$  and a near degenerate pair of modes lie at 518  $\text{cm}^{-1}$ . The latter are split by 0.2  $\text{cm}^{-1}$ , and lie below the 526  $\text{cm}^{-1}$  Raman frequency given by the Musgrave-Pople potential. They are recognized by their large amplitude on the two shells of Si neighbors to oxygen and arise from the compression of the back bonds by oxygen, but the oxygen atom does not participate in their motion. This follows from the insensitivity of these two lower modes to the oxygen mass (Table 4.3). However, a shift of 1  $\text{cm}^{-1}$  occurs when one of the neighboring Si atoms is replaced by  $^{30}\text{Si}$ . In  $D_{3d}$ , the two highest modes have  $A_{2u}$  and  $A_{1g}$  symmetry. The latter is infra-red inactive and implies that its analogue in  $C_2$  at 621  $\text{cm}^{-1}$  would be only weakly IR-active. The lower pair of modes have  $E_u$  symmetry. The vibrational modes associated with these frequencies are shown in Figure 4.3(a), (b) and (c).

The calculated LVMs for both  $C_2$  and  $D_{3d}$  symmetries are similar to each other and in good agreement with the experimental data. This is especially true for the mode around

Table 4.3: Calculated LVMS,  $\text{cm}^{-1}$ , and their downward isotopic shifts for different configurations for  $\text{O}_i$  in Si. Results of previous calculations are given along with observed modes. Two-phonon modes are estimated by simple summation of asymmetric and symmetric fundamentals.

	Mode	$^{28}\text{Si } ^{16}\text{O } ^{28}\text{Si}$	$^{30}\text{Si } ^{16}\text{O } ^{28}\text{Si}$	$^{28}\text{Si } ^{18}\text{O } ^{28}\text{Si}$	$^{30}\text{Si } ^{18}\text{O } ^{28}\text{Si}$
	$A + B$	1729	14	53	66
Calc. <sup>a</sup>	$B$	1108	4	50	54
$C_2$	$A$	621	10	3	12
	$A, B$	518	2	0	2
	$A_{1g} + A_{2u}$	1803	14	54	68
Calc. <sup>a</sup>	$A_{2u}$	1184	4	55	58
$D_{3d}$	$A_{1g}$	619	10	0	10
	$E_u$	519	1	0	1
Calc. <sup>b</sup>	$B$	1098		50	
	$A$	630		2	
Calc. <sup>c</sup>	$A$	1104		53	
	$B$	554		1	
		1748.6	12.2	52.6	—
		1136.4	3.7	51.4	55.2
Observed <sup>d</sup>		$\sim 618$	9.5	$\sim 0$	—
		517.8	—	0.0	—

<sup>a</sup>This work.

<sup>b</sup>Pesola *et al.* (1999a)

<sup>c</sup>Jones *et al.* (1992)

<sup>d</sup>Pajot *et al.* (1995), except the  $618 \text{ cm}^{-1}$  band from Hallberg *et al.* (1998).

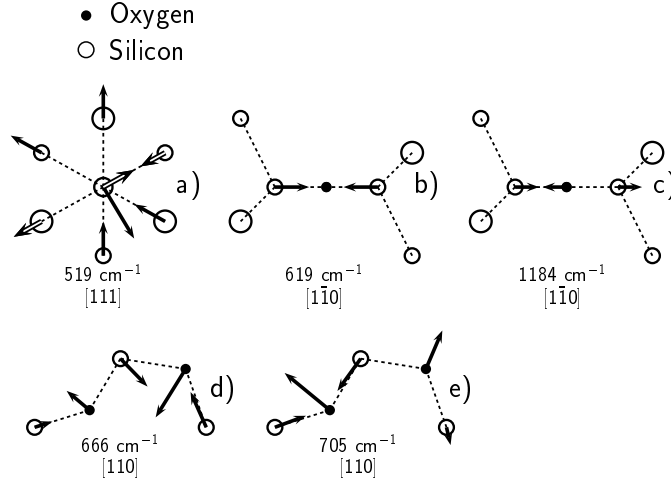


Figure 4.3: Normal coordinates of the vibrational modes for  $O_i$  in Si [a), b) and c)], and for the dimer modes at 666 and 705  $\text{cm}^{-1}$  [d) and e)]. The two components of the  $E_u$  mode in a) are distinguished by filled and outlined arrows. The 666  $\text{cm}^{-1}$  mode in d) has a small induced dipole moment arising from the movements of the oxygen atoms which are out of phase with each other. The normal to the projected plane is given in each case.

621  $\text{cm}^{-1}$  which has been detected as a partner in two combination bands (Yamada-Kaneta *et al.*, 1990; Hallberg *et al.*, 1998). Thus, there is nothing in the observed or calculated modes which allows the symmetry of the defect to be unambiguously identified. As described above, the  $D_{3d}$  model has been singled out as it can explain the fine structure of the 30  $\text{cm}^{-1}$ -band. However, this band is too low in frequency to be accurately modeled using *ab-initio* methods. Nevertheless, the effect of pressure on the high frequency modes allows us to discriminate between these models.

Figure 4.4 shows the LVMS as a function of pressure. This dependence can be expressed through either the isotropic piezospectroscopic tensor element  $A_1$ , given in Table 4.5, and appropriate for a trigonal defect, or through the Gruneisen parameter,  $\gamma = -\partial \ln \omega / \partial \ln V$ . We find that, for the  $D_{3d}$  structure,  $A_1$  is positive for all LVMS — in agreement with experiment at low pressures (Hrostowski and Kaiser, 1957; Hallberg *et al.*, 1998; Kaiser, 1962; Artacho *et al.*, 1982). The large difference between the values of  $A_1$  for the 1136  $\text{cm}^{-1}$ -band found by uniaxial and hydrostatic stress experiments is in part due to the non-linear

Table 4.4: Calculated LVMs,  $\text{cm}^{-1}$ , and their downward isotopic shifts for  $\text{O}_i$  in Ge. Results of previous calculations are given along with observed modes. Two-phonon modes are estimated by simple summation of asymmetric and symmetric fundamentals.

	Mode	$^{70}\text{Ge } ^{16}\text{O } ^{70}\text{Ge}$	$^{74}\text{Ge } ^{16}\text{O } ^{74}\text{Ge}$	$^{70}\text{Ge } ^{18}\text{O } ^{70}\text{Ge}$	$^{74}\text{Ge } ^{18}\text{O } ^{74}\text{Ge}$
	$A + B$	1248	8	55	63
Calc. <sup>a</sup>	$B$	847	2	44	46
$C_2$	$A$	401	6	11	17
	$A + B$	1293	8		
Calc. <sup>b</sup>	$B$	878	3		
	$A$	416	6		
		1274.0	8.3	—	—
Observed <sup>c</sup>		862.91	1.01	43.28	45.45
		412.1 <sup>d</sup>	7.3 <sup>d</sup>	—	—

<sup>a</sup>This work.

<sup>b</sup>Artacho *et al.* (1982)

<sup>c</sup>Mayur *et al.* (1994)

<sup>d</sup>This frequency was calculated by assuming the existence of a combination mode  $A + B$  at  $1274.0 \text{ cm}^{-1}$ .

fit employed in the latter (McCluskey, 1999).

However,  $A_1$  is negative for the  $C_2$  structure as the buckling increases with pressure and leads to slightly dilated Si-O bonds. Experimentally, the asymmetric stretch mode decreases with increasing hydrostatic pressures beyond about 1 GPa (McCluskey and Haller, 1997). This can be explained as a change from a  $D_{3d}$  configuration at low pressures to the buckled form for pressures  $\sim 1$  GPa.

Table 4.5: Calculated values for the isotropic piezospectroscopic tensor element  $A_1$  ( $\text{cm}^{-1}\text{GPa}^{-1}$ ) for local modes of  $\text{O}_i$  along with the experimental data. Grüneisen parameters for each mode are between parentheses.

Mode	Si: $C_2$		Si: $D_{3d}$		Obs.	Ge: $C_2$	
$A_{2u} + A_{1g}/A + B$	-0.78	(-0.13)	2.28	(0.37)		3.68	(0.50)
$A_{2u}/B$	-2.11	(-0.55)	1.81	(0.45)	0.77 <sup>a</sup> , 0.2 <sup>b</sup>	1.64	(0.44)
$A_{1g}/A$	1.33	(0.62)	0.47	(0.22)		0.82	(0.50)
$E_u/A, B$	0.86	(0.47)	0.84	(0.47)	$\sim 1.1$ <sup>b</sup>		

<sup>a</sup>McCluskey and Haller (1997)

<sup>b</sup>Bosomworth *et al.* (1970)

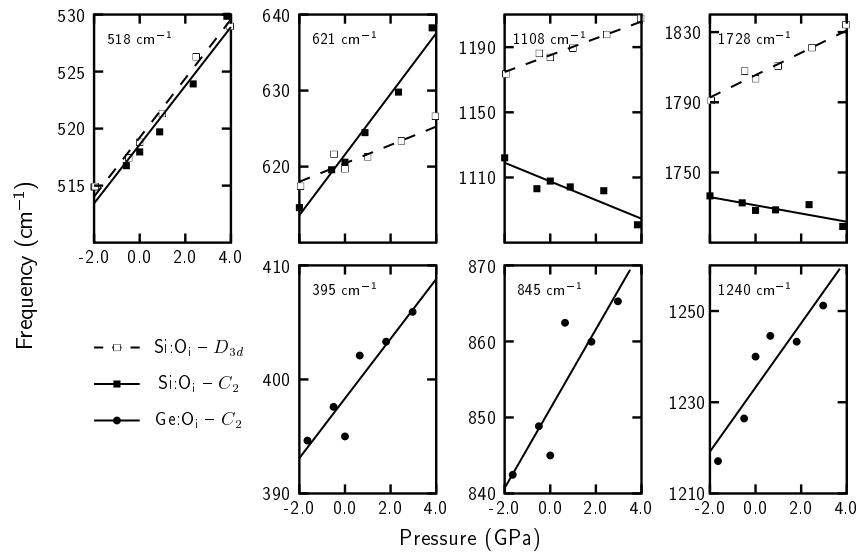


Figure 4.4: Effect of pressure on LVMs of interstitial oxygen in Si (upper row) and Ge (lower row).

#### 4.2.4 Stress-energy tensor

The stress tensor for  $O_i$  in Si has been calculated as described above. We find the principal values for the  $D_{3d}$  structure are  $B_3 = -2B_2 = -2B_1 = -10.71$  eV with the principal direction of  $B_3$  along the  $C_3$  axis. The negative value of  $B_3$  indicates that the defect is compressive along the Si-O-Si bond as expected. These are in fair agreement with the experimental results of  $B_3 = -2B_2 = -2B_1 = -15.2$  eV (Watkins, 1996).

#### 4.2.5 Diffusion of interstitial oxygen

Detailed experimental studies have established that the diffusion process is governed by the hopping of a single oxygen atom between bond centered sites with an activation energy of 2.53 eV (Mikkelsen, 1986). However, theoretical studies have enjoyed mixed success in reproducing this fundamental property. Early cluster calculation by Jones *et al.* (1991) gave 2.8 eV but this value has not been found by supercell calculations where an underestimation has been consistently reported (Ramamoorthy and Pantelides, 1996; Needels *et al.*, 1991a; Oshiyama and Saito, 1990; Capaz *et al.*, 1999). The diffusion barrier is the energy difference between the buckled stable configuration and the saddle point which has long been considered to be the Y-lid configuration where the oxygen atom lies mid-way between two second neighboring Si atoms. This energy difference has been found between 1.8 and 2.2 eV and it has been suggested that this discrepancy arises from the neglect of the kinetic energy of the O atom (Needels *et al.*, 1991b), and subsequently to the neglect of a simultaneous motion of Si neighbors (Ramamoorthy and Pantelides, 1996). However, reaction rate theory includes both of these effects and assumes only that the system once reaching the saddle point executes a diffusive step (Flynn, 1975).

The activation energy for an oxygen atom hopping between neighboring bond centers in Si has been measured by stress-induced dichroism (Corbett *et al.*, 1964a) to be 2.56 eV and the same barrier was found for the long range diffusion of oxygen as measured by secondary-ion mass spectrometry (Mikkelsen, 1986). In Ge, the diffusion energy is 2.08 eV (Corbett *et al.*, 1964a). The similarities in the oxygen diffusion energies in Ge and Si suggests an



identical diffusion mechanism.

The saddle point for hopping between bond centers has been found to be the Y-lid configuration with  $C_{2v}$  symmetry and shown in Figure 4.1(c) (Jones *et al.*, 1991). In this configuration, both the O atom and the Si<sub>1</sub> neighbor are three-fold coordinated.

The energy of the Y-lid was calculated by relaxing 32, 64 and 128 atom cells with the symmetry maintained to be  $C_{2v}$ . The lattice parameter was again taken to be given by the calculated bulk value. We found that in Si this energy is 2.1 to 2.2 eV higher than the  $C_2$  structure when using cells with these sizes (Coutinho *et al.*, 2000b). Allowing the volume of the cell to relax lowered the energy of the Y-lid configuration by 10 meV. This has negligible effect on the diffusion energy, and gives us confidence regarding the size of the supercell. If the O atom is slightly perturbed, then, upon relaxation without any constraint, it returns to the stable  $C_2$  site. Thus the calculated diffusion energy is about 2.2 eV compared with an experimental value of 2.5 eV. This may be compared with previous estimates of 2.8 (Newman and Jones, 1994), 1.8 (Needels *et al.*, 1991a), 2.2 (Ramamoorthy and Pantelides, 1996), and 2.0 eV (Oshiyama and Saito, 1990).

In a similar way, the energy of the Y-lid structure in Ge is found to be 1.70 eV above its ground state. In both materials, the diffusion barrier is underestimated by about 0.3 eV. This may result from inadequacies in local density functional theory or slow convergence in cell size or basis.

An intriguing problem is the fact that pre-exponential factor  $D_0$  has been measured as  $0.13 \text{ cm}^2\text{s}^{-1}$ , corresponding to an attempt frequency of  $3.5 \times 10^{14} \text{ s}^{-1}$ . This also suggests a hopping enhancement due to about  $4k_B$  of motional entropy (Newman and Jones, 1994). Although this is not clear, several reasons could explain this effect (Stoneham, 1989): (i) vibrational entropy, (ii) configurational entropy, (iii) thermal expansion.

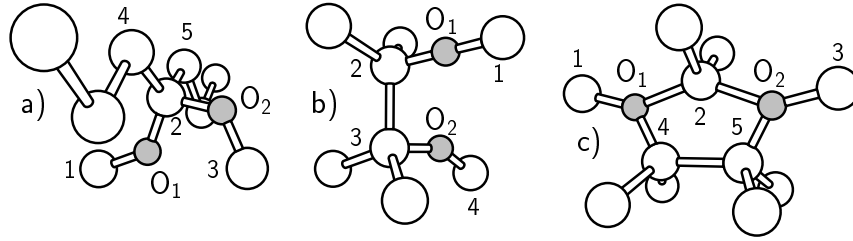


Figure 4.5: Schematic structure of oxygen dimers. a) Staggered ( $O_{2i}^{\text{st}}$ ), b) Skewed ( $O_{2i}^{\text{sk}}$ ), and c) Double Y-lid ( $O_{2i}^{\text{dy}}$ ). Oxygen atoms are grey.

## 4.3 Interstitial oxygen dimer

### 4.3.1 Introduction

One puzzling feature that characterizes the TDD growth process, is its low  $\sim 1.8$  eV activation energy (Wagner *et al.*, 1992; Newman and Jones, 1994). If the conversion is due to oxygen aggregation, then this implies that some oxygen species can diffuse at a much faster rate than isolated oxygen atoms. Moreover, careful studies of the loss of the intensity in the  $1136\text{ cm}^{-1}$ -band with prolonged anneals below  $500^\circ\text{C}$ , strongly suggest a fast diffusing dimer. This makes the dimer species a key entity in kinetic studies of oxygen aggregation in Si (Åberg *et al.*, 1998; McQuaid *et al.*, 1999).

The first suggestion for a fast diffusing oxygen-related species was made by Gösele and Tan (1982) and attributed to an  $\text{O}_2$  molecule. However, later calculations indicated that the molecule was less stable than an oxygen dimer where both oxygen atoms are tilted along the  $\langle 110 \rangle$  direction with respect to each other (see Figure 4.5(a)) (Needels *et al.*, 1991a). Here the oxygen atoms were found to be bound by 1 eV.

Subsequent infra-red absorption studies have identified the LVMS of an oxygen dimer. These lie at  $1060$ ,  $1012$ ,  $690$  and  $556\text{ cm}^{-1}$ . The intensities of these modes vary with the square of the  $\text{O}_i$  concentration (Öberg *et al.*, 1998) and in the  $^{16}\text{O}$ - $^{18}\text{O}$  mixed isotopic case, unique modes are detected demonstrating the presence of two oxygen atoms that are dynamically coupled. The two oxygen atoms,  $\text{O}_1$  and  $\text{O}_2$ , must be inequivalent as

these unique modes are only found in one of the  $^{16}\text{O}_1\text{-}^{18}\text{O}_2$  combinations. This unusual behavior is reflected in the intensities of the modes (Öberg *et al.*, 1998).

Further investigations suggested that a second dimer, called the skewed (see Figure 4.5(b)) because a Si-Si bond separates the Si-O-Si units which lie in different  $\{110\}$  planes, is energetically competitive with the staggered dimer (Murin *et al.*, 1998; Öberg *et al.*, 1998). Previously, we found, using the cluster method, that the skewed dimer possesses LVMS closer to the experimental values than those of the staggered dimer. The converse was, however, found by Pesola *et al.* (1999b). To address this problem, the LVMS have been re-evaluated using the supercell method.

In Ge, interstitial oxygen dimers have only been identified recently (Litvinov *et al.*, 2001). Here only the high-frequency bands were observed. Their location at 780.5 and 818.0  $\text{cm}^{-1}$  is very near to what we would expect after scaling bands in Si by  $\nu_{\text{Ge}}/\nu_{\text{Si}} = 862/1136$ , where  $\nu_{\text{Ge}}$  and  $\nu_{\text{Si}}$  are the asymmetric stretch mode frequencies of  $\text{O}_i$  in Si and Ge respectively. Annealing kinetics studies estimate that O atoms are bound by  $\sim 0.4$  eV — about 0.1 eV stronger than the dimer in Si (Litvinov *et al.*, 2001). Despite that only few theoretical studies have been performed (Chadi, 1996), it is reasonable to expect that oxygen clustering in Ge will start with the dimer formation as in Si.

