Problem

An infinite plane in empty space carries a uniform surface charge σ . Find the electric field.

Solution:

Draw a Gaussian 'Pillbox' extending equal distances above and below the plane:

Apply Gauss's law to the box.

$$\oint E \cdot da = \frac{1}{\varepsilon_0} Q_{enc}$$

In this case $Q_{enc} = \sigma A$ where A is the area of the lid of the 'pillbox'.

$$\int E \cdot da = 2A/E/$$

The sides contribute nothing.

$$E = \frac{\sigma}{2\varepsilon_0}\hat{n}$$