The Plasma frequency of Caesium

Caesium is a body centred cubic metal.

Each atom donates one electron to the conduction band.

The cube spacing of caesium is 6.05×10^{-10} m.

From this information determine the plasma wavelength of caesium.

Solution:

Bcc, therefore 2 atoms per unit cell.

Each atom contributes one electron to the conduction band.

Therefore the electron density N is given as:

$$N=2/(6.05\times10^{-10})^3 = 9.031\times10^{27} \text{ m}^{-3}$$

Therefore the plasma frequency ω_p is given by:

$$\begin{split} \omega_{\rm p} &= ({\rm Ne}^{2}/{\rm m}\epsilon_{0})^{1/2} \\ &= [9.031 \times 10^{-27} \times (1.6 \times 10^{-19})^{-2}]/[9.1 \times 10^{-31} \times 8.8 \times 10^{-12}] \ {\rm s}^{-1} \\ &\qquad \omega_{\rm p} = 5.37 \times 10^{-15} \ {\rm s}^{-1} \\ &\qquad \lambda = 2\pi c/\omega_{\rm p} = 351 \ {\rm nm} \end{split}$$