### 4.3.2 Structure of the oxygen dimer

The structures investigated, i.e., the staggered, skewed, and double-Y-lid dimers shown in Figure 4.5, were calculated mainly in 64 atom supercells, although some calculations used 96 or 216 atom supercells (Coutinho *et al.*, 2000b).

Table 4.2 gives the formation energy of these dimers. Cells with 64 and 96 silicon atoms give values within 0.04 eV, suggesting that they are sufficiently large. The formation energy calculated in the largest 216 cell is not necessarily more accurate than found in the 64 or 96 atom cells as only one  $\mathbf{k}$ -point ( $\Gamma$ ) was used to sample the band structure in this case. Figure 4.2(b) demonstrated that the effect of allowing the cell volume to relax is negligible consistent with the view that 64 atom cells are sufficiently large.

Table 4.6: Binding energies (eV) for interstitial di-oxygen centers in Si and Ge. *fccN*, *scN*, *bccN* and *ttrN* denote face-centered-cubic, simple-cubic, body-centered-cubic and tetragonal cells with  $N$  Si or Ge atoms. In the third column,  $n$  denotes the BZ sampling scheme utilized.

	Crystal	MP- $n^3$	Cell	$O_2^{st}$	$O_2^{sk}$	$O_2^{dy}$
	Si	1	<i>sc216</i>	0.44		
This work	Si	2	<i>sc64</i>	0.54	0.35	-1.17
	Si	2	<i>ttr96</i>	0.58		
	Si	1	<i>fcc128</i>	0.2	0.1	
Pesola <i>et al.</i> (1999 <i>a</i> )	Si	2	<i>bcc32</i>	0.6	0.2	
	Si		<i>bcc32</i>	0.4		
Chadi (1996)	Si		<i>fcc16 – sc64</i>	1.0		
This work	Ge	2	<i>sc64</i>	0.62	0.07	-1.23
	Ge	2	<i>ttr96</i>	0.65		
	Ge		<i>bcc32</i>			0.7

The binding energies for the dimers obtained from the formation energies in Table 4.2 are given in Table 4.6 where they are compared with previous studies.

The binding energy of the oxygen atoms in the staggered dimer is found to be about 0.5 and 0.6 eV in Si and Ge respectively. An experimental estimate in Si is about 0.3 eV Murin *et al.* (1998). The skewed configuration is less favored by about 0.2 eV in Si, but is only marginally bound in Ge. Table 4.7 gives structural details of the dimers.

The symmetric double-Y-lid dimer is found to be energetically disfavored by about 1.2 eV relative to two isolated oxygen atoms in both Si and Ge. This is in contrast with previous work on this structure in Ge which found this structure to be bound with an energy of 0.7 eV. Chadi (1996) Nevertheless, the 1.2 eV required to form the symmetric double Y-lid suggests that the dimer can diffuse with at least this activation energy which is lower than the barrier for single oxygen diffusion. This is a subject we shall investigate in the next

Table 4.7: Bond lengths ( $\text{\AA}$ ) and angles (degrees) for oxygen dimers in Si and Ge (represented by X), shown in Figure 4.5.

Crystal Dimer	Si			Ge		
	staggered	skewed	double-Y-lid	staggered	skewed	double-Y-lid
$O_1-X_1$	1.66	1.61	1.75	1.77	1.73	1.86
$O_1-X_2$	1.64	1.62	2.11	1.74	1.74	2.19
$O_1-X_4$			1.75			1.85
$O_2-X_2$	1.63		2.11	1.74		2.19
$O_2-X_3$	1.67	1.63	1.75	1.77	1.75	1.86
$O_2-X_4$		1.63			1.74	
$O_2-X_5$			1.75			1.85
$X_2-X_3$		2.29			2.39	
$X_4-X_5$			2.37			2.57
$X_1-O_1-X_2$	130	166	146	125	147	147
$X_1-O_1-X_4$			131			128
$X_2-O_2-X_3$	127		146	124		147
$X_3-O_2-X_4$		148	131		138	128

section.

We also investigated the O<sub>2</sub> molecule lying at a *T*-site. This oxygen dimer is not stable: being 6.03 eV higher in energy than the staggered dimer. We discuss the stability relative to VO<sub>2</sub> in Subsection 4.5.2 and now turn to the vibrational modes of the dimers.

### 4.3.3 Local vibrational modes

The LVMs for the staggered and skewed dimers were found by evaluating the energy second derivatives between the O atoms and their Si neighbors. They are given in Tables 4.8 and 4.9 along with the observed modes. There are five modes of the dimer but only four have been detected. The calculated modes are within 40 cm<sup>-1</sup> of the observed ones. However, of great importance is their isotopic shifts. For the staggered dimer, when the oxygen atom labeled O<sub>2</sub> in Figure 4.5 is replaced by its <sup>18</sup>O isotope, the 1017 cm<sup>-1</sup>-mode drops only by 2 cm<sup>-1</sup> but the 984 cm<sup>-1</sup> mode drops by 41 cm<sup>-1</sup>. These are in excellent agreement with observed drops of ~0 and 42 cm<sup>-1</sup> respectively. However, when O<sub>1</sub> in Fig. 4.5 is replaced by <sup>18</sup>O, the 1017 cm<sup>-1</sup>-mode is expected to drop by about 40 cm<sup>-1</sup> bringing it close to the 984 cm<sup>-1</sup>-mode. The two modes then are in resonance and become coupled leading to shifts of 28 and 17 cm<sup>-1</sup> in each mode. These are to be compared with observed shifts of 39 and 8 cm<sup>-1</sup>. Clearly the degree of coupling is overestimated but is less than that found by the cluster method previously.

The calculated shifts in the 705, and 666 cm<sup>-1</sup>-modes are 14 and 10 cm<sup>-1</sup> respectively and 0 cm<sup>-1</sup> for the 543 cm<sup>-1</sup>-mode. These shifts are in reasonable agreement with shifts in the observed bands at 690 and 556 cm<sup>-1</sup>.

In the skewed configuration, the modes are essentially decoupled and the frequencies too high. They resemble those of two isolated oxygen interstitials. This suggests that the observed modes arise from the staggered dimer.

Only one of the modes around 690 cm<sup>-1</sup> has been detected probably because the transition moment in the other is very small. The displacements of the atoms are shown schematically in Figure 4.3(d) and (e). Locating point charges at each O and neighboring Si atoms, leads

Table 4.8: Calculated LVMs ( $\text{cm}^{-1}$ ) and their downward isotopic shifts for staggered and skewed dimers ( $\text{O}_{2i}^{\text{st}}$  and  $\text{O}_{2i}^{\text{sk}}$  respectively) in Si, along with the experimental observations.

	$^{16}\text{O}_1, ^{16}\text{O}_2$		$^{16}\text{O}_1, ^{18}\text{O}_2$		$^{18}\text{O}_1, ^{16}\text{O}_2$		$^{18}\text{O}_1, ^{18}\text{O}_2$	
	Calc. <sup>a</sup>	Calc. <sup>b</sup>	Calc. <sup>a</sup>	Calc. <sup>b</sup>	Calc. <sup>a</sup>	Calc. <sup>b</sup>	Calc. <sup>a</sup>	Calc. <sup>b</sup>
$\text{Si:O}_{2i}^{\text{st}}$	1017	1033	2	1	28	40	46	46
	984	984	41	42	17	6	42	42
	705	697	4	4	9	6	14	11
	666	661	9	6	3	3	10	8
	543	566	0	0	0	0	0	0
$\text{Si:O}_{2i}^{\text{sk}}$	1166	1104	0	1	52	52	53	50
	1094	1091	48	48	1	-3	49	50
	636	643	3	2	0	1	3	3
	624	627	1	1	0	2	1	3
	552	558	0	0	0	0	0	0
Observed <sup>c</sup>	1060		$\sim 0$		39		48	
	1012		42		8		43	
	690		4		$\sim 4$		10	
	—		—		—		—	
	556		$\sim 0$		$\sim 0$		0	

<sup>a</sup>This work

<sup>b</sup>Pesola *et al.* (1999b)

<sup>c</sup>Öberg *et al.* (1998)

to an induced dipole moment which is three times greater in the  $705\text{ cm}^{-1}$ -mode than in the  $666\text{ cm}^{-1}$ -mode. This probably occurs as the displacements of the oxygen atoms are in phase in the  $705\text{ cm}^{-1}$ -mode and out of phase in the  $666\text{ cm}^{-1}$ -mode. We therefore assign the observed  $690\text{ cm}^{-1}$ -band to the higher frequency.

In Ge, the dimer modes are very similar to those in Si and the two high frequency stretch modes are reduced by a factor of 0.77 from the asymmetric stretch mode of  $\text{O}_i$  while the lower pair are reduced by a factor of about 0.73. A band at  $780\text{ cm}^{-1}$  detected in annealed electron irradiated oxygen-doped Ge has been attributed to the dimer (Whan, 1965). In a recent work by Litvinov *et al.* (2001), this band was correlated with a second band at  $818\text{ cm}^{-1}$ . Both  $818$  and  $780\text{ cm}^{-1}$ -bands shift downwards by  $42$  and  $40\text{ cm}^{-1}$  in  $^{18}\text{O}$  doped samples, and its intensity has a square dependence on the concentration of oxygen. The position of the dimer bands and its isotopic shifts agrees with the calculated modes at  $784$  and  $749\text{ cm}^{-1}$  which shift  $41$  and  $38\text{ cm}^{-1}$  with  $^{18}\text{O}$  doping. However, further work is necessary to observe the other modes of the dimer. Further support for the assignment of this band to an oxygen aggregate comes from recent findings of a strong enhancement in thermal-donor concentrations consequent upon annealing irradiated material containing the  $780\text{ cm}^{-1}$  band (Klechko *et al.*, 1999).

The dimer modes in Si are observed to display an anomalous temperature dependence. Normally, the fundamental frequency of a defect increases with decreasing temperature resulting from a strengthened bonds arising from the lattice contraction. However, the bands at  $1012$  and  $1060\text{ cm}^{-1}$  shift downwards with temperature (Öberg *et al.*, 1998). To investigate this anomaly we decreased the lattice parameter in the 64 atom supercell containing the staggered dimer. The effect was to decrease further the Si-O-Si angles, i.e., increase their buckling, and reduce the asymmetric stretch modes as shown in Figure 4.6. Thus, if the effect of lowering the temperature is simply to contract the lattice and impose a pressure on the dimer, then the upper two modes would decrease in frequency while the lower modes would increase. The same situation holds for the dimer in Ge — in contrast with what was found for  $\text{O}_i$  in this material. However, the band at  $780\text{ cm}^{-1}$ , attributed to dimers in Ge does not appear to shift anomalously with temperature. There clearly are



Table 4.9: Calculated LVMs ( $\text{cm}^{-1}$ ) and their downward isotopic shifts for staggered and skewed dimers ( $\text{O}_{2i}^{\text{st}}$  and  $\text{O}_{2i}^{\text{sk}}$  respectively) in Ge, along with the experimental observations.

	$^{16}\text{O}_1, ^{16}\text{O}_2$	$^{16}\text{O}_1, ^{18}\text{O}_2$	$^{18}\text{O}_1, ^{16}\text{O}_2$	$^{18}\text{O}_1, ^{18}\text{O}_2$
Ge: $\text{O}_{2i}^{\text{st}}$	784	8	17	41
	749	32	23	38
	517	8	11	22
	466	13	9	18
	849	4	1	44
Ge: $\text{O}_{2i}^{\text{sk}}$	843	40	42	44
	389	1	10	11
	366	7	0	7
	818			42
Observed <sup>a</sup>	780			40

<sup>a</sup>Litvinov *et al.* (2001)

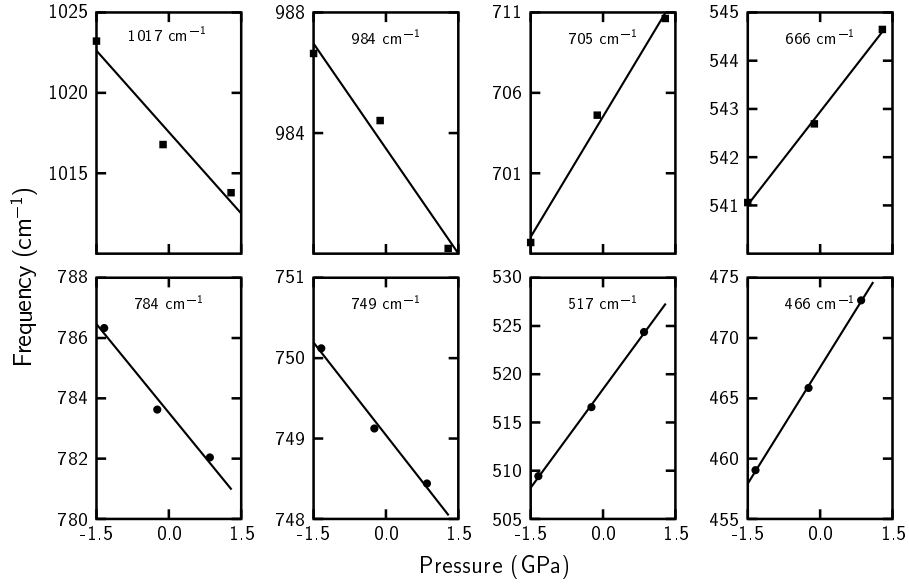


Figure 4.6: Effect of pressure on LVMs of the staggered dimer in Si (upper row), and Ge (lower row).

two opposing effects at work: the first is an increased buckling which leads to a downward shift in frequency, and the second is the compression of the X-O bond lengths which lead to a frequency increase. In Si, the first effect is dominant, but the second dominates in Ge.

#### 4.3.4 Stress-energy tensor

The staggered dimer has  $C_{1h}$  symmetry, and hence its stress-energy tensor will have one principal direction (say  $B_2$ ) normal to a  $(10\bar{1})$  plane where the defect lies. The other two principal directions,  $B_1$  and  $B_3$ , lie on that plane, but will be rotated by an angle  $\theta$  away from the crystallographic directions  $[010]$  and  $[101]$  respectively. This can be seen in Figure 4.7. The calculations give principal values of  $-9.29$ ,  $6.17$  and  $3.12$  eV for  $B_1$ ,  $B_2$  and  $B_3$  respectively, with  $\theta_B = 31^\circ$ . This defect can be then understood as a perturbed  $O_i$ . Figure 4.7 indicates that the compressive component  $B_1$  is  $\sim 4^\circ$  away from the  $[1\bar{1}1]$  trigonal direction. The staggered dimer is formed by two unequivalent O-atoms. One of them ( $O_1$  in Fig. 4.5(a)), is near the bond-center site, and dominates the B-tensor

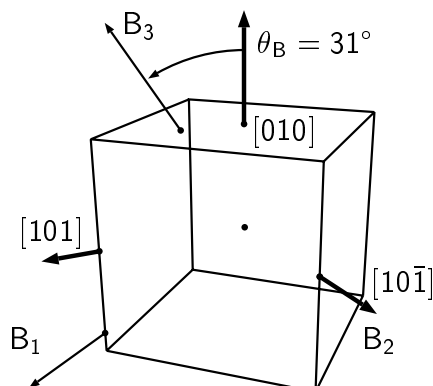


Figure 4.7: Principal directions of the stress-energy tensor for the oxygen dimer. The defect lies on the  $(10\bar{1})$  plane.

properties. The other O-atom is strongly buckled and acts as a perturbation.

### 4.3.5 Diffusion of the dimer

The activation energy for movement of the dimer was investigated using three different diffusion paths (Coutinho *et al.*, 2000*b*): (i) a correlated jump of both oxygen atoms from the staggered configuration through the asymmetric double-Y-lid structure of Figure 4.8(i), (ii) a partial dissociation involving an asymmetric Y-lid as in Figure 4.8(ii), and a transition between the staggered and skewed dimers as proposed by Pesola *et al.* (1999*b*) and shown in Figure 4.8(iii). The migration energies were determined by relaxing the cell with constraints on the lengths of the O-X bonds as described earlier and shown in the figure.

Path (i) leads to a migration energy of 1.4 eV, (ii) leads to a similar barrier of 1.6 eV, although the complete diffusion event requires the oxygen atom at the left side to make a similar jump to reform the dimer. However, symmetry considerations require this second step to be equivalent to the first. Path (iii) is activated by a barrier of 2.2 eV, and resembles the diffusion of isolated interstitial oxygen.

One can rationalize these results by noting that in (i) both three-fold coordinated Si

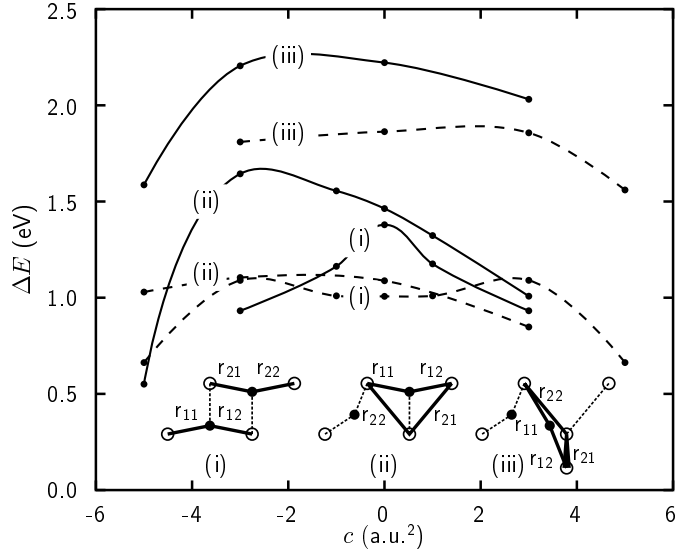


Figure 4.8: Energies, eV, along three diffusion paths discussed in the text for oxygen dimers in Si (solid lines) and Ge (dashed lines).  $\Delta E$  is the energy relative to a stable dimer. The  $x$ -axis refers to the value of the constrained variables  $c = \mathbf{r}_{11}^2 - \mathbf{r}_{12}^2 = \mathbf{r}_{21}^2 - \mathbf{r}_{22}^2$ .

atoms labeled 1 in Figure 4.1(c) are now bonded to the other O-atoms. Similarly, in (ii) the tensile strain along [110] in the Y-lid is off-set by the presence of the second O atom. The effect of both these processes is to transport the dimer along [110] but both lead to a staggered dimer which tilts in the opposite direction. Before long range migration can occur, the dimer must reorientate and point in the opposite direction. The energy barrier for this is found to be below 0.38 eV in Si and 0.65 eV in Ge.

Thus we conclude that the diffusion path probably occurs by the staggered dimer migrating along its [110] axis with a correlated jump of both oxygen atoms.

For Ge, Figure 4.8 shows that the energy surface around the saddle-point is flatter than in Si. This is because the smaller Ge-O-Ge angle means that the oxygen atom is *closer* to the saddle point and consequently the *length* of the trajectory is shorter.

In summary, the calculations demonstrate that oxygen dimers diffuse in Si and Ge with barriers about 0.8 and 0.6 eV respectively below the calculated barriers for  $O_i$ .

## 4.4 Formation of staggered aggregates

### 4.4.1 Introduction

The idea of a fast-diffusing O-dimer opens up several questions. Such dimers would be expected to be trapped mainly by single oxygen interstitials and form trimers. If the trimer were stable and immobile, then their concentration would gradually build up and larger oxygen aggregates would not easily form. The trimer bottleneck can be removed in two ways. Either the binding energy of the trimer is negligible so that they dissociate into dimers and  $O_i$ , and further growth is based on dimer association, or the trimer is stable but mobile and  $O_{4i}$  defects are rapidly formed. The first hypothesis requires that the trimer is unstable but previous calculations suggest that this is not the case (Chadi, 1996; Pesola *et al.*, 1999a). However, the other proposal leaves unresolved the rate at which larger aggregates can form. One suggestion is that these aggregates along with thermal donors are all mobile (Murin and Markevich, 1996).

### 4.4.2 Chain energetics

We find that oxygen atoms cluster preferentially along [110] directions with decreasing Si-O-Si angles with increasing chain length (see Fig. 4.9(a)). As all O-atoms bridge first nearest Si neighbours, we shall refer as  $O_n$ -1NN to these chains.

Formation energies relative to quartz, vary from 1.81 eV, for the single interstitial, to about 1.0 eV per oxygen atom for the longer chains. Despite the clear *driving force* to form these 1NN aggregates, saturation is attained for chains with more than 6-7 oxygen atoms.

### 4.4.3 Migration of oxygen-chains

Consider, now the migration of such chains. As the chain moves through the lattice along the [110] valley in which it lies, a single or group of O atoms moves to the symmetric Y-lid

Table 4.10: Formation energies per oxygen atom of  $O_n$ -1NN chains in Si, with  $n$  between 1 and 9. All values are relative to the energy of each O-atom in a  $\alpha$ -SiO<sub>2</sub> environment. Binding energies  $E_b = [E_f(n-1) + E_f(1)] - E_f(n)$  are also included. All values in eV.

	1	2	3	4	5	6	7	8	9
$E_f(n)/n$	1.81	1.54	1.33	1.23	1.18	1.13	1.10	1.06	1.05
$E_b$		0.54	0.91	0.88	0.84	0.91	0.90	1.04	0.80

configuration as illustrated in Fig. 4.9(b). An upper limit for the diffusion barrier is found by relaxation with a constraint that forces atoms to approach this configuration. In Si, this energy drops from 2.2 eV for the single oxygen species to 1.4, 1.3 and 1.2 eV for  $O_n$ ,  $n = 2, 3$  and 4 Coutinho *et al.* (2000a). For Ge, there are similar reductions. Despite the underestimation of the migration barrier for  $O_i$ , a rapid diffusion of oxygen chains is to be expected with a barrier around 1.2 eV and 1.0 eV in Si and Ge respectively. The marked reduction of the migration barriers comes from two effects. Firstly, the decreasing Si-O-Si angles which bring the staggered form closer to the Y-lid form, and secondly, the absence of Si dangling bonds at the saddle point for all clusters *except*  $O_1$ . This is clearly shown in Figure 4.9(b). With isolated oxygen concentrations of  $\sim 10^{18}$  cm<sup>-3</sup> and maximum donor concentrations of  $\sim 10^{16}$  cm<sup>-3</sup> the diffusing chain will most likely encounter a single oxygen interstitial, either lying in the same or a nearby  $\langle 110 \rangle$  valley. In the latter case, there will have to be single oxygen jump before a longer chain is formed. It is this rapid chain diffusion which enables long chains to grow rapidly Lee *et al.* (2001), but raises the question as to whether the increasing stress leads to a kick-out of a Si interstitial. This issue is dealt in Section 4.5.

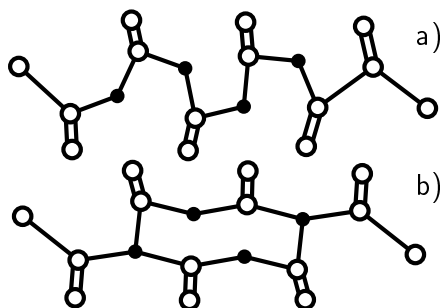


Figure 4.9: The staggered  $O_4$  chain aligned along  $[110]$ . b) structure close to saddle-point for migration of the chain. This structure could be displaced to *fall* either into a) or the structure in a) displaced along  $[110]$ . White and black spheres are Si and O atoms respectively.

## 4.5 Ejection of self-interstitials

### 4.5.1 introduction

Another important question concerns the critical size of an oxygen aggregate which is thermodynamically unstable against vacancy-oxygen ( $VO_n$ ) formation. As oxygen clusters grow, there is an increase in strain energy which will be relieved at a critical size by the ejection of a self-interstitial ( $I$ ). We will show here that  $VO_n$  formation becomes exothermic only for  $n = 4$  but the activation barrier probably prevents this happening around  $450^\circ\text{C}$ .

### 4.5.2 Energetics of $VO_n$ against $O_n$ defects

Simple geometric considerations suggest that oxygen clusters beyond a certain size are unstable and release a Si self-interstitial forming a  $VO_n$  defect. We investigate these reactions in detail and conclude that they can spontaneously occur only for  $n$  equal or greater than 4 (Coutinho *et al.*, 2000a). The energy of the reaction  $O_{ni} \rightarrow VO_n$  is found by moving the abstracted Si atom to a reservoir of bulk Si. Thus for neutral defects,  $\Delta E_f$  is simply  $E_f(VO_n) + \mu - E_f(O_{ni})$  where  $\mu$  is the energy of a Si atom in bulk material.

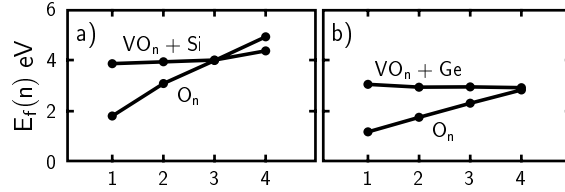


Figure 4.10: Formation energies of  $VO_n$  defects and staggered  $O_n$  chains, a) Si, b) Ge. Formation of each  $VO_n$  defect imply the creation of a bulk Si/Ge atom.

Figure 4.10 (right) gives these formation energies found from supercells of 128 atoms and demonstrates that the threshold for the reaction is around  $n = 4$ .

The activation barrier to the process must include the formation energy of the self-interstitial near the vacancy aggregate. It is not clear what this barrier is but when the interstitial is far from  $VO_n$ , then the energy difference includes the formation energy of the interstitial which is found to be around 3.3 eV in both Si and Ge respectively. It is unlikely that this barrier can be reduced significantly by the formation of an  $IO_n$  defect as such complexes are not thought to be stable above 200°C (Abdlullin *et al.*, 1998; Hermansson *et al.*, 1999). As the formation rates of thermal donors are activated with much smaller barriers, we conclude that  $VO_4$  defects will not be formed around the temperatures where thermal double donors are stable.

## 4.6 Summary

In summary, the calculations find that interstitial oxygen in Si, at normal pressures, is likely to tunnel between bent Si-O-Si configurations with effective  $D_{3d}$  symmetry. In this configuration, there are two localized fundamentals at 1184 ( $A_{2u}$ ), 619 ( $A_{1g}$ ) and an  $E_u$  resonance at 519  $\text{cm}^{-1}$ . The frequency of the modes increase with pressure. However, for a critical pressure, the energy difference between the  $C_2$  and  $D_{3d}$  configurations increases, and tunneling no longer occurs. In this case the O atom could still rotate around the  $\langle 111 \rangle$  axis with the asymmetric stretch mode decreasing with increasing pressure.

In germanium, the  $D_{3d}$  structure has energy 0.1 eV higher than the others which are all



degenerate (see Table 4.1). The Ge-O-Ge angle is  $143^\circ$  and the oxygen atom lies  $0.55 \text{ \AA}$  away from the BC site with the Ge-O bond length at  $1.73 \text{ \AA}$ . The energy barrier to the  $D_{3d}$  case suggests that tunneling cannot occur, but the oxygen atom may rotate around the  $\langle 111 \rangle$  axis. Table 4.4 gives the calculated and experimental LVMS. Two fundamental LVMS lie at  $847$  and  $401 \text{ cm}^{-1}$  and represent asymmetric and symmetric stretch modes of the Ge-O-Ge buckled unit. In general, these results are in agreement with previous investigations (Martinez *et al.*, 1987; Jones *et al.*, 1992; Artacho *et al.*, 1982; Pesola *et al.*, 1999a; Laßmann *et al.*, 1999). In contrast with Si, these frequencies do not drop with increasing pressure and no mode around the Raman frequency occurs. The difference in behavior is probably due to the very different bond angle in the two materials.

The oxygen dimer, in both Si and Ge, is stable in the staggered form with modes calculated to be in good agreement with experiment. It is surprising that the two stretch modes of the dimer, in which the oxygen atoms share a common Si neighbor, are *almost* dynamically decoupled. The anomalous temperature dependence for the modes in Si has been linked to an increased buckling occurring during the contraction of the crystal when cooled. This seems to be a signature of a buckled oxygen bridge in Si and its observation has implications for other defects. The dimer is found to be stable against the formation of  $\text{O}_2$  molecules. The barrier to diffusion of the dimer is about  $0.8 \text{ eV}$  and  $0.6 \text{ eV}$  lower in Si and Ge respectively than that of  $\text{O}_i$ . The diffusion path involves a concerted movement of the pair of atoms along a path which eliminates dangling bonds at the saddle point.

In conclusion, we have shown that oxygen atoms lying in chains diffuse quickly and form extended chains lying along  $[110]$ . The most stable small chains involve O atoms linking first neighbouring Si atoms (O-1NN). The chains are less stable than an  $\text{SiO}_2$  precipitate but form through their rapid kinetics.

A comparison between the formation energies of  $\text{O}_{ni}$  and  $\text{VO}_n$  defects, leads us to conclude that the ejection of self-interstitials from  $\text{O}_{ni}$  aggregates does not occur for  $n \leq 4$ . The reaction is exothermic for  $\text{O}_{4i}$  defects in Si but the activation barrier prevents this happening during TDD growth.

## Chapter 5

# Thermal double donors

### 5.1 Introduction

Thermal double donors (TDD) are formed by annealing oxygen rich Si or Ge at temperatures between 300 and 500°C. They comprise a family of at least 16 double donors which form sequentially and are distinguished by their increasingly shallow levels (Jones, 1996). In spite of extensive studies, they remain a mystery. There are in essence two current models. The first, much favoured in theoretical studies (Snyder and Corbett, 1985; Jones, 1990; Chadi, 1996; Pesola *et al.*, 1999*b*; Ramamoorthy and Pantelides, 1999), suggests that they consist of an increasing number of O atoms surrounding a core containing at least one over-coordinated oxygen defect. The second considers them to be a silicon self-interstitial-oxygen complex  $I_nO_m$  (Newman, 1985; Deák *et al.*, 1992). It must be admitted that the bulk of experimental evidence favours the latter. Three examples reveal the difficulties of the oxygen-only model. Firstly, the activation energy for the transformation of TDD( $N$ ) into TDD( $N + 1$ ) varies from 1.2 eV for  $N = 1$ , to 1.7 eV for larger  $N$  in Si. This leads to an anomalously fast transformation when compared with the 2.5 eV migration barrier for oxygen (Newman, 2000). Secondly, EPR and ENDOR studies on the NL8 family, assigned to TDD( $N$ )<sup>+</sup>, reveal two shells of O atoms, apparently bridging neighbouring Si atoms, possessing almost infinitesimally small spin-densities (Michel *et al.*, 1989; Spaeth, 1996).

The isotropic  $^{17}\text{O}$  hyperfine interaction is less than 0.5 MHz in NL8 and much less than 3 MHz found on oxygen in  $\text{VO}^-$ , in spite of the fact that oxygen in  $\text{VO}^-$  is located in a nodal plane of the spin-density (van Kemp *et al.*, 1989*b*). How, one wonders, can the source for the donor activity be oxygen when there is so little spin-density associated with it? Thirdly, the oxygen-only model requires an increasing number of oxygen related local vibrational modes (LVMS) to be associated with the later donors, but only at most two such modes have been assigned to any donor (Lindström and Hallberg, 1994, 1996). Thus, any credible model must address all these well established observations.

## 5.2 The self-interstitial model

It is well known that carbon suppresses TDD formation in Si (Newman and Willis, 1965; Bean and Newman, 1972). Although this suppression process is not well understood, both the oxygen-only and self-interstitial-oxygen models give an explanation. In the oxygen-only model it is argued that diffusing oxygen is trapped by substitutional carbon. The resulting  $\text{C}_s\text{O}_n$  defects have been reported in the literature to appear during TDD annealing conditions (Bean and Newman, 1972; Yamada-Kaneta *et al.*, 1996). However, according to the self-interstitial-oxygen model,  $I$  defects are trapped by  $\text{C}_s$  (Ourmazd *et al.*, 1984), and via Watkins replacement mechanism, produce carbon-interstitial defects ( $\text{C}_i$ ). The later are necessary to explain the appearance of the photoluminescent  $T$ -line at 0.935 eV, associated with the  $\text{C}_i\text{C}_s\text{H}$  complex, which appears after prolonged 450°C heat treatments of oxygen-rich Si (Safonov *et al.*, 1996).

The most successful TDD model containing self-interstitials was proposed by Deák *et al.* (1992). As shown in Figure 5.1(c), labelled as form- $\text{U}_1$  (*unstable one*), its active core consists of two oxygen atoms bonded to a self-interstitial located nearby the  $T$ -site. The popularity of this model relies fundamentally on the fact that it possesses  $C_{2v}$  symmetry, and no O atom is present in the  $C_2$  symmetry axis along  $[001]$ , consistent with the ENDOR data. Its donor activity arises from the overlap of anti-bonding crystal states with the silicon-interstitial.

Table 5.1: Binding energies  $E_b$ , and relative energies  $E_r^q$  in charge state  $q$  (eV) for all structures considered (see Figs. 5.1 and 5.2). Binding energies represent the total energy difference between an  $IO_2$  defect and a staggered dimer plus a split-interstitial infinitely separated.

Structure	$E_b$	$E_r^-$	$E_r^0$	$E_r^+$
A	0.39	0.57	0.35	0.00
B	0.75	0.03	0.00	0.07
C	0.63	0.00	0.13	0.34
U <sub>1</sub>	-4.78		5.53	
U <sub>2</sub>	-0.19		0.94	
U <sub>3</sub>	-0.43		1.18	
U <sub>4</sub>	-0.38		1.13	

In agreement with Deák *et al.* (1992), we found the symmetric  $IO_2$  model to be a good candidate as a shallow double-donor. It possesses a fully occupied Kohn-Sham band *touching* the conduction-band. However, we abandoned this model as it is not stable. Its total energy is 5.53 eV higher than that the form-B of the  $IO_2$  defect depicted in Figure 5.2(c). In fact the symmetric U<sub>1</sub> model is 4.78 eV more costly than a split-interstitial far away from a staggered  $O_{2i}$  defect (see Table 5.1). Figure 5.1 shows other  $IO_2$  complexes with  $C_{2v}$  symmetry, but as shown in Table 5.1, all were found to be unstable.

Within the  $IO_n$  defects investigated, none of them possess binding energies compatible with the thermal stability of the TDD defects (see Table 5.1). Observations seem to support these results, as no  $IO_n$  complex has been observed above  $\sim 200^\circ\text{C}$  (Hermansson *et al.*, 1999). Early infra-red experiments by Whan (1966*a,b*) revealed three IR absorption bands located at about 936, 944 and 956  $\text{cm}^{-1}$ , later assigned to arise from a  $I_2O_i$  (936  $\text{cm}^{-1}$ ) and  $IO_i$  (944 and 956  $\text{cm}^{-1}$ ) complexes (Whan and Vook, 1967; Hermansson *et al.*, 1999).

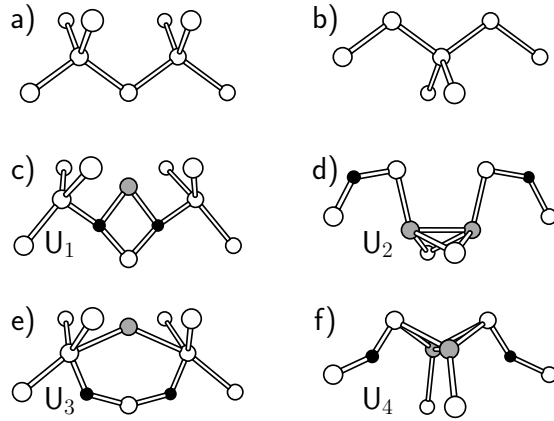


Figure 5.1: Unstable and metastable structure candidates for an  $IO_2$  complex. Oxygen and Si atoms are black and white respectively. a) and c) are pure Si regions where the defects lie. In c) and e), the self-interstitial is near the  $T$ -site — grey atom. In d) and f) two Si atoms share a Si site (grey atom), making a *split-interstitial*.

Recent IR absorption measurements in electron irradiated Cz-Si revealed an  $IO_2$  complex (Lindström *et al.*, 2001). Here, a clear correlation was found between the disappearance of bands from the oxygen dimer with the appearance of two bands at 1037 and 922  $\text{cm}^{-1}$ . Again, this defect was found to break slightly above 200°C, and therefore also incompatible with the thermal stability of TDD defects.

Figure 5.2 shows the three favourite structures for the  $IO_2$  defect. From Table 5.1 one can notice that all structures have similar formation energies, and each one is favoured for a particular charge state. Neutral forms B and C are separated by an energy barrier as small as 0.3 eV. This suggests that the defect could be bi-stable, or even tri-stable, depending on the position of the Fermi level. Bi-stability has been observed in a variety of defects like the EL2 in GaAs (Martin and Markram-Ebeid, 1992), thermal double donors (Makarenko *et al.*, 1985),  $C_sC_i$  pair (Song *et al.*, 1988), or the D1 shallow donor (Markevich *et al.*, 1994). This problem was reviewed by Watkins (1990), and is normally associated with large structural relaxations after capture or emission of carriers.

LVMs were calculated for forms B and C. These are compared with the observations

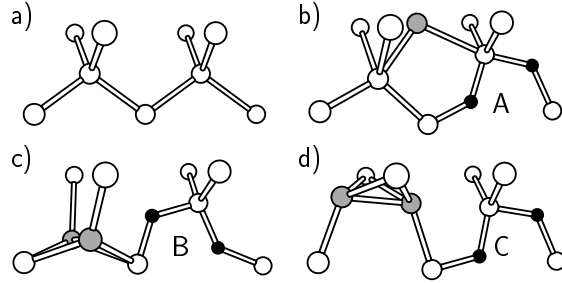


Figure 5.2: Lowest energy structures for an  $IO_2$  complex. Oxygen and Si atoms are black and white respectively. a) is pure Si region where the defects lie. In b) the self-interstitial is near the  $T$ -site (grey atom). In c) and d) two Si atoms share a Si site (grey atom), making a *split-interstitial*. Structures b), c) and d) are the most stable in the positive, neutral and negative charge states.

in Table 5.2. Clearly, form-B is the one that better reproduces the measured absolute frequencies. Moreover, the absence of mixed modes is also accounted by form-B. The mixed-mode calculations indicate that despite their spatial proximity, both O atoms are almost dynamically decoupled, and splittings should be hidden under the  $\sim 6 \text{ cm}^{-1}$ -wide  $^{16}\text{O}$ - $^{16}\text{O}$  and  $^{18}\text{O}$ - $^{18}\text{O}$  absorption bands.

DLTS experiments assigned an acceptor level at  $E_c - 0.11 \text{ eV}$  to the  $IO_2$  defect (Lindström *et al.*, 2001). However, no IR-bands were yet observed for the defect in the negative charge state. This could be an indication of bi-stability, and further work needs to be done. Nevertheless, the small binding energies of  $IO_n$  complexes and the high energy cost to eject a self-interstitial from a small  $O_n$  defect, clearly favour the oxygen-only model.

### 5.3 Infinite oxygen-chains

As oxygen atoms were found to cluster preferentially long the  $[110]$  direction, several *periodic infinite* chains were investigated (see Fig. 5.3).

The most stable is the O-2NN model, shown in a), where oxygen atoms are bonded to second neighbour Si atoms in two parallel chains along  $[110]$  (Jones *et al.*, 2001). An ionic

Table 5.2: Calculated and measured LVM frequencies ( $\text{cm}^{-1}$ ) for the  $\text{IO}_2$  defect. First two columns are absolute frequencies, and columns three onwards are downwards isotopic shifts ( $\text{cm}^{-1}$ ). ND stand for not detected.

	$^{16}\text{O}-^{16}\text{O}$	$^{16}\text{O}-^{18}\text{O}$	$^{18}\text{O}-^{16}\text{O}$	$^{18}\text{O}-^{18}\text{O}$
	1020.7	44.9	0.3	45.8
	958.9	0.7	40.9	41.0
form-B	703.0	1.4	12.9	14.9
	659.1	7.1	1.4	7.9
	545.0	0.1	0.1	0.2
	929.6	2.4	23.5	41.1
	898.7	37.1	17.3	39.2
form-C	720.5	14.6	2.9	18.9
	667.4	2.8	12.3	13.7
	541.6	0.1	0.1	0.2
Obs. <sup>a</sup>	1037	ND	ND	46
	922	ND	ND	39

<sup>a</sup>Lindström *et al.* (2001)

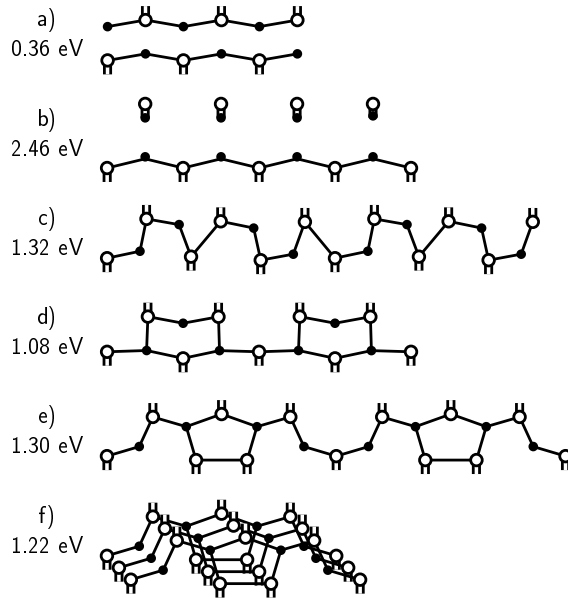


Figure 5.3: Periodic infinite sub-oxide chains. a) O-2NN, b)  $\text{VO}_2$ , c)  $\text{O}_2$ -1NN, d) Ring, e) D-Ylid, f) parallel D-Ylid. Formation energies per O-atom are shown on the left hand side of each structure.

bonding character was found across and along the chains. We can then think that each oxygen atom is divalent, and each Si atom tetravalent. This is shown in Figure 5.4, where a plot of the total charge density reveals electrons much more localised on the anions (oxygen atoms), than on cations (Si atoms), i.e. the chain is a sub-oxide. The formation energy per oxygen atom (0.36 eV) is very small when compared with the 1.81 eV to form an isolated  $\text{O}_i$  defect. Nevertheless, this chain is metastable with respect to quartz, and it must break after sufficient annealing time.

It is tempting to identify the O-2NN chains with the donors. Although they have the same  $C_{2v}$  symmetry for odd  $n$ , this cannot be correct. The band structures for bulk Si and the infinite O-2NN chain, in the same supercell, are shown in Figs. 5.5(a) and 5.5(b) respectively. These demonstrate that the chain is insulating with a highest occupied band close to that of bulk Si. They also reveal that the six degenerate lowest empty bands associated with the  $\langle 100 \rangle$  valleys in bulk Si are split in  $\text{O}_\infty$ -2NN, with the lowest pushed downwards by  $\sim 0.2$  eV from their centre of mass by the  $[001]$  stress arising from oxygen. The ionic



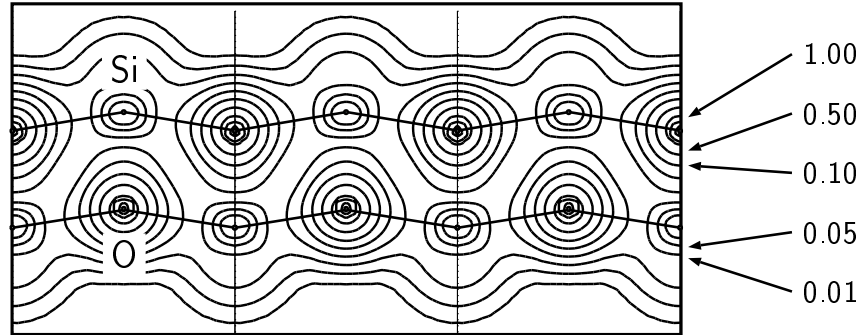


Figure 5.4: Contour plot of the charge density along the infinite O-2NN chain (see Fig. 5.3(a)). Contour levels (a.u.<sup>-3</sup>) are shown on the right hand side of the plot.

character of the sub-oxide is supported by Fig. 5.9(a), which shows that the wavefunction of the empty stress induced gap level is localised on the Si cations and avoids the oxygen anions as expected for conduction band states in ionic materials.

## 5.4 The O-2NN model

### 5.4.1 Energetics and bi-stability

Finite  $O_n$ -2NN chains are terminated by O-atoms bridging Si nearest neighbours as shown in Fig. 5.6(b). Consequently, a topological defect involving an over-coordinated O-atom or an under-coordinated Si-atom, must be present at the interface between the two types of oxygen atoms. While short  $O_n$ -1NN chains — where all O atoms bridge first Si neighbours (see Fig. 4.9(a)) — are more stable than short  $O_n$ -2NN chains, the reverse is true for long ones and the cross-over occurs around  $N = 6$  and  $N = 8$  oxygen atoms. This cross-over is shown in Figure 5.8, where the stabilising factor in  $O_n$ -2NN chains is its low formation energy core. Note that each core oxygen atom only costs 0.36 eV.

It is known that the first three TDD members in Si (the first four in Ge), are bi-stable. They have an inactive species labelled  $X(N)$  and a double donor  $TDD(N)$  form. As shown in Figure 5.7, for  $0 \leq N \leq 2$  the neutral X-form is more stable than the active form. As the

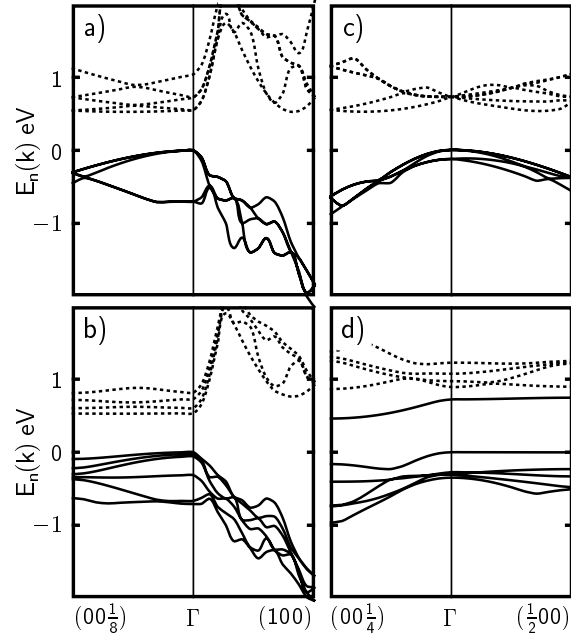


Figure 5.5: Band structure for a) defect-free Si in 48 Si atom supercell, and b) the same supercell containing the infinite O-2NN chain from Fig 5.6(a). Solid and dashed lines represent filled and empty states. Band gap of 0.54 eV in a) is consequence of density functional theory. Reciprocal-space points are in units of  $2\pi/a_0$ , where  $a_0$  is the Si lattice constant. Note that degenerate valleys along (001) and (100) in a) are split in b). c) and d) show band structures for 112 Si atom defect-free supercell and same cell containing O<sub>9</sub>-2NN as in Fig. 5.6(b). Note that d) exhibits double donor behaviour.

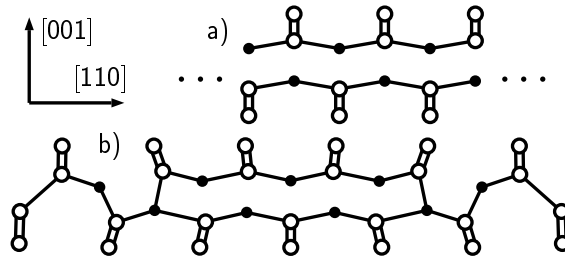


Figure 5.6: Most stable structures for a) *infinite chain* (referred as O<sub>∞</sub>-2NN), and b) the TDD model O<sub>9</sub>-2NN finite chain. O and Si are shown as black and white circles respectively.

donor form can be populated after illuminating the sample with above-band-gap light, non-equilibrium  $(0/+)$  deep levels occur at 0.75, 0.48 and 0.29 eV below the conduction-band. In the TDD-form, the donor levels are shallow, and the system forms a negative- $U$ , i.e., it is energetically favourable to form  $\text{TDD}^{++} + \text{TDD}^0$  than  $2 \times \text{TDD}^+$ , and the positive defect is not thermodynamically stable. Hence the equilibrium  $(0/+ +)$  occupancy level lies mid-way between the  $(0/+)$  and  $(+ / + +)$  levels. As the aggregation process goes on, the  $\text{TDD}(N)$ -form is stabilised, and a cross-over occurs for  $N = 3$ . Now the defects have a ground state with double donor character. Further details about bi-stability of defects can be found in a review by Watkins (1990).

In the TDD-form, the first ionisation energy is  $69.2 \text{ meV} \geq E(0/+) \geq 49.9 \text{ meV}$  for  $1 \leq N \leq 11$ , and second ionisation energy  $156.3 \text{ meV} \geq E(+ / + +) \geq 116.0 \text{ meV}$  for  $1 \leq N \leq 9$ . These are very close to He-like effective-mass binding energies, where  $E(0/+) = 55.8 \text{ meV}$  and  $E(+ / + +) = 126.8 \text{ meV}$ . For  $N = 0$ , the donor form is metastable by about 0.7 eV and of difficult preparation. Hence its donor levels were not measured yet (Murin, 2001).

As first suggested by Chadi (1996), the short 1NN chains (see Figure 4.9(a)) are good candidates for the X-form of the thermal donor defects. Here we support this assignment. As we shall see in Subsection 5.4.2, finite  $\text{O}_n$ -2NN chains are shallow double donors, and after looking again to Figure 5.8, we conclude that the first non bi-stable  $\text{O}_n$ -2NN defects have about 6 or 7 oxygen atoms.

### 5.4.2 The quantum dot analogy

Whereas the infinite chain is insulating, the finite chain is not. The highest occupied state in  $\text{O}_9$ -2NN shown in Fig 5.5(d) now borders the conduction band. It might then be expected that the wavefunction of this shallow double donor level must be localised on the over-coordinated oxygen atoms but, as Fig. 5.9(b) shows, this is not the case. The donor state is the *same* stress-induced gap state found for the infinite O-2NN chain. We understand this as follows. The interface region leads to an energy level lying *above* the strain

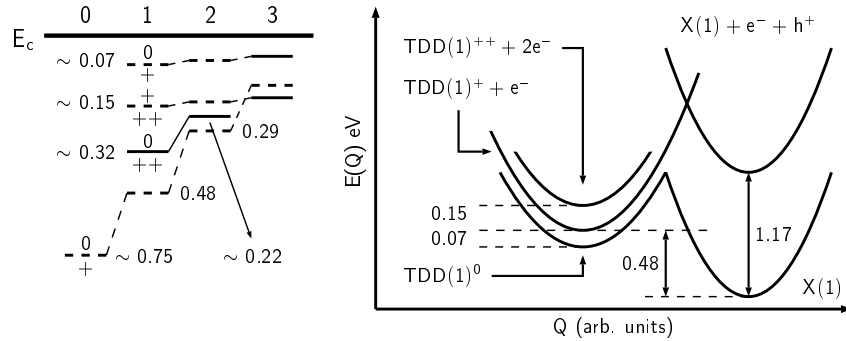


Figure 5.7: Configuration coordinate diagram for the thermal double donors in Si after Makarenko *et al.* (1985). All energies are given in eV. Solid and dashed levels represent equilibrium and non-equilibrium occupancy levels respectively.

induced gap level due to the O-2NN core. Consequently, electrons drop into the stress induced gap state with minimal overlap with oxygen. This explains the ENDOR/EPR results for a lack of spin-density on oxygen even though oxygen is the source of the donor activity (Jones *et al.*, 2001).

A simple analogy can be made with an externally doped GaAs quantum dot embedded in AlAs. An electron arising from a Si donor in the AlAs matrix drops into the lower lying unoccupied dot state arising from the band off-set between GaAs and AlAs. A magnetic resonance experiment then reveals a spin-density on Ga but not on Si. It might be then erroneously concluded that the source of the donor activity is a Ga interstitial. The important point is that these experiments do not reveal the primary cause of donor activity in the thermal donors. The strain induced level is also consistent with the effect of uniaxial-stress on electronic IR absorption (Stavola *et al.*, 1985).

### 5.4.3 Interaction with hydrogen

Thermal donors can interact with atomic hydrogen leading to the formation of TDD-H defects (Johnson and Hahn, 1986; Weber and Bohne, 1996). The kinetics of dissociation of TDD-H was studied in DLTS, where an activation barrier of 1.9 eV and 1.1 eV was derived for TDD(1) and later donors respectively (Weber and Bohne, 1996; Pearton *et al.*, 1992).

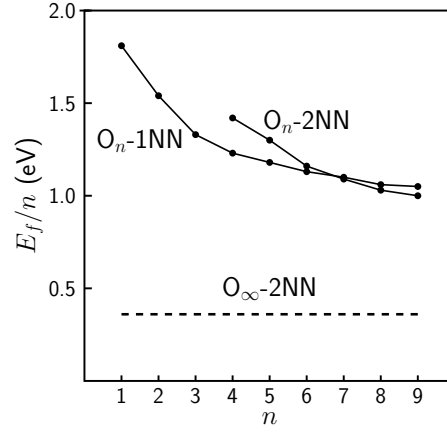


Figure 5.8: Formation energy per oxygen atom (eV), for  $O_n$ -1NN and  $O_n$ -2NN finite chains. The *driving force* to form  $O_n$ -2NN structures is its low energy core (see  $E_f/n$  for  $O_\infty$ -2NN).

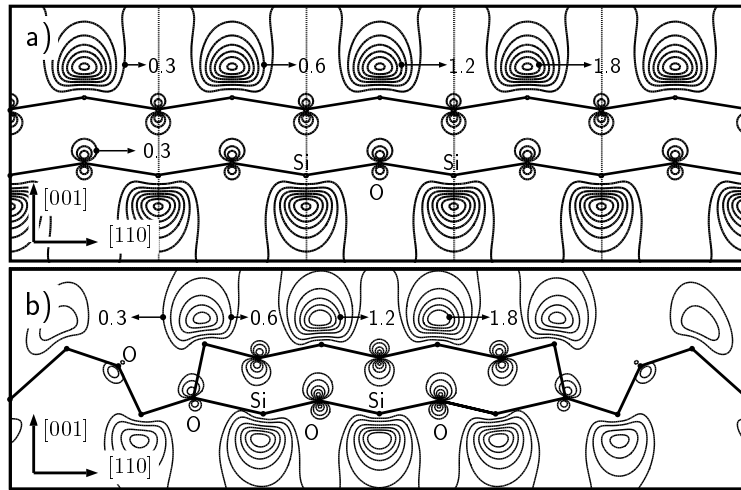


Figure 5.9: Contour plot of  $|\psi_{n\mathbf{k}}(\mathbf{r})|^2 \times 1000$  for a) the lowest unoccupied band in the infinite O-2NN chain, and b) the highest occupied band in the  $O_9$ -2NN chain. For both,  $\mathbf{k}$ -points in the middle of the zone along (001) were taken. Contour levels are the same in both plots.

Hydrogen has also been detected by ENDOR in the shallow thermal donor (STD) family (Martynov *et al.*, 1995). However the thermal stability of the STD defects — formed at 450°C — implies a fundamental difference between TDD-H and the STD single donors.

Efficient H-attachment to the O-2NN TDD model can be attained if the topological defect is eliminated. This is done in a manner shown in Figure 5.10. Here, the coordination of all silicon, oxygen and hydrogen atoms is such so that the two electrons in the stress-induced states fall into the valence band. The binding energy of each H atom, compared when it is bond-centred and away from the chain, is 1.8 eV. This value is near the experimental observations, 1.9 eV for the first TDD members. As shown in Fig. 5.10, the H-atom is already near a Si-Si bond-centre site, and hence we expect a low capture barrier. Standard  $sp^3$  Si-H bonds are very strong. In Si crystals these normally have 1.5 Å, with a Si-H bond energy of about 2.5 eV (Hourahine *et al.*, 1999). However, in the case of the H-(O<sub>n</sub>-2NN)-H defects, the Si-H bond is almost 1.7Å. This is due to a complex hybridisation of the end-Si atom, still interacting with the end-O atoms (see Fig. 5.10), leading to a weaker binding energy, and hence explaining the low thermal stability of the TDD-H defects.

Although there is still no experimental evidence for the kind of structure shown in Fig.5.10, these results can be useful for experimentalists in two main aspects. (i) The stress-induced state is not removed after H-attachment — it is simply depopulated. This would suggest that TDD-H defects can act now as acceptors, with a deep electron trap at  $\sim 0.15$  eV, and possibly a second acceptor level at  $\sim 0.07$  eV. These are the donor levels observed in DLTS for the active TDD species (Henry *et al.*, 1984; Benton *et al.*, 1985). The second aspect is (ii) that the longer Si-H bonds in the O<sub>n</sub>H<sub>2</sub>-2NN defects imply than any Si-H related stretch vibrational mode should fall below the usual 2000 cm<sup>-1</sup> region. Further work on this issue is required.

#### 5.4.4 TDD family members

We can now identify the donors with different oxygen chains. The chains with odd number of oxygen atoms have  $C_{2v}$  symmetry but ones with even numbers have  $C_{2h}$  symmetry. The

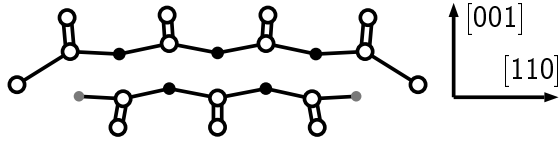


Figure 5.10: Structure for the hydrogenated  $O_5$ -2NN defect. Silicon, oxygen and hydrogen are shown in white, black and gray circles. Note that all Si, O and H atoms are four-fold, two-fold and mono-coordinated respectively.

vibrational modes of  $O_2$  and  $O_3$  have been identified and these species are not thermal donors (Murin and Markevich, 1996). TDD(0) may be identified with a chain of perhaps four or five O atoms suggesting TDD( $N$ ) is  $O_n$  with  $n = N + 4$  or  $N + 5$  (Jones *et al.*, 2001). This agrees with observations that a loss of around 9-10 oxygen atoms per TDD from solution accompanies the formation of the average donor, taken to be TDD(5) or TDD(6) (Schroder *et al.*, 1988; Newman, 1985). We have also mentioned above that  $O_n$ -2NN chains are more stable than  $O_n$ -1NN chains for more than 6-8 O-atoms. We are not convinced by the recent suggestion that different donors are alternative conformations with the same number of O-atoms. This is because the barriers between these conformations are too low – around 0.3 eV (Lee *et al.*, 2001), and stress-alignment experiments show that the donors can be aligned with barriers comparable with single oxygen diffusion. Thus during stress alignment, the cluster appears to dissociate and subsequently reforms with a different alignment.

Recent high field EPR experiments indicate that the symmetry of all the donors, except the second, is not strictly  $C_{2v}$  although the difference appears small (Dirksen *et al.*, 1998). Furthermore, ENDOR studies (Michel *et al.*, 1989; Spaeth, 1996) indicate the presence of two shells of  $^{17}O$  hyperfine tensors with axes around  $62^\circ$  with [001] and close to that expected from oxygen lying between neighbouring Si atoms.

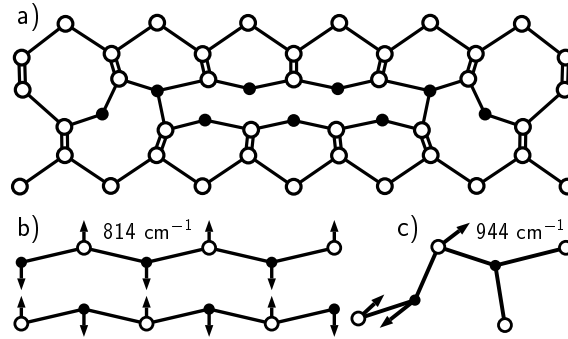


Figure 5.11: a)  $O_9$ -2NN double donor. The white and black circles denote Si and O atoms respectively. The two observed O-bands in TDD( $N$ ) at  $\sim 720$  and  $\sim 1000$   $\text{cm}^{-1}$  in Si ( $\sim 600$  and  $\sim 780$   $\text{cm}^{-1}$  in Ge), are assigned to chain and end oxygen modes shown in b) and c) respectively.

#### 5.4.5 Infrared absorption spectra

Further support for the model comes from the observations and analysis of the LVMs associated with each donor. The bands related to TDD are positioned in the wavenumber regions of 945-1000, 700-730 and 575-580  $\text{cm}^{-1}$  (Lindström and Hallberg, 1994; Murin *et al.*, 2001). These can be seen in Figure 5.12. The 1000 and 730  $\text{cm}^{-1}$ -bands undergo upward sequential shifts (with  $N$ ) of about 10 and 4  $\text{cm}^{-1}$  respectively, and display an oxygen origin as they shift with  $^{18}\text{O}$ . The 580  $\text{cm}^{-1}$ -band does not shift noticeably with  $N$  or oxygen isotopic mass. By using mixtures of  $^{16}\text{O}$  and  $^{18}\text{O}$ , it has been found that the upper band does not yield any new modes (spectra 3 and 4), suggesting that any oxygen atom is decoupled from any other. However, the 730  $\text{cm}^{-1}$ -band exhibits mixed modes proving for the first time that oxygen atoms are coupled together and in close spatial proximity (Murin *et al.*, 2001).

Similar results have also been obtained for the 600  $\text{cm}^{-1}$ -band in Ge co-doped with  $^{16}\text{O}$  and  $^{18}\text{O}$  (see Fig. 5.13), i.e., an unique mixed mode at about 595  $\text{cm}^{-1}$  is observed after HT at 370°C for 15 h. However, unlike in Si, a mixed mode appears also in the upper band region at 755  $\text{cm}^{-1}$ , along with  $^{16}\text{O}$  and  $^{18}\text{O}$  modes at 780 and 742  $\text{cm}^{-1}$  (Murin *et al.*, 2001).



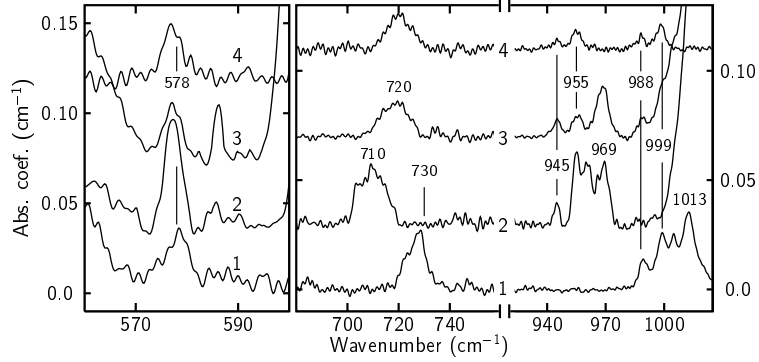


Figure 5.12: Absorption spectra measured at 300 K for Si:O samples heat-treated at 420°C for 15h: 1 -  $[^{16}\text{O}_i]=1.3\times 10^{18} \text{ cm}^{-3}$ ; 2 -  $[^{18}\text{O}_i]=1.5\times 10^{18} \text{ cm}^{-3}$ ; 3 and 4 -  $[^{16}\text{O}_i]=8\times 10^{17} \text{ cm}^{-3}$ ,  $[^{18}\text{O}_i]=7\times 10^{18} \text{ cm}^{-3}$ . The spectrum of a non-annealed sample was used as a reference in 4. Data kindly provided by L. I. Murin.

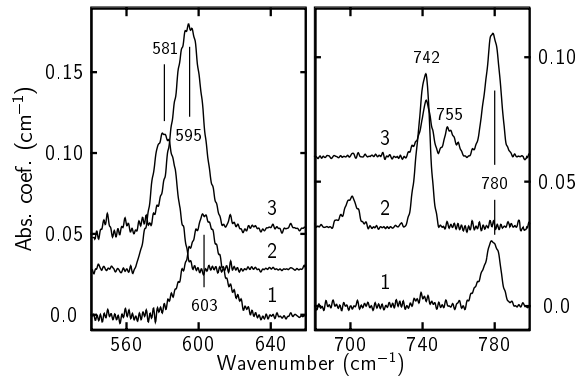


Figure 5.13: Absorption spectra measured at 300 K for Ge:O samples heat-treated at 370°C for 20 h: 1 -  $[^{16}\text{O}_i]=2.3\times 10^{17} \text{ cm}^{-3}$ ; 2 -  $[^{18}\text{O}_i]=3.2\times 10^{17} \text{ cm}^{-3}$ ; 3 -  $[^{16}\text{O}_i]=2.3\times 10^{17} \text{ cm}^{-3}$ ,  $[^{18}\text{O}_i]=1.7\times 10^{17} \text{ cm}^{-3}$ . Data Kindly provided by V. V. Litvinov.

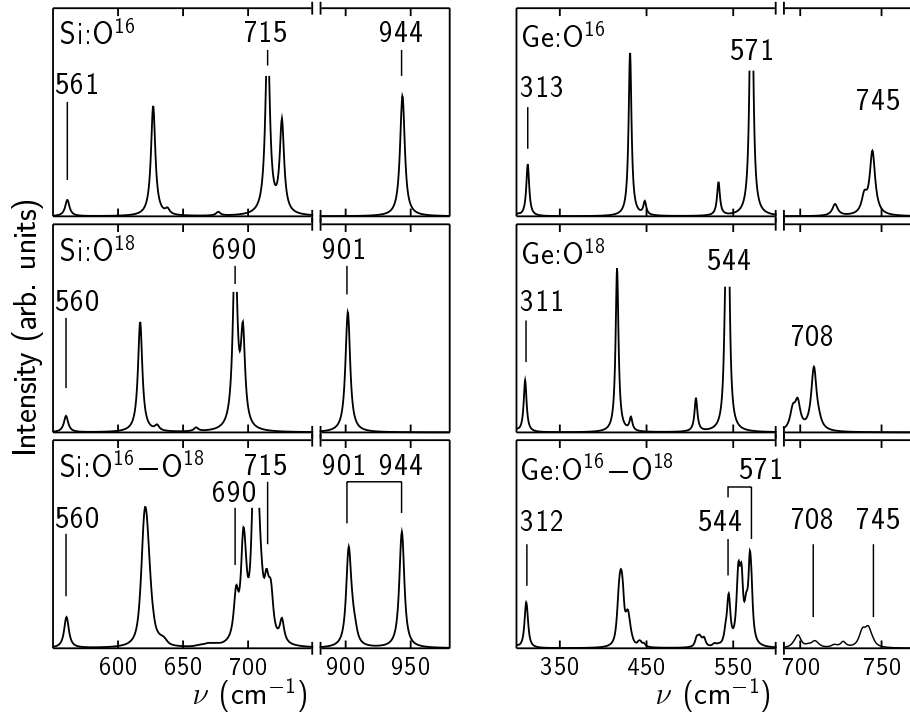


Figure 5.14: Calculated IR-intensities of the modes for  $O_7$ -2NN in Si, broadened with Lorentzian functions by  $4 \text{ cm}^{-1}$ , and evaluated as described above.  $^{16}\text{O}$  and  $^{18}\text{O}$  spectra are shown in a) and b) respectively, whereas the  $2^7$  combinations for a 50-50  $^{16}\text{O}$ - $^{18}\text{O}$  mixture is depicted in c).

To understand the LVMs of the donors, we first calculate the long wavelength modes of an infinite periodic O-2NN chain. The two IR-active modes lie at  $564$  and  $814 \text{ cm}^{-1}$  in Si and  $323, 625 \text{ cm}^{-1}$  in Ge. The  $814 \text{ cm}^{-1}$  is shown in Fig. 5.11(b) and clearly induces a dipole moment along  $[001]$ . The  $564 \text{ cm}^{-1}$  mode involves very little movement of oxygen atoms, and is localised to the Si atoms above and below the core whose bonds are compressed by the  $[001]$  stress. This has a dipole moment along  $[1\bar{1}0]$ , and orthogonal to the chain. Thus the simple periodic chain model explains why only a few oxygen modes can be detected in each donor, as only transverse long wavelength modes are IR-active.

We now consider the oxygen related modes arising from the ends of the chain (Fig. 5.11(c)). The highest frequency modes, evaluated from the dynamical matrices of the end-O atoms,

Table 5.3: Observed and calculated high frequency  $^{16}\text{O}$  modes ( $\text{cm}^{-1}$ ), of TDD( $N$ ) and  $\text{O}_{N+4}\text{-2NN}$  respectively.

$N$	1	2	3	4
Calc.	940	951	963	969
Obs.	975	988	999	1006

are given in Table 5.3. There is a 11:12:6  $\text{cm}^{-1}$  increase with  $N$  in excellent agreement with the observed increases of 13:11:7  $\text{cm}^{-1}$  for TDD(1), TDD(2), TDD(3) and TDD(4). For Ge, the calculated increments are 9:8:7  $\text{cm}^{-1}$  compared with 5:4:3  $\text{cm}^{-1}$  observed for TDD(1), TDD(2), TDD(3) and TDD(4). Thus the model accounts for the shift in the high frequency mode with  $N$ .

We turn now to the effect of a 50-50 mixture of  $^{16}\text{O}$  and  $^{18}\text{O}$ . We consider  $\text{O}_7\text{-2NN}$  and plot in Fig. 5.14 the calculated relative intensities of the local modes. We note that the end-mode at 944  $\text{cm}^{-1}$  does not split in agreement with the data. This is because the displacement of the atoms shown in Fig. 5.11(c) is localised to the end  $\text{O}\text{-1NN}$  atom. However, in contrast with this, the mode around 715  $\text{cm}^{-1}$  due to the  $\text{O}\text{-2NN}$  core splits in the mixed case (Fig 5.14), again in agreement with the data. This reflects its chain origin illustrated in Fig. 5.11(b). The chain related 560  $\text{cm}^{-1}$  Si mode is quite insensitive to  $\text{O}$ -substitution consistent with an assignment to the observed 580  $\text{cm}^{-1}$  band. It is also important to note that the calculated  $^{16}\nu/^{18}\nu$  ratios for the 715 and 944  $\text{cm}^{-1}$ -modes are 1.036 and 1.046, in good agreement with the observations. Fig. 5.14 also shows that other modes around 726 and 627  $\text{cm}^{-1}$  in Si are expected to be IR-active but have not yet been detected.

In the case of Ge, both the end-mode at 745  $\text{cm}^{-1}$  and the chain mode at 571  $\text{cm}^{-1}$  ( $^{16}\text{O}$ ) are, however, split in the mixed isotopic case, again in agreement with the data. The different behaviour of the end-mode from that in Si is striking and originates from the the closeness in the Ge-O-Ge angles at the ends and middle of the chain when compared with Si. This can be compared with the  $\sim 140^\circ$  Ge-O-Ge and  $\sim 160^\circ$  Si-O-Si angles for

interstitial oxygen (Coutinho *et al.*, 2000b). In Ge, two superimposed modes at  $\sim 745 \text{ cm}^{-1}$  are IR-active. The stronger mode behaves as in silicon — with no mixed modes, but the weaker mode gives rise to mixed bands. Hence, the integrated absorption of the mixed bands is considerably smaller than twice of the  $^{16}\text{O}$ - and  $^{18}\text{O}$ -bands.

#### 5.4.6 Stress-energy tensor

The compressive stresses exerted by the O-2NN core and O-1NN ends are different. The former lies along [001] and the latter along [111] and  $[\bar{1}\bar{1}1]$ . Thus the [001] displacement of Si along the chains is different for the two regions. Table 5.4 shows that the central Si atoms exert a very large compressive strain which decreases with the length of the chain. This has implications for the stress-energy or piezospectroscopic tensors for the donors. Table 5.4 shows that the calculated tensors for the smaller  $C_{2v}$  chains possess principal values very close to those observed by electronic infra-red and EPR experiments. Note that O<sub>6</sub>-NN has  $C_{2h}$  symmetry, and hence two principal directions of the tensor are rotated by  $\theta = 9^\circ$  from the [001] and [110] crystallographic axes. It is unclear whether this angle lies inside the experimental error for the tensors of those donors displaying lower symmetry than  $C_{2v}$  (Dirksen *et al.*, 1998). However, the calculations correctly reproduce the principal values of the stress tensor and their variation with donor species. We note that the decreasing [001] strain with increasing  $N$  would result in shallower strain induced states consistent with the decreasing donor level.

### 5.5 Summary

In conclusion, we have shown that oxygen atoms lying in chains diffuse quickly and form extended chains lying along [110]. The most stable long chains involve O atoms linking second neighbouring Si atoms (O-2NN). The chains are less stable than an  $\text{SiO}_2$  precipitate but form through their rapid kinetics. The activation energy for the kick-out of a single Si interstitial appears to be considerable and will not occur during the early-stages at  $450^\circ\text{C}$ . The chains give rise to a compressive stress along the [001], leading to a stress induced

Table 5.4: Calculated [001] displacements ( $\text{\AA}$ ),  $\delta_c(001)$  and  $\delta_e(001)$ , of central and end Si-atoms, and stress-energy tensor elements  $B$  along [001] and [110] (eV), for  $O_n$ -2NN chains. Observed tensors for the early TDD members were measured by FTIR spectroscopy and EPR (starred values) (Trombetta *et al.*, 1997; Watkins, 1996).

Calc.	$O_5$ -2NN $C_{2v}$	$O_6$ -2NN $C_{2h}$	$O_7$ -2NN $C_{2v}$	$O_\infty$ -2NN
$\delta_c(001)$	0.43	0.42	0.41	0.34
$\delta_e(001)$	0.22	0.22	0.22	–
$B_{001}$	–13.8	–13.2	–12.1	–
$B_{110}$	10.5	9.9	8.3	–
Obs.	TDD(2)	TDD(3)	TDD(4)	
$B_{001}$	–12.2	–11.9	–11.4	
$B_{110}$		10.3*	8.5*	

empty gap level lying below the conduction-band, whose effective-mass wavefunction is localised on  $\sim 1000$  surrounding Si atoms. The ends of the finite chain are terminated by O-1NN atoms. The donor activity arises from a pair of over-coordinated O-atoms at the interfaces between two species of oxygen in the chain. The energy levels of these regions lie above the stress induced gap level and electrons preferentially occupy the latter.

The two types of oxygen lead to different stress distributions. The core region is highly compressive along [001] while the end region leads to stress along the chain. The magnitudes of the calculated stress-energy tensor are consistent with experimental values. The same model also accounts for the vibrational modes of the donors (Murin *et al.*, 2001).

It is to be noted that the model suggests that single donors can be formed by substitution of O or Si by group-III or group-V impurities. Other possibilities include substitution of O by a tri-valent complex as a C-H unit. The former probably leads to the NL10(Al) family (Gregorkiewicz *et al.*, 1987; Ammerlaan *et al.*, 1996) and the later to the H-related shallow thermal donors (Ewels *et al.*, 1996a).

The vibrational spectra have been calculated for a model of the thermal donor consisting of O atoms arranged in a periodic chain. The high and low frequency bands of each donor are assigned to modes of the end-atoms and to IR-active long wavelength bands of the chain respectively. The observations of only a few O-related bands is accounted for even though each donor contains many O atoms. The great disparity in Si-O-Si bond angles between the core and end atoms explains why these atoms are not coupled in Si. This is not the case in Ge. The model also accounts for the shift in the bands with increasing  $N$  and gives two additional modes for small O chains which have not yet been observed.

## Chapter 6

# Shallow thermal donors with hydrogen

### 6.1 Introduction

Low temperature  $e$ -irradiation of Si generates mobile Si interstitials which are readily trapped by substitutional carbon defects forming carbon interstitials ( $C_i$ ) (Watkins and Brower, 1976). In turn, these are mobile at room temperature and subsequently complex with many impurities including oxygen. The interstitial carbon-oxygen centre ( $C_iO_i$ ), is a product of the latter interaction and is a stable defect with an annealing temperature around 350-450°C. It has been detected by all four principal methods used to characterise defects. Electron paramagnetic resonance (EPR) experiments relate the G15 signal to  $C_iO_i^+$ . The similarity of its magnetic properties with that of the carbon interstitial implies that the C-atom is only slightly affected by oxygen which is assumed to be bonded to remote Si atoms such as  $Si_2$  and  $Si_3$  shown in Figure 6.1(a) (Trombetta and Watkins, 1987, 1988).

The defect gives a prominent 0.7896 eV photoluminescent (PL) signal (C-band) (Yukhnevich *et al.*, 1966), associated with several local mode replicas (Kurner *et al.*, 1989; Lightowers and Safonov, 1997). Previous Fourier transform infra-red (FTIR) spectroscopic experi-

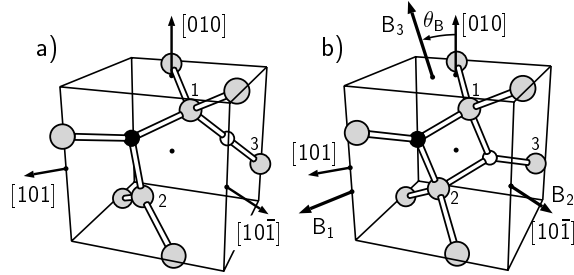


Figure 6.1: Models for  $C_iO_i$ . (a) Divalent oxygen model, (b) Trivalent oxygen model. Gray, black, white atoms are Si, C, O. Crystallographic axes and principal directions of the  $B$  tensor are also shown.

ments have identified local vibrational modes (LVMs) at 1116, 865, 742, 550 and  $529.8\text{ cm}^{-1}$ , the highest of which is carbon and not oxygen related (Davies *et al.*, 1986). Finally, deep level transient spectroscopy (DLTS) has linked a donor level at  $E_v + 0.38\text{ eV}$  with the defect (Mooney *et al.*, 1977).

Earlier theoretical modelling had found that the oxygen atom was strongly affected by carbon and was not divalent as in Fig. 6.1(a), but rather, was bonded to three Si atoms as illustrated in Fig. 6.1(b) (Jones and Öberg, 1992; Snyder *et al.*, 1996). This is because the greater electronegativity of carbon encouraged electron transfer from the  $Si_2$  atom with the dangling bond shown in Fig. 6.1(a). This leaves the dangling bond orbital empty and leads to a dative bond with a lone pair orbital on oxygen. Thus the oxygen atom is trivalent. Over-coordinated oxygen atoms are currently of interest because of their possible role in thermal donor defects (Jones, 1996).

The main evidence in support of this model lay in the lack of any mode around  $1136\text{ cm}^{-1}$  related to bond-centred interstitial oxygen ( $O_i$ ). Here we present further support to the model and demonstrate that its calculated donor level and stress-energy, or piezospectroscopic, tensor are in agreement with the observations.

Further interest in the defect has recently arisen from the observation of a marked reduction in its concentration in irradiated samples into which hydrogen had been introduced by wet-etching (Feklisova and Yarykin, 1997; Feklisova *et al.*, 1999). These studies suggested



that the  $C_iO_i$  defect can trap up to two hydrogen atoms and that the single hydrogenated centre possessed a deep hole trap H4 at  $E_v + 0.28$  eV (Feklisova *et al.*, 1999). This hole trap was recently reassigned to the VOH defect (Feklisova *et al.*, 2001)

In view of these developments, we have investigated the interaction of the defect with hydrogen paying attention to its electrical properties. It is clear that the defect with two H atoms is inert but a single H atom results in a bi-stable defect with intriguing properties. In one form it behaves as a deep acceptor but in another configuration, it is a shallow donor. The calculated configuration energy curves for the defect are strikingly similar to a hydrogen related radiation-induced shallow donor labelled D1. Moreover, the calculated oxygen related vibrational mode and its anomalous upward shift with hydrogen are close to the values observed for D1.

This defect appears to be the first of a family of shallow single donors which are successively produced on annealing  $e$ -irradiated Czochralski-grown Si (Cz-Si) into which hydrogen had been introduced (Markevich *et al.*, 1994). The first two members D1 and D2 are formed around 350°C and 450°C respectively and have  $(0/+)$  levels at  $E_c - 42.6$  meV and  $E_c - 37.0$  meV which are comparable with phosphorus ( $E_c - 45.6$  meV). The defects possess a Rydberg series of excited states, and the effective-mass IR transitions for D2 and D3, are identical with those of the shallow thermal donors STD(H)2 and STD(H)3 found by annealing O-rich Si containing hydrogen (Newman *et al.*, 1996, 1998). The STD(H) $N$  family members are known to contain hydrogen as their electronic transitions shift in deuterated material. However, the STD defects are formed in annealed Cz-Si without prior irradiation and they have been suggested to be responsible for the NL10(H) family of shallow single thermal donors (Newman *et al.*, 1996). It has also been proposed that these centres contain, in addition to hydrogen, interstitial carbon and oxygen (Ewels *et al.*, 1996*a,b*). However, there is no spectroscopic evidence for these impurities in the DN and STD(H) $N$  families. Nevertheless, weak  $^{17}\text{O}$ -hyperfine satellites have been found in NL10 shallow donors in Al doped samples (Gregorkiewicz *et al.*, 1987, 1988).

A considerable body of information about D1 has been found by electrical, photo-electrical, optical and magnetic experiments (Markevich *et al.*, 1994, 1998*a*, 1995, 1997*b,a*, 1998*b*).

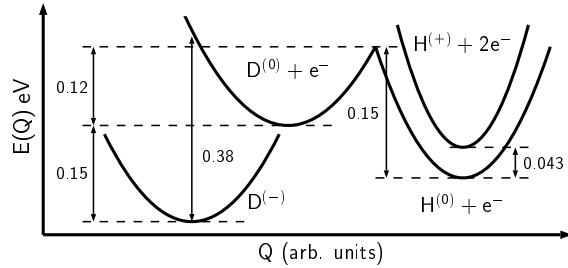


Figure 6.2: Configuration coordinate diagram for D1 according to Markevich *et al* (Markevich *et al.*, 1997b). Quoted energies are based on electrical, optical and capacitance measurements.

Thus it is known that the defect is bi-stable, assuming the H-form in the positive and neutral charge states and the D-form in the negative charge state. A metastable neutral D-form (originally labelled X), also exists. Hall effect and conductivity studies show that the defect has a negative- $U$  with an occupation level (the average of the donor and acceptor levels) at  $E_c - 0.076$  eV. Electronic IR absorption studies show a donor level lying 43 meV below the conduction band and this then places the acceptor level, or the difference between  $D^-$  and  $H^0$ , at  $E_c - 0.11$  eV. DLTS and optical absorption studies were used to determine the other energies in the configuration coordinate diagram shown in Fig. 6.2.

The D-form of D1 has also been correlated with a local vibrational mode at  $1025.5\text{ cm}^{-1}$  that shifts *upwards* to  $1027.9\text{ cm}^{-1}$  with deuterium, demonstrating that this defect contains H (Markevich *et al.*, 1998b). This unusual shift has not been explained previously but here we link it to an anti-crossing with an unobserved carbon-hydrogen wag mode. No vibrational modes have been found for the H-form.

The neutral H-form of D1 has also been associated with an EPR centre labelled TU1 detected under illumination conditions (Markevich *et al.*, 1997a). Its isotropic  $g$ -tensor probably arises from the delocalised spin-density which does not reflect the true symmetry of the defect. One  $^{29}\text{Si}$  hyperfine satellite has been resolved having an isotropic interaction of about 60 MHz. Comparing this with the isotropic hyperfine interaction of 4594 MHz arising from a free  $^{29}\text{Si}$  atom (Morton and Preston, 1977), gives 1.3% of the spin-density

located on this unique atom. Hyperfine interactions with hydrogen were recently observed for D1 and D2 by using electron-nuclear double resonance (ENDOR) spectroscopy (Langhanki *et al.*, 2001). One principal axis of the hyperfine tensor is nearly parallel to the  $\langle 110 \rangle$  direction suggesting a H bond lying along this direction. The isotropic part of the hyperfine tensor corresponds to a minute spin-density on H of  $6 \times 10^{-3}\%$ . Similar densities and hyperfine tensors were measured for the NL10(H) defects (Ammerlaan *et al.*, 1996), strengthening the link between the STD(H)*N*, NL10(H), and DN families.

It has been suggested that D1 is a complex of hydrogen with an oxygen-related radiation induced defect like VO or  $C_iO_i$  (Markevich *et al.*, 1994). However, VOH is an acceptor with a level at  $E_c - 0.31$  eV (Svensson *et al.*, 1989; Artacho and Ynduráin, 1989; Nielsen *et al.*, 1999; Peaker *et al.*, 1999), while VOH<sub>2</sub> is passive (Markevich *et al.*, 2000). We show that D1 has many properties in common with  $C_iO_iH$ . This in turn suggests that the shallow thermal donors STD(H)*N* also contain interstitial carbon. It is known that interstitial carbon can be produced as a by-product of oxygen aggregation in annealed Cz-Si and does not require irradiation for its formation. This follows as annealing Cz-Si to about 450°C produces a set of prominent photoluminescent lines. One of these is the T-line at 0.935 eV which is known to be a complex involving interstitial carbon bonded to hydrogen and is stable up to  $\sim 600^\circ\text{C}$  (Safonov *et al.*, 1996). This thermal stability is comparable with the STD(H)*N* family which disappear around 550°C (Newman *et al.*, 1998).

## 6.2 The interstitial carbon-oxygen defect

### 6.2.1 Infra-red absorption spectrum

Table 6.2 gives the LVM-frequencies and their  $^{13}\text{C}$  and  $^{18}\text{O}$  isotopic shifts assigned to the  $C_iO_i$  defect Davies *et al.* (1986); Coutinho *et al.* (2001a). In descending frequency, they will be labelled as the 1116, 865, 742, 585, 550, 540 and 529  $\text{cm}^{-1}$ -bands respectively. The most important result is the observation of a significant 33.4  $\text{cm}^{-1}$  oxygen isotopic

shift *only* for the 742  $\text{cm}^{-1}$ -band, clearly indicating its oxygen character. This shift is in agreement with observations based on PL vibrational spectroscopy which only detects  $A_1$  modes (Kurner *et al.*, 1989; Lightowers and Safonov, 1997; Davies and Newman, 1994). Table 6.2 then clearly shows that the highest oxygen related frequency lies at 742  $\text{cm}^{-1}$ , compared with 1136  $\text{cm}^{-1}$  for  $O_i$ , and possesses an  $^{18}\text{O}$  shift considerably smaller than that of the asymmetric stretch mode in  $O_i$  (51.4  $\text{cm}^{-1}$ ) (Pajot *et al.*, 1995), where the O atom bridges neighbouring Si atoms.

The 585 and 540  $\text{cm}^{-1}$ -bands were recently identified with the  $C_iO_i$  complex (Coutinho *et al.*, 2001a). All the bands in Table 6.2 anneal out between 300-400°C along with bands related to VO. Simultaneously, there is a strong increase in the intensities of lines related to  $C_sO_i$ . Evidently, the annealing behaviour of two dominant defects,  $C_iO_i$  and VO, are closely related. Either vacancies, generated upon A-centre dissociation, are trapped by  $C_iO_i$ , or  $C_i$  atoms liberated from  $C_iO_i$  interact with VO. In both cases  $C_sO_i$  is formed.

## 6.2.2 Structure and energetics

In agreement with previous calculations (Jones and Öberg, 1992), we find the ground state structure of  $C_iO_i$ , is one where both carbon and oxygen are three-fold coordinated and form two vertices of a ring as shown in Figure 6.1(b). The structure where the O atom lies at the centre of the dilated Si-Si bond, shown in Fig. 6.1(a), relaxes spontaneously to the ring defect for both the neutral and positively charged centre. The binding energy between  $C_i$  and  $O_i$  is 1.7 eV and this large value is consistent with the high thermal stability of the defect.

## 6.2.3 Electrical activity

Table 6.1 shows that  $E(0) - E(+)$  for  $C_iO_i$  lies 0.08 eV above that for  $C_i$ . Therefore a deep donor level is estimated at  $E_v + 0.36$  eV in agreement with the observed DLTS level at  $E_v + 0.38$  eV (Mooney *et al.*, 1977). No acceptor or second donor levels were found. A Mulliken bond population analysis gives 25.4% and 0.1% of spin-density localised around

Table 6.1: Formation energies  $E_f$ ,  $E(-/0)$ ,  $E(0/+)$ , and acceptor  $(-/0)$  and donor  $(0/+)$  levels of  $O_i$ ,  $C_i$ ,  $C_iO_i$ ,  $C_iO_iH$  and  $C_iO_{2i}H$  defects (eV).  $C_iO_iH$  and  $C_iO_{2i}H$  defects have forms R and O. Values are calculated using Gaussian  $s, p$ -orbitals with 1 set of Gaussian functions at bond-centre sites (4 orbitals), and bracketed values are runs with 2 Gaussians (8 orbitals).  $E_f$  was calculated by taking chemical potentials of Si, O, C and H from silicon,  $\alpha$ -quartz, diamond, and molecular  $H_2$  environments respectively. The last two columns are estimates of acceptor and donor levels relative to the band edges found as described in the text.

	$E_f$	$E(-/0)$	$E(0/+)$	$E_c - (-/0)$	$(0/+) - E_v$
$O_i$	1.809 (1.817)				
$C_i$	4.122 (4.056)	7.073 (6.963)	6.666 (6.603)		
$C_iO_i$	4.212 (4.107)		6.750 (6.731)		0.364 (0.408)
$C_iO_iH$ -(R)	3.309 (3.281)		7.506 (7.416)		1.120 (1.093)
$C_iO_iH$ -(O)	3.475 (3.331)	6.908 (6.865)		0.265 (0.198)	
$C_iO_{2i}H$ -(R)	3.923 (3.858)		7.547 (7.419)		1.161 (1.096)
$C_iO_{2i}H$ -(O)	4.479 (4.308)	6.859 (6.798)		0.314 (0.265)	

the carbon and oxygen atoms respectively. The first is in agreement with the 28.6% spin localisation on carbon measured for G15 (Trombetta and Watkins, 1987). In addition, the four Si atoms bonded to Si<sub>1</sub> and Si<sub>2</sub> in Figure 6.1(b) share about 15% of the unpaired spin-density. The presence of oxygen rotates the Si<sub>2</sub>-C bond through 22° away from the [010] axis. This is in excellent agreement with the angle of  $\theta_A = 20^\circ \pm 5^\circ$  that two of the principal directions of the <sup>13</sup>C-hyperfine tensor make with the crystallographic axes (Trombetta and Watkins, 1987).

#### 6.2.4 Stress-energy tensor

The principal directions of the calculated stress-energy tensor are shown in Figure 6.1(b). The  $C_{1h}$  symmetry of the defect implies that one principal direction (corresponding to the  $B_2$  component) lies along  $[10\bar{1}]$  but the other directions are rotated from the [010] and the [101] axes. For the positively charged defect, the rotation angle is calculated to be  $\theta_B = 22^\circ$ , and the principal values of the tensor are 8.5, 2.3 and  $-11.8$  eV for  $B_1$ ,  $B_2$  and  $B_3$  respectively. The angle arises from the perturbation to the structure caused by the oxygen atom as it vanishes for the  $C_i$  defect. Stress alignment experiments give the measured values of  $B_1$ ,  $B_2$  and  $B_3$  for G15 to be 8.6, 0.2 and  $-8.8$  eV and  $\theta_B = 15^\circ$ , and thus the model accounts well the observations.

#### 6.2.5 Local vibrational modes

The LVMs for the neutral defect are shown in Table 6.2. Of special interest are the oxygen related modes. The highest of these lies at  $760\text{ cm}^{-1}$  – well below the asymmetric stretch mode for interstitial oxygen at  $1136\text{ cm}^{-1}$ . This is a characteristic of the weakened bonds of over-coordinated oxygen relative to those in Si-O-Si. The oxygen mode is very close to the observed band at  $742.8\text{ cm}^{-1}$ . The observed and calculated <sup>18</sup>O-shifts are also very close, lying at  $33.4$  and  $35.6\text{ cm}^{-1}$  respectively. Two carbon related modes are calculated to lie at  $1138$  and  $876\text{ cm}^{-1}$ , close to the observed  $1116$  and  $865\text{ cm}^{-1}$ -bands. Their shift with <sup>13</sup>C demonstrates that they are carbon related in agreement with the observations.

Table 6.2: Observed and Calculated Local Vibrational Modes ( $\text{cm}^{-1}$ ), for  $\text{C}_i\text{O}_i^0$ . First three columns report absolute frequencies, whereas columns four onwards give their downward isotopic shifts.

$^{16}\text{O}, ^{12}\text{C}$		$^{16}\text{O}, ^{13}\text{C}$		$^{18}\text{O}, ^{12}\text{C}$		$^{18}\text{O}, ^{13}\text{C}$	
Obs.	Calc.	Obs.	Calc.	Obs.	Calc.	Obs.	Calc.
1116.3	1137.6	36.4	37.7	1.0	1.0		38.8
865.9	876.1	23.9	24.5	0.15	0.1		24.6
742.8	759.6	0.5	0.3	33.4	35.6		35.8
$\sim 588$	593.4	—	0.1	$\sim 3$	3.2		3.3
549.8	555.8	0.2	0.3	0.3	0.2		0.5
$\sim 542$	544.7	$\sim 0.5$	0.1	$\sim 1.5$	0.5		0.5
529.6	544.2	0.1	0.0	5.2	5.4		5.5

The four remaining low frequency modes at 593, 556, 545 and 544  $\text{cm}^{-1}$  have not been assigned previously. They arise from vibrations of Si neighbours to the defect core, and are properly described only when energy second derivatives with these atoms are calculated directly from the *ab-initio* program. In this sense they are similar to the lattice-induced band at 517  $\text{cm}^{-1}$  due to interstitial oxygen (Coutinho *et al.*, 2000b). These modes display very small isotopic shifts upon C or O substitution. Frequencies and isotopic shifts of the 544 and 545  $\text{cm}^{-1}$ -modes agree well with those of the measured 529 and 540  $\text{cm}^{-1}$ -bands, supporting the assignment of the later to  $\text{C}_i\text{O}_i$  (see Subsection 6.2.1). However, the symmetry of the 556 and 544  $\text{cm}^{-1}$  modes is  $B$  and in conflict with the claim that only  $A$  modes are detected as phonon replicas. According to group theory, this is not actually the case for a  $C_{1h}$  defect although then the dipole matrix element must involve components parallel and perpendicular to the mirror plane (or vice-versa) for the zero phonon line and replica respectively.

In summary, the agreement between the calculated and observed modes, their isotopic shifts, the energy level and stress-tensor, give convincing evidence for the ring structure

Table 6.3: Relative energies (eV) for five  $C_iO_iH$  structures differing in the attachment of hydrogen. R (ring) and O (open) core structures were considered.  $X$ -H represent structures where the H atom is bonded to  $X$ , where  $X$  can be C,  $Si_1$ ,  $Si_2$ , or the O atom in Figure 6.1(b). NS stand for Not Stable.

Core	R			O		
	Charge state +	0	-	+	0	-
C-H	0.00	0.00	NS	NS	0.17	0.00
$Si_1$ -H	NS	NS	NS	NS	NS	NS
$Si_2$ -H	NS	NS	NS	1.67	0.89	0.53
O-H	2.93	2.89	2.32	NS	NS	NS

of  $C_iO_i$ .

### 6.3 Hydrogenation of $C_iO_i$ and the STD defects

It is well established that hydrogen interacts effectively with both deep and shallow centres, displacing or eliminating their energy levels in the gap. Moreover, dangling bonds are particularly attractive sites for H-attack (Pearson *et al.*, 1992; Coomer *et al.*, 2000; Lightowers *et al.*, 1994).

#### 6.3.1 $C_iO_iH$ as a precursor for STD(H)

The  $C_iO_i$  defect, in the neutral or positive charge states, possesses one fully or partially occupied  $p$ -like dangling orbital centred on the carbon atom. This is a likely place for H attachment as the carbon atom is then saturated leaving the electrical activity confined to the  $Si_2$  dangling bond. If this is empty, as in the positively charge defect, then a ring structure involving oxygen is likely to form in the same way as in  $C_iO_i$ . However, in the neutral or negative centre, an anti-bonding orbital will be occupied and we expect that



the ring will break. This would leave an occupied dangling bond orbital on the Si radical near an oxygen atom in its normal interstitial bond centred configuration. We call the ring structure the R-form and the open configuration, the O-form. However, there are several other possible sites for H attachment. It could bond with silicon atoms Si<sub>1</sub> and Si<sub>2</sub> in Figure 6.1(b), or with the oxygen atom. The relative energies when H is in all these structures are given in Table 6.3 for the positive, neutral and negative charge states. Our conclusion is that H prefers to bond with carbon in all cases. However, as expected, the structure depends on the charge state with the R-form lowest in energy for the positive and neutral defects and the O-form in the negative centre.

In Fig. 6.3, a configuration diagram is shown for the defect (Coutinho *et al.*, 2001a). Here, quoted values correspond to the results of the calculations, and the parabolic shapes are only schematic. In the neutral defect, the R-form has the lowest energy while the O-form is metastable by 0.17 eV. By carefully mapping the energy surface linking the two structures, we find  $\sim 0.10$  and  $\sim 0.27$  eV barriers for O $\rightarrow$ R and R $\rightarrow$ O paths respectively. In the positive charge state, the ring form is again stable but the O-form is now unstable and relaxes spontaneously to R.

In the negative charge state, however, the Si<sub>2</sub> dangling bond is occupied with two electrons and a dative bond with oxygen cannot occur. Thus the ring form is unstable and spontaneously relaxes to the O-form. Consequently the defect is bi-stable taking the O-form in the negative state and the R-form in the positive case.

The dissociation energy of the R-form into C<sub>i</sub>H and O<sub>i</sub> defects was estimated to be 1.4 eV. Once this dissociation has occurred, it is expected that the defects would be lost as previous theory has indicated that C<sub>i</sub>H diffuses faster than C<sub>i</sub> (Leary *et al.*, 1998). The dissociation path involving the release of H is unlikely to occur. This is because the binding energies of H with the C<sub>i</sub>O<sub>i</sub> centre are found to be about 2.5 eV. These were calculated by moving H<sup>-</sup> or H<sup>(0)/(+)</sup> from the defect and placing it at an interstitial T or BC sites respectively.

We now consider the energy levels of the defect. These were calculated for the R and O-forms separately, as these are the ground states for the positive and negative charge states respectively (see Table 6.3). The difference in energies of O<sup>-</sup> and O<sup>0</sup> when compared with

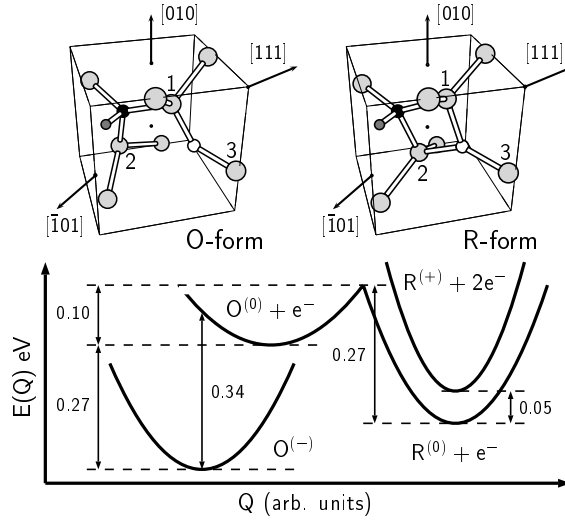


Figure 6.3: Configuration coordinate diagram for  $C_iO_iH$ . Atomic structures for O and R-forms are also shown. Gray, black, and white atoms are Si, C, and O respectively. The small gray atom bonded to carbon is H. Quoted values were calculated by the total energy method.

$C_i^-$  and  $C_i^0$  shows that the  $(-/0)$  level lies at  $E_c - 0.27$  eV. This is not the thermodynamic level as the neutral O-form is metastable with respect to the R-form. Nevertheless, it can be compared with the 0.15 eV emission barrier measured for D1 in the D-form (see Figure 6.2). In the R-form, the  $(0/+)$  level lies at  $E_c - 0.05$  eV. This demonstrates that the defect is a shallow donor in one form and a deep acceptor in the other. Using the 0.17 eV difference in energies of the two neutral forms, yields the thermodynamic  $(-/0)$  level at  $E_c - 0.1$  eV in excellent agreement with the  $(-/0)$  level at  $E_c - 0.11$  eV for the D1 centre described in the introduction.

These results are summarised in Figure 6.3. If the charge state of  $O^-$  configuration is changed to become neutral, the energy drops 0.06 eV upon relaxation. The barrier for  $R^0 \rightarrow O^0$  is about 0.27 eV while  $R^0$  is 0.17 eV more stable than  $O^0$ . The inverted order of energy levels implies that  $U = E(-/0) - E(0/+) = -0.05$  eV is negative.

The bi-stability properties and electronic levels for  $C_iO_iH$  shown in Fig. 6.3, and those for the D1 defect shown in Fig. 6.2 are strikingly similar. Thus we identify the R and O-forms

with the experimentally labelled H and D-forms respectively. The experimental  $(- / 0)$ ,  $(0 / +)$  levels and  $H^0 \rightarrow D^0$  barrier energies are 0.11, 0.0426, and 0.15 eV respectively.

The  $C_iO_iH$  complex has two paramagnetic states, with the  $R^0$  form more stable, and therefore, we investigated the character of the spin-density by analysing the Mulliken populations of the highest occupied band of the neutral defects.

In the R-form, the Mulliken bond populations show only  $\sim 0.5\%$  and  $\sim 0.1\%$  of the spin-density lying on C and H, and none on the oxygen atom. The vanishing spin-density on oxygen is striking and unexpected as the over-coordinated oxygen atom is the source of donor activity. We interpret this result in the following way. The anisotropic defect creates a compressive stress along the C-Si<sub>2</sub> bond which is rotated by  $22^\circ$  away from [010]. This stress will split the six conduction band valleys along cube directions, lowering the energy of the pair along [010] (the alignment of C-Si<sub>2</sub> in Fig. 6.3) relative to the other two pairs (Ramdas and Rodriguez, 1981). Figure 6.4 shows the band structure for the Si crystal folded into the 64 atom cell. The conduction band minima for Si lie near the folded X-points at  $\pm \frac{2\pi}{a_0} \langle \frac{1}{4} 00 \rangle$ . However, in the case when the defect occupies the unit cell, Fig 6.4 shows that the band close to the conduction band minima near  $\pm \frac{2\pi}{a_0} (0 \frac{1}{4} 0)$  is now pushed downward into the gap which we suggest is due to the compressive stress of the defect along (010). This strain leads to an effective-mass gap level localised on Si atoms and this explains why the resulting state has so little amplitude on C, H and O. In essence, the potential giving rise to the gap state is due to stress and not the chemical identity of the atoms making up the defect.

The partial occupation of the strain induced gap level is however dependent on the presence of these impurities. The C atom is fully saturated and cannot lead to any donor activity. Consider now the trivalent oxygen atom. One of the electrons in the lone pair on oxygen forms a bond with the Si<sub>2</sub> radical, leaving a single electron in an anti-bonding level. If this level lies *above* the gap state arising from the compressive stress of the defect, then the donor electron would drop into the stress induced defect level and lose its oxygen parentage. In this way, the lack of spin-density on oxygen is explained. The explanation is similar to the origin and behaviour of the double donor activity of the NL8 TDD( $N$ )

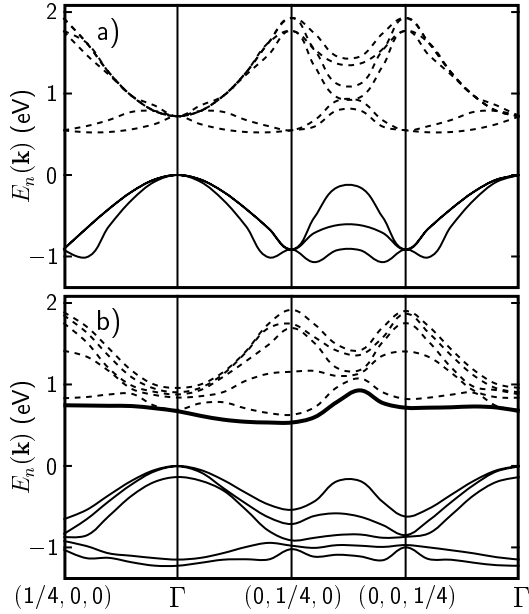


Figure 6.4: One-electron band structure for bulk Si (a), and the R-form of the neutral  $C_iO_iH$  defect (b) folded in 64 Si-atom supercells. All  $\mathbf{k}$  vectors are in  $2\pi/a_0$  units, where  $a_0 = 5.390 \text{ \AA}$  is the calculated Si lattice parameter. Alignment of the defect is as shown in Fig. 6.3. Solid and dashed lines represent filled and empty bands, where the highest half-filled band is emphasised as a thick branch in (b).

defect (Jones *et al.*, 2001).

In the neutral O-form, 30% of the spin-density lies on the  $Si_2$  radical. The wavefunction is composed of 15%  $s$  and 85%  $p$  (approximately parallel to  $[101]$ ) respectively. Smaller spin-densities of about 3-4% lie on both Si atoms bound to  $Si_2$  on the left hand side of Figure 6.3. Again, little spin-density is found on carbon or oxygen. Finally, we note that in both forms the C-H bond is aligned along  $\langle 110 \rangle$  — the same direction as the H-hyperfine interaction in D1.

We now turn to the local vibrational modes of the R and O forms given in Table 6.4. The first three rows give the modes localised mainly on C-H, C and O respectively. One of the most noticeable features is that the oxygen related mode is very sensitive to its bonding. In the ring structure (R-form) its LVM lies around  $720 \text{ cm}^{-1}$  but this increases to  $1010 \text{ cm}^{-1}$

for the O-form where it assumes its normal bond centred location. The C-H stretch mode lies around  $2700\text{ cm}^{-1}$  while two wag-modes are found around  $1000\text{ cm}^{-1}$  and are split by about  $80\text{-}100\text{ cm}^{-1}$ . Two carbon related modes lie around  $800$  and  $900\text{ cm}^{-1}$ , although these differ in the two forms, and four other less localised modes lie close to the Raman edge.

Calculations of  $^{18}\text{O}$  and  $^{12}\text{C}$  related isotopic shifts are shown in the second and third columns of numerical data. The oxygen related mode has shifts of  $29$  and  $43\text{ cm}^{-1}$  in the R and O-forms. In the deuterated case, a complicated reordering occurs, with a change in character in some of the modes. For this reason it has not been possible to give its downward isotopic shifts and Table 6.4 reports the calculated mode with starred values.

Of great significance is the  $1009.7\text{ cm}^{-1}$  oxygen related mode in the O-form which shifts  $3.1\text{ cm}^{-1}$  *upwards* with deuterium. This is close to a mode observed for the D-form of D1, described in the introduction, at  $1025.5\text{ cm}^{-1}$  which also shifts  $2.4\text{ cm}^{-1}$  upward with deuterium. We can now understand this anomalous shift as arising from a coupling with the undetected C-H wag mode at  $1027.4\text{ cm}^{-1}$ . In the deuterated defect, this wag mode shifts down to around  $900\text{ cm}^{-1}$  and below the oxygen related mode and hence the attempted crossing leads to an increase in the frequency of the oxygen related mode. Oxygen related modes usually possess large effective charges while the wag and stretch modes due to C-H have not been detected presumably because of the low values of their effective charges.

In summary, the  $\text{C}_i\text{O}_i\text{H}$  defect is bi-stable with donor and acceptor levels close to the shallow thermal donor D1 defect. The thermal stability, negative- $U$  character, and vibrational modes are consistent with an assignment to this defect which is also known to contain H.

### 6.3.2 Full passivation

The interaction between the  $\text{C}_i\text{O}_i\text{H}$  defect and a second H atom was also investigated. One would then expect that the two H atoms would passivate the Si and C radicals leading to an inert defect. Indeed, among several alternative structures, the lowest energy one is

Table 6.4: Local vibrational modes and their downward isotopic shifts ( $\text{cm}^{-1}$ ) for the R- and O-forms of  $\text{C}_i\text{O}_i\text{H}$ ,  $\text{C}_i\text{O}_i\text{H}_2$  and  $\text{C}_i\text{O}_{2i}\text{H}$  defects in the neutral charge state. For  $\text{C}_i\text{O}_i\text{H}$  and  $\text{C}_i\text{O}_{2i}\text{H}$ , the first, second and third rows correspond to modes which are mainly localised on C-H, C and O atoms respectively. For  $\text{C}_i\text{O}_i\text{H}_2$ , the second row gives modes localised on the Si-H unit, and the third and fourth rows list O and C-related modes. The last four frequencies in all defects correspond to modes mainly localised on Si atoms. Stared values list the actual frequencies of modes of mixed character and not their isotopic shift.

Defect	$^{12}\text{C}, ^{16}\text{O}, \text{H}$	$^{12}\text{C}, ^{18}\text{O}, \text{H}$	$^{13}\text{C}, ^{16}\text{O}, \text{H}$	$^{12}\text{C}, ^{16}\text{O}, \text{D}$
$\text{C}_i\text{O}_i\text{H}$ R-form	2754.4, 1072.3, 943.0	0.0, 0.3, 0.2	7.6, 8.7, 4.2	735.9, 978.5*, 782.3*
	933.3, 752.7	1.3, 5.1	22.1, 11.2	740.9*, 656.0*
	719.6	28.6	7.6	-1.6
	594.3, 563.3,	1.7, 4.5,	2.9, 0.6,	3.9, 0.9,
	544.6, 530.5	0.2, 1.5	0.2, 1.0	6.4, 3.0
$\text{C}_i\text{O}_i\text{H}$ O-form	2767.9, 1027.4, 947.9	0.0, 2.1, 0.1	7.8, 7.1, 3.9	739.9, 924.5*, 815.4*
	881.4, 790.1	0.3, 0.1	21.0, 20.1	704.8*, 665.2*
	1009.7	42.7	0.9	-3.1
	639.7, 586.9,	6.4, 0.1,	0.2, 4.6,	0.1, 4.7,
	549.1, 531.8	0.0, 0.1	0.2, 0.4	4.7, 3.2
$\text{C}_i\text{O}_i\text{H}_2$	2723.4, 1032.4, 964.1	0.0, 1.1, 0.0	7.6, 9.0, 5.1	727.7, 927.1*, 839.6*
	1982.3, 772.5, 719.3	0.0, 0.0, 0.0	0.1, 6.0, 0.1	561.3, 701.8*, 672.1*
	997.9	43.3	0.2	-2.5
	878.9, 817.4	0.3, 0.1	18.3, 16.0	634.7*, 586.3*
	635.1, 588.0,	6.5, 0.1,	0.2, 3.7,	0.1, 1.5,
560.2, 534.0	0.0, 0.1	0.8, 0.3	7.5, 3.6	
$\text{C}_i\text{O}_{2i}\text{H}$	2730.5, 954.6, 943.6	0.0, 2.5, 0.9	7.6, 10.5, 13.7	729.7, 999.5*, 792.1*
	1079.9, 756.9	0.5, 1.9	10.4, 17.3	737.7*, 673.0*
	1004.1, 811.3	44.6, 33.3	0.1, 2.5	-0.1, -3.4
	670.1, 569.5	12.1, 11.6	0.5, 1.4	2.1, 1.0
	593.0, 549.0	1.6, 5.8	3.4, 0.1	4.0, 0.4

where the second hydrogen atom binds to the  $\text{Si}_2$  radical in Figure 6.3 (O-form) on the opposite side of the oxygen atom. The alternative, where H binds to  $\text{Si}_2$  nearby the oxygen is 0.6 eV higher in energy. There are then no donor or acceptor levels and the defect is fully passivated. The oxygen atom is bound to  $\text{C}_i\text{H}_2$  with an energy of 1.4 eV, while the second H atom is bound with an energy of  $\sim 2.5$  eV.

Table 6.4 gives the LVMS for the defect. These are similar to the O-form of  $\text{C}_i\text{O}_i\text{H}$ , but there are three additional Si-H related stretch and bend modes at 1982, 773 and 719  $\text{cm}^{-1}$ . The O-mode is now close to 1000  $\text{cm}^{-1}$  reflecting its divalent character. The lower carbon mode at 817  $\text{cm}^{-1}$  is pushed up by coupling with the Si-H wag modes. As for the singly hydrogenated complex, deuteration results in a cross-over and mixing of several modes. The C-H mode at 1032  $\text{cm}^{-1}$  falls below the oxygen mode which is consequently displaced upwards from 998 to 1000  $\text{cm}^{-1}$  in a similar manner to the  $\text{C}_i\text{O}_i\text{H}$  defect.

## 6.4 Further oxygen aggregation

We briefly describe the effect of adding a second oxygen atom to  $\text{C}_i\text{O}_i\text{H}$ . There are now a greater number of candidate structures but among those investigated, the ones with the additional O-atom lying in the same ( $\bar{1}01$ ) plane as  $\text{C}_i\text{O}_i$  are energetically favorable. Several ring (R) and open (O) structures have low formation energies and are shown in Fig. 6.5. The  $\text{O}'$  structure was proposed previously as a candidate for a H-related shallow thermal donor (Ewels *et al.*, 1996*a,b*).

The energies of all these forms are listed in Table 6.5. Defects in the positive, neutral and negative charge states were considered. Once again, the R-form is found to be the ground state configuration for the neutral and positively charged states, whereas the O-form is stable in the negative charge state. Forms  $\text{R}'$  and  $\text{O}'$  are metastable by  $\sim 0.5$  eV, with a slight preference for the asymmetric  $\text{R}'$ -form.

The electronic levels were evaluated for the R and O forms. Again, the former is a shallow donor with a calculated level at  $E_c - 0.01$  eV. The O-form has a deep ( $-/0$ ) level at  $E_c - 0.3$  eV, and the barrier for the  $\text{O}^0 \rightarrow \text{R}^0$  transition is only 0.02 eV. However, the

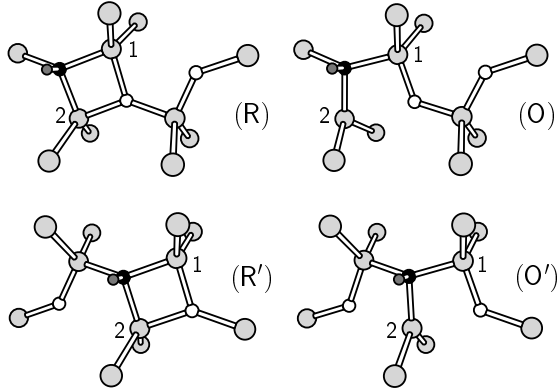


Figure 6.5: Structures for  $C_iO_{2i}H$  considered in our study. Gray, black, white atoms are Si, C, O. The small gray atom is H. Relative energies are listed in Table 6.5.

Table 6.5: Relative energies (eV) for four  $C_iO_{2i}H$  structures R, O, R' and O' shown in Figure 6.5. NS stand for Not Stable.

Charge state	+	0	-
R	0.00	0.00	NS
O	NS	0.56	0.00
R'	0.37	0.45	NS
O'	0.61	0.56	NS

$O^0$ -form is now metastable by 0.56 eV compared with 0.17 eV for  $C_iO_iH$ . This shows that the thermodynamic  $(-/0)$  level is now above the conduction band bottom and hence the defect can never be prepared in the negative charge state. These results are summarized in Fig. 6.6. Thus  $C_iO_{2i}H$  is *not* bi-stable.

Our conclusions are then that the ring form is stabilized in  $C_iO_{2i}H$  which can only be a shallow donor defect. This is consistent with an assignment to D2, and therefore to STD(H)2, as this defect is not known to be bi-stable.

The LVMs of the  $R^0$  are given in Table 6.4. The C-H stretch mode lies around  $2700\text{ cm}^{-1}$ , well above a series of strongly coupled C-H modes. Two O-modes appear at 1080 and



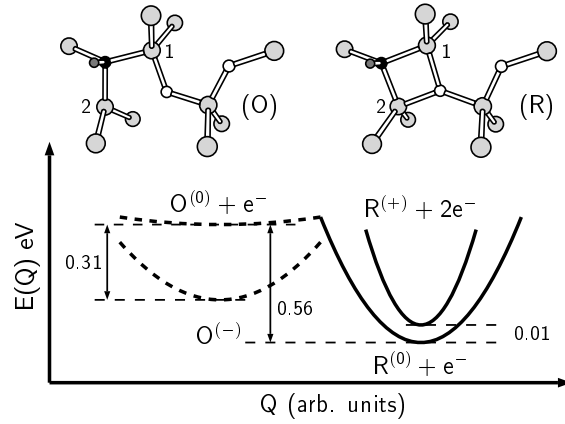


Figure 6.6: Configurational diagram for the  $C_iO_{2i}H$  defect. Dashed potential curves indicate that the O-form is unstable under thermodynamic equilibrium – the  $C_iO_{2i}H$  complex is a single shallow donor.

$757\text{ cm}^{-1}$ , consistent with the presence of a divalent and trivalent oxygen. Modes around  $600\text{ cm}^{-1}$  also shift considerably with  $^{18}\text{O}$  substitution. These are similar to a low frequency pair also found in the interstitial oxygen dimer (Coutinho *et al.*, 2000b; Öberg *et al.*, 1998; Pesola *et al.*, 1999b).

## 6.5 Summary

It is found that the IR-activity from the  $C_iO_i$  defect can be divided into three sets of bands classified according to their isotopic shifts. The carbon-related  $1116$  and  $865\text{ cm}^{-1}$ -bands, the oxygen  $742\text{ cm}^{-1}$ -band, and the four low frequency  $585$ ,  $550$ ,  $540$ ,  $529\text{ cm}^{-1}$ -bands, where the  $585$  and  $540\text{ cm}^{-1}$ -bands have not been reported previously. Of particular interest is the position and  $^{18}\text{O}$  isotopic shift observed for the  $742\text{ cm}^{-1}$ -band ( $33.4\text{ cm}^{-1}$ ), much less pronounced than that of  $O_i$  ( $51.4\text{ cm}^{-1}$ ) (Pajot *et al.*, 1995). There is evidence for absorption bands with similar character related to the thermal double donors in Si. These lie at  $\sim 720\text{ cm}^{-1}$  and shift by  $\sim 24\text{ cm}^{-1}$  in  $^{18}\text{O}$  rich samples (Lindström and Hallberg, 1994, 1996). These observations favor here a different bonding of oxygen, as an alternative to is *normal* bond-centered location.

The calculations have shown that the  $C_iO_i$  defect has a ring structure involving an over-coordinated oxygen atom. The weak oxygen bonding then leads to the highest oxygen related vibrational band lying around  $720\text{ cm}^{-1}$  and far from the  $1136\text{ cm}^{-1}$ -band of interstitial oxygen. This supports previous studies of the defect (Jones and Öberg, 1992; Snyder *et al.*, 1996). This mode is relatively unaffected when H is added to the defect and appears to be a signature for this type of oxygen. All seven observed band frequencies and their isotopic shifts are remarkably well described by the model. The calculated donor level and energy-stress tensor are also in good agreement with the measured values.

The defect can trap one or two H atoms and is electrically inert in the latter. The single hydrogenated center has remarkable properties. It is bi-stable, *i.e.*, the negative charge state has a divalent oxygen atom, whereas in the positively charged defect the oxygen is over-coordinated. The effective ionisation correlation term,  $U$ , is negative and a shallow donor level lies  $0.05\text{ eV}$  above a deep acceptor.

None of the calculated levels are in agreement with an assignment to the hole trap H4 at  $E_v + 0.28$  (Feklisova *et al.*, 1999). On the other hand the  $C_iO_iH$  defect has similar properties to the first species of a family of shallow donors, labelled  $DN$ , found in irradiated Si (Markevich *et al.*, 1994, 1998a, 1995, 1997b,a, 1998b). D2 and D3 have been associated with the shallow thermal donor defects STD(H)2 and STD(H)3 (Newman *et al.*, 1998; Markevich *et al.*, 1998a). The energy levels, the oxygen related vibrational mode and its shift with hydrogen are all consistent with an assignment of  $C_iO_iH$  and  $C_iO_{2i}H$  with D1 and D2 respectively. The negligible spin-densities on C, H and O and the alignment of the C-H bond along  $[\bar{1}01]$  are consistent with ENDOR results. However, to our knowledge, no  $DN$  defects have been detected in H-plasma or wet chemical etched and irradiated Cz-Si samples. Moreover, the presence of carbon and oxygen in the defects remains to be verified by a spectroscopic technique. According to the calculations, the ground state for the effective-mass  $R^0$  defect is localized on a strain induced gap level mainly localized on Si atoms. The donor character originates from the over-coordinated oxygen atom which possesses a level higher up in energy. The electron in this level then falls into the strain induced gap level. Thus the character of the spin-density of the donor level does not reflect

its oxygen parentage and this is consistent with the ENDOR studies. Thus, as for the NL8 thermal double donor defects, the chemical composition of the  $DN$  and  $STD(H)N$  families may be difficult to determine by magnetic resonance.

Finally, we point out that other STD models could be obtained by substituting the  $C_i$ -H unit in  $C_iO_{ni}H$  defects by a group III atom, or indeed a complex with equivalent coordination. In particular, Al and N are obvious candidates for the  $STD(Al)$  and  $STD(X)$  families (Gregorkiewicz *et al.*, 1988).

## Chapter 7

# Concluding remarks

For a long time it was believed that a self-interstitial is inevitably produced when two O-atoms cluster. The argument was based on the volume of a SiO<sub>2</sub> quartz unit which is  $\sim 2.25\times$  the volume of a host Si atom. Here it is shown that O-atoms can be accommodated in the Si matrix by bending their Si-O-Si units. Only clusters of at least four O-atoms are expected to produce self-interstitials. Moreover, due to the high formation energy of self-interstitial defects, we conclude that these do not form during the early stages of TDD formation (Coutinho *et al.*, 2000a).

In collaboration with experimental groups, the VOH<sub>2</sub> defect has been identified by means of IR-spectroscopy (Markevich *et al.*, 2000). This defect is responsible for three LVM-bands, two H-related and one O-related at 2151, 2126 and 943 cm<sup>-1</sup> respectively. The singly hydrogenated VO has not been detected by IR, but one electron and one hole trap were linked to the defect. The calculations support these assignments

The well known interstitial oxygen defect has been reviewed in detail. In Si, it was found that its potential around the bond centre site varies only by  $\sim 10$  meV between the bond-centre ( $D_{3d}$  symmetry) and puckered configurations ( $C_2$  and  $C_{1h}$  symmetry). This is flat enough to allow the defect to tunnel between these configurations at room temperature. In Ge, the situation is somewhat different, with the BC-form considerably higher in energy, so that the defect tunnels only between the puckered forms. Two local

vibrational modes (symmetric and asymmetric stretch) were found, and their combination supports the assignment of the  $1750\text{ cm}^{-1}$ -band to a phonon replica (Coutinho *et al.*, 2000*b*).

The effect of hydrostatic pressure on the local modes and structure of  $O_i$  and the oxygen dimer has been considered. We found that puckered Si-O-Si units are favoured in the high pressure regime, explaining the trends of the asymmetric-mode frequency in high-pressure measurements. Similar arguments were presented to explain the anomalous temperature-shifts suffered by the O-dimer bands (Coutinho *et al.*, 2000*b*).

We investigated previous suggestions that the oxygen dimer could act as a fast oxygen carrier. Its migration barrier was estimated to be  $\sim 1\text{ eV}$  lower than that of the single interstitial oxygen (2.5 eV). Further investigations revealed that the oxygen trimer and larger aggregates can diffuse through even lower barriers, explaining the fast TDD transformation process. These results are vital to the all oxygen aggregation process. If the dimer was the only fast-diffusing species, soon it would reach extinction after being captured by dominant  $O_i$  centres (Jones *et al.*, 2001).

Regarding the structure and composition of TDD defects, we started by investigating the model preferred by experimentalists — the self-interstitial-oxygen model. Here it was shown that a self-interstitial defect is only marginally stable when bound to an oxygen precipitate, and therefore these defects are not expected to survive to temperatures where TDD's form. These conclusions are supported by experiments, where  $IO_n$  complexes are observed to break below  $200^\circ\text{C}$ . On the other hand, a strong candidate for an  $IO_2$  defect was presented. In this model, an O-dimer and a split-interstitial are bound by only 0.7 eV, and the calculated LVM frequencies are in good agreement with the measurements.

The revelation that the infinite 2NN chain is an insulating sub-oxide presents a definite breakthrough. From ENDOR measurements, we know that the donor electron avoids the TDD core. An electrically inactive core is therefore a *desired* property for the model. In fact, the repulsive core makes the task of experimentalists very difficult. Here we present a novel model for the TDD defects based on electron transfer. The insulating core produces a *stress-induced* empty state overlapping neighbouring Si atoms, lying below

those produced by over-coordinated oxygens at the ends. Electrons from the later then drop into the former, lose their oxygen parentage, and therefore explain the ENDOR data (Jones *et al.*, 2001; Coutinho *et al.*, 2001*b*).

The model is also consistent with electronic IR-data, where the effective strain along [001] decreases with the chain length. This suggests a decreasing deformation potential for the stress-induced state, and hence a decrease of the ground state binding energy. This trend is also reproduced by the stress-energy tensor. Of particular importance are the results from a collaboration with an experimental group. At most three distinct vibrational bands were observed for each donor, all well accounted by the model. In Si, the high-frequency band at  $\sim 1000\text{ cm}^{-1}$  is localised at the ends, and does not produce new modes in the mixed  $^{16}\text{O}$ - $^{18}\text{O}$  isotopic samples. This is not the case for the  $\sim 720\text{ cm}^{-1}$  and  $\sim 580\text{ cm}^{-1}$ -bands, which are localised at the core O and Si atoms respectively. In Ge, the picture is similar, but due to the more pronounced buckled ends, both O-related modes couple several O-atoms (Murin *et al.*, 2001).

The shallow thermal donors were also investigated. Here we focused on the STD defects containing hydrogen. In view of recent experimental progress, we assigned a  $\text{C}_i\text{O}_i\text{H}$  interstitial complex to a shallow donor labelled D1, believed to be a precursor for the STD(H) family. This defect is of particular interest as it displays bi-stability with negative- $U$  ordering of ionisation energies. We found that a large local distortion coupled with a strong change in the electronic structure triggers this phenomenon. In the negative charge state the oxygen atom is two-fold coordinated, but in the positive defect the O-atom is over-coordinated (Coutinho *et al.*, 2001*a*). These structures are consistent with the observed  $1025\text{ cm}^{-1}$ -band for the  $\text{D1}^-$ , and its disappearance for  $\text{D1}^+$ . In the latter case, the band is expected to fall in the  $700\text{ cm}^{-1}$  region. Unfortunately this band escaped detection. These results support a previous suggestion by Ewels *et al.* (1996*a*), where a model for the STD(H) family containing a carbon atom was put forward.

I should now conclude with some remarks regarding some problems still unsolved. The interaction between self-interstitials and oxygen is a technologically important problem. There is much work to be done here, with the most *fundamental* defects such as the single

interstitial or the  $IO_i$  complex unresolved. The interest in these problems stems from the fact that in large scale integration technology, implantation of dopants is an important issue. This is especially the case for packed materials such as SiC or diamond, where in-diffusion is not an option. The  $IO_2$  complex has an acceptor level at  $E_c - 0.11$  eV. However, only LVMs for the neutral defect were observed. We expect that the defect will change its structure after trapping an electron.

In Chapter 5 we saw how hydrogen can effectively interact with the O-2NN chains. This interaction can itself be used to test the model experimentally. First, the Si-H bonds should produce IR-active LVM bands, and secondly it is expected the doubly hydrogenated complex to act as an acceptor with an electron trap  $\sim 150$  meV below the conduction band. Such observation would provide convincing evidence for the strain-induced state. The capture cross section for the donor model should display a large anisotropy along directions orthogonal and along the (110) plane. This feature has been observed after measurements of a Poole-Frenkel effect with different orientations of the electric field (Michel and Kimerling, 1994). However, the trends of the capture cross section could also be measured for different stages of TDD( $N$ ) formation. This would allow us to compare the approximately linear dependence of the capture cross section with  $N$ , for the O-2NN chain.

Effective-mass theory has proven to be effective in modelling shallow states. A description of the TDD model within EMT, which takes into account the microscopic features of the chain, is expected to provide extra information, especially the trends and splittings of the energy levels. Extensive IR-absorption data is available, awaiting for comparison with the theory.

The O-2NN model also predicts IR-active bands which have not yet been observed. This is an obvious track that should be pursued by experiment. It is possible that these modes are affected by strong broadening due to short life-times, and therefore difficult to detect. Another possibility is the fact that the Si samples possess a strong background absorption due to free-carriers between  $\sim 600$  and  $\sim 800$   $\text{cm}^{-1}$ , hiding the TDD-related LVMs.

The  $C_iO_iH$  and  $C_iO_{2i}H$  complexes were assigned to D1 and D2 [or STD(H)2] defects. Here

we give detailed insight about the mechanism that triggers bi-stability, i.e., the switching between three-fold and two-fold coordinated oxygen atoms. Several results lead us to suggest the assignment of D1 to the  $C_iO_iH$  complex. These include the LVMs, electrical levels and their negative correlation. The presence of carbon is assumed on the basis of such observations.

Although we only dealt with the hydrogen-related shallow thermal donors, much work has also to be done on other families. This is the case of the STD(Al) and STD( $X$ ), where  $X$  is still unknown. Until now, only oxygen, aluminium and hydrogen have been detected by ENDOR. Unfortunately, as for the TDD defects, we anticipate a negligible amplitude of the donor wavefunction at the core. This feature seems to be the very reason for our poor understating of TD's after so many years of research effort. We need then to find alternative ways to probe these defects.

Finally, I would like to stress the enormous success resulting from the close collaboration between theorists and experimentalists. Fruitful discussions and suggestions were very much responsible for the results reported here.



